

The HI-to-H₂ Transition and HI columns in Galaxy Star-Forming Regions

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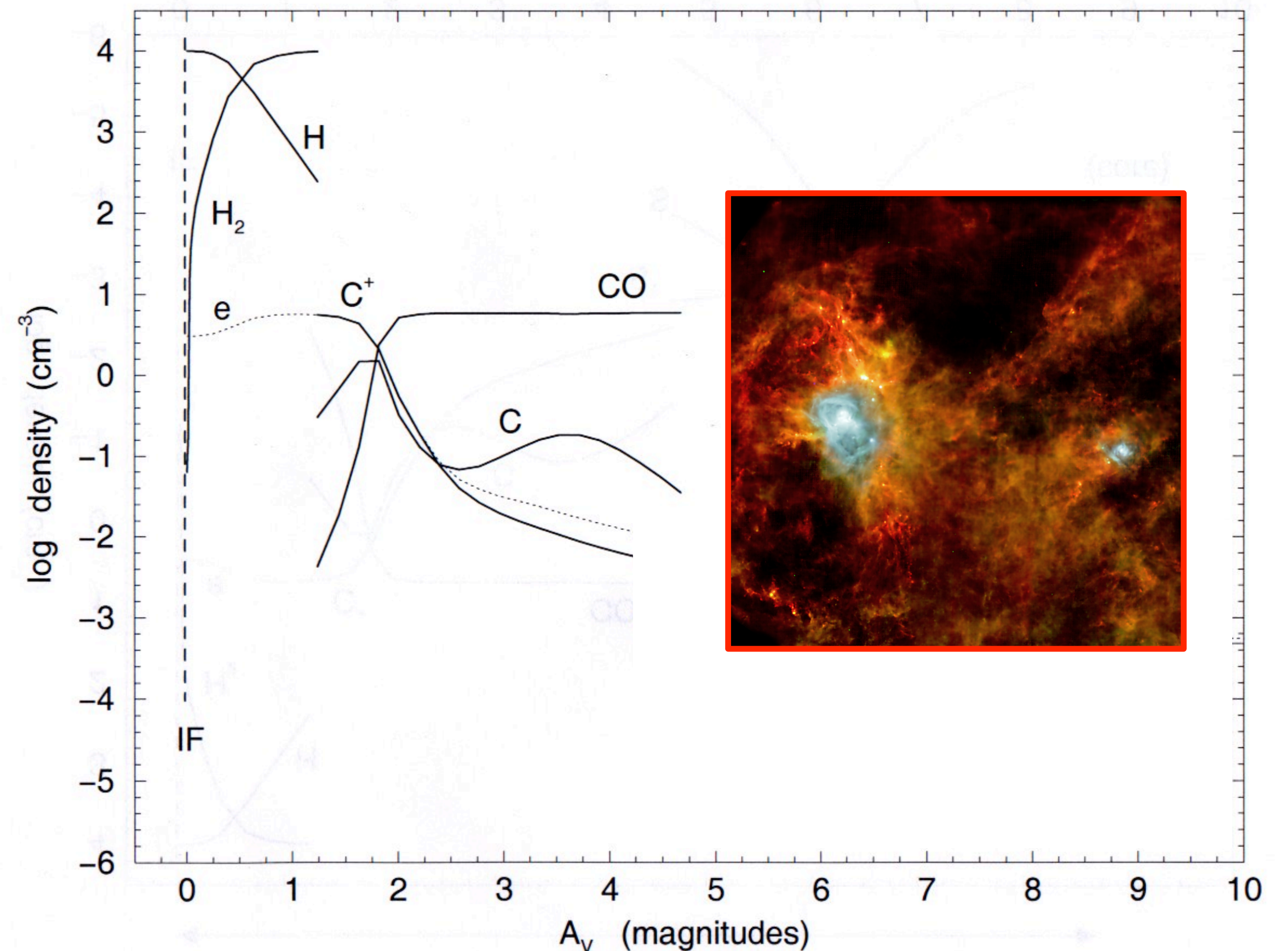
Star Formation Across Space and Time
14 November 2014



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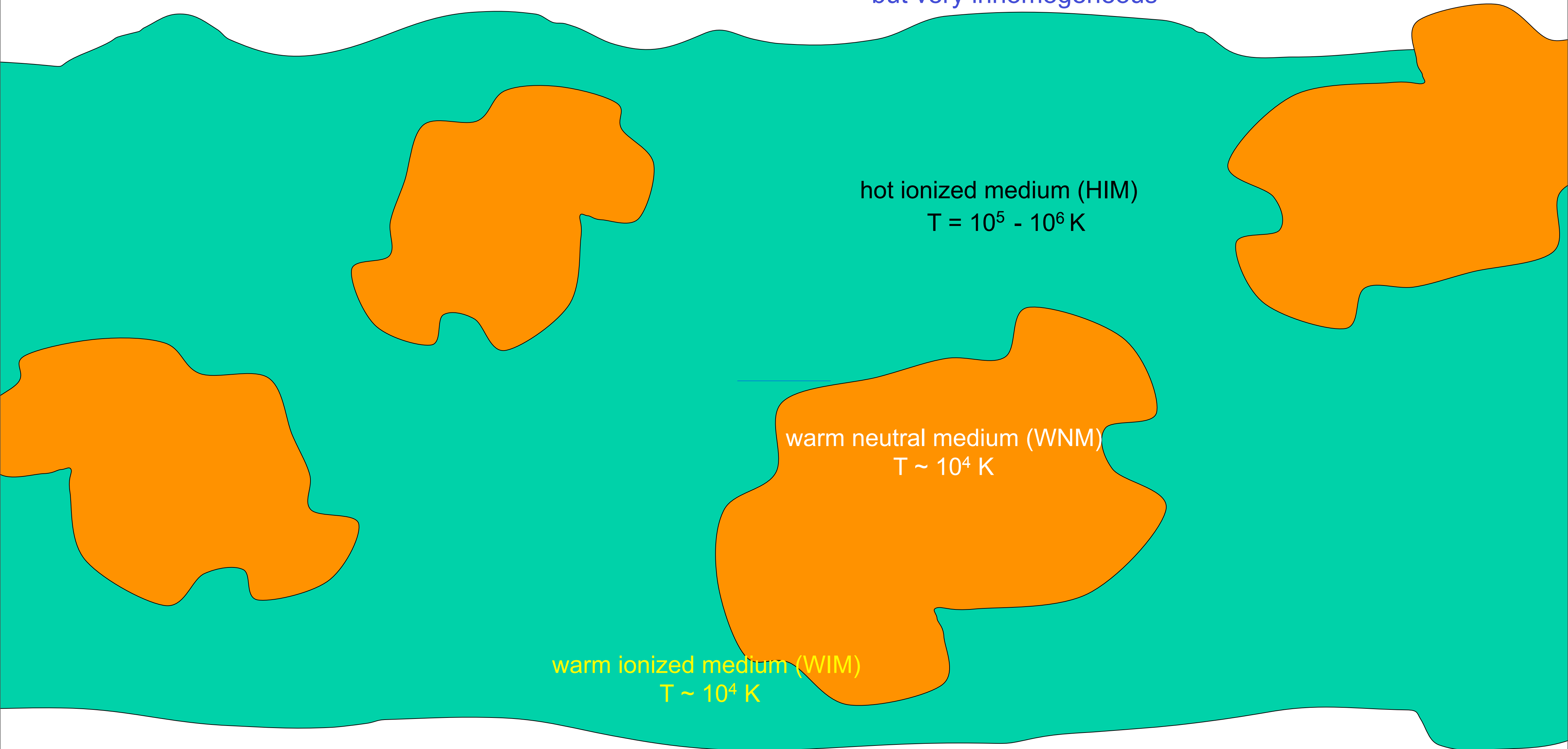
The Multi-Phased Interstellar Medium (ISM) and Star-Formation:

<density> = 1 cm^{-3}
but very inhomogeneous

hot ionized medium (HIM)
 $T = 10^5 - 10^6 \text{ K}$

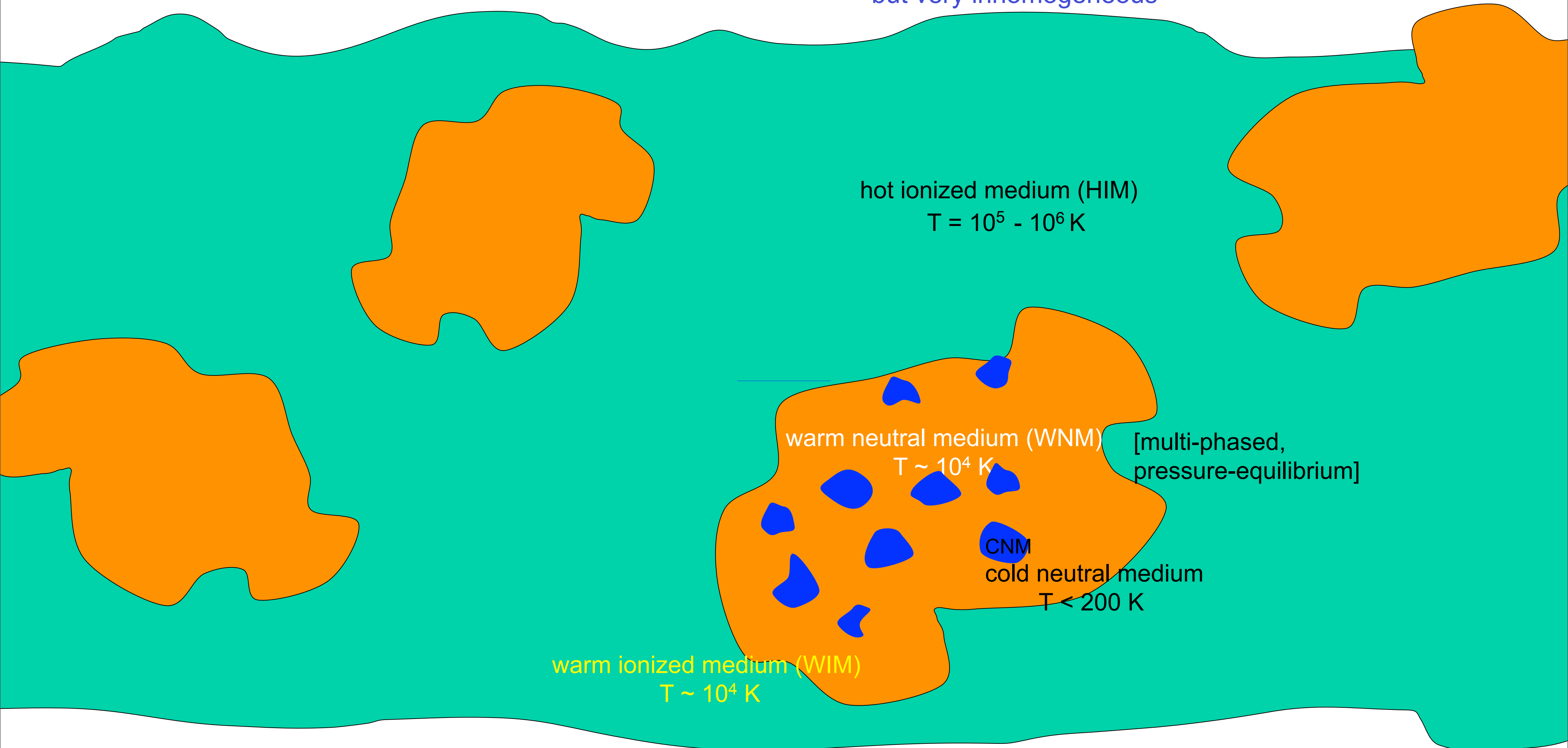
warm neutral medium (WNM)
 $T \sim 10^4 \text{ K}$

warm ionized medium (WIM)
 $T \sim 10^4 \text{ K}$



The Multi-Phased Interstellar Medium (ISM) and Star-Formation:

$\langle \text{density} \rangle = 1 \text{ cm}^{-3}$
but very inhomogeneous



The Multi-Phased Interstellar Medium (ISM) and Star-Formation:

Interstellar gas exposed to

starlight
shock waves
energetic particles (cosmic-rays)
magnetic fields

Global ISM heated and energized by stars
(outflows, radiation, and supernova explosions).

Turbulent!

Total Galactic ISM mass = $5 \times 10^9 M_{\odot}$

Mid-plane thermal pressure = $2.5 \times 10^3 \text{ cm}^{-3} \text{ K}$
(at Solar circle)

95% of mass in cold neutral hydrogen phase
95% of volume in warm/hot ionized phase.

$\langle \text{density} \rangle = 1 \text{ cm}^{-3}$
but very inhomogeneous

hot ionized medium (HIM)
 $T = 10^5 - 10^6 \text{ K}$

warm neutral medium (WNM)
 $T \sim 10^4 \text{ K}$

[multi-phased,
pressure-equilibrium]

CNM
cold neutral medium
 $T < 200 \text{ K}$

warm ionized medium (WIM)
 $T \sim 10^4 \text{ K}$

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95% of mass in cold neutral hydrogen phase
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stars form in cold molecular (H_2) clouds:
Galactic star-formation rate $\sim 3 M_{\odot} \text{ yr}^{-1}$

$\langle \text{density} \rangle = 1 \text{ cm}^{-3}$
but very inhomogeneous

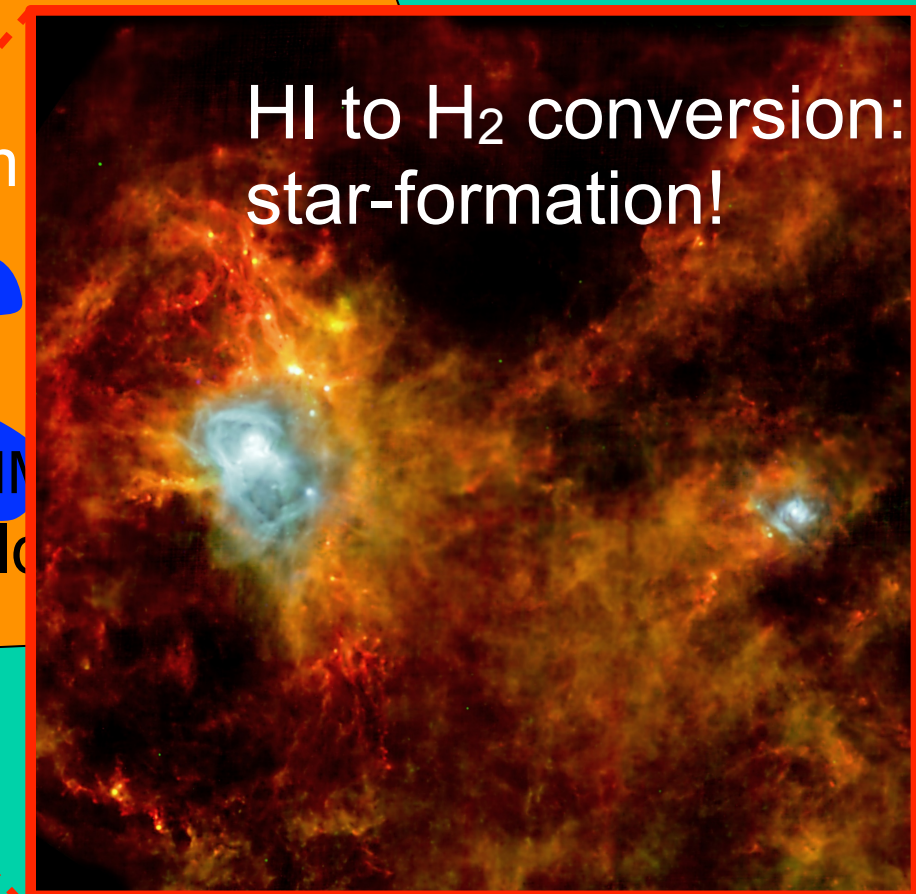
hot ionized medium (HIM)
 $T = 10^5 - 10^6 \text{ K}$

warm neutral medium
 $T \sim 10^4 \text{ K}$

warm ionized medium (WIM)
 $T \sim 10^4 \text{ K}$

HI to H_2 conversion:
star-formation!

Herschel views Aquila



Talk Outline:

- motivation.
- HI-to-H₂ transition, some radiative transfer computations.
- analytic formula for the HI column density.
- self-regulated media.
- observations: from Perseus to galaxies.

HI-to-H₂ Transitions and HI Column Densities in Galaxy Star-Forming Regions

Amiel Sternberg¹, Franck Le Petit², Evelyne Roueff,² and Jacques Le Bourlot²

2014 ApJ 790 10



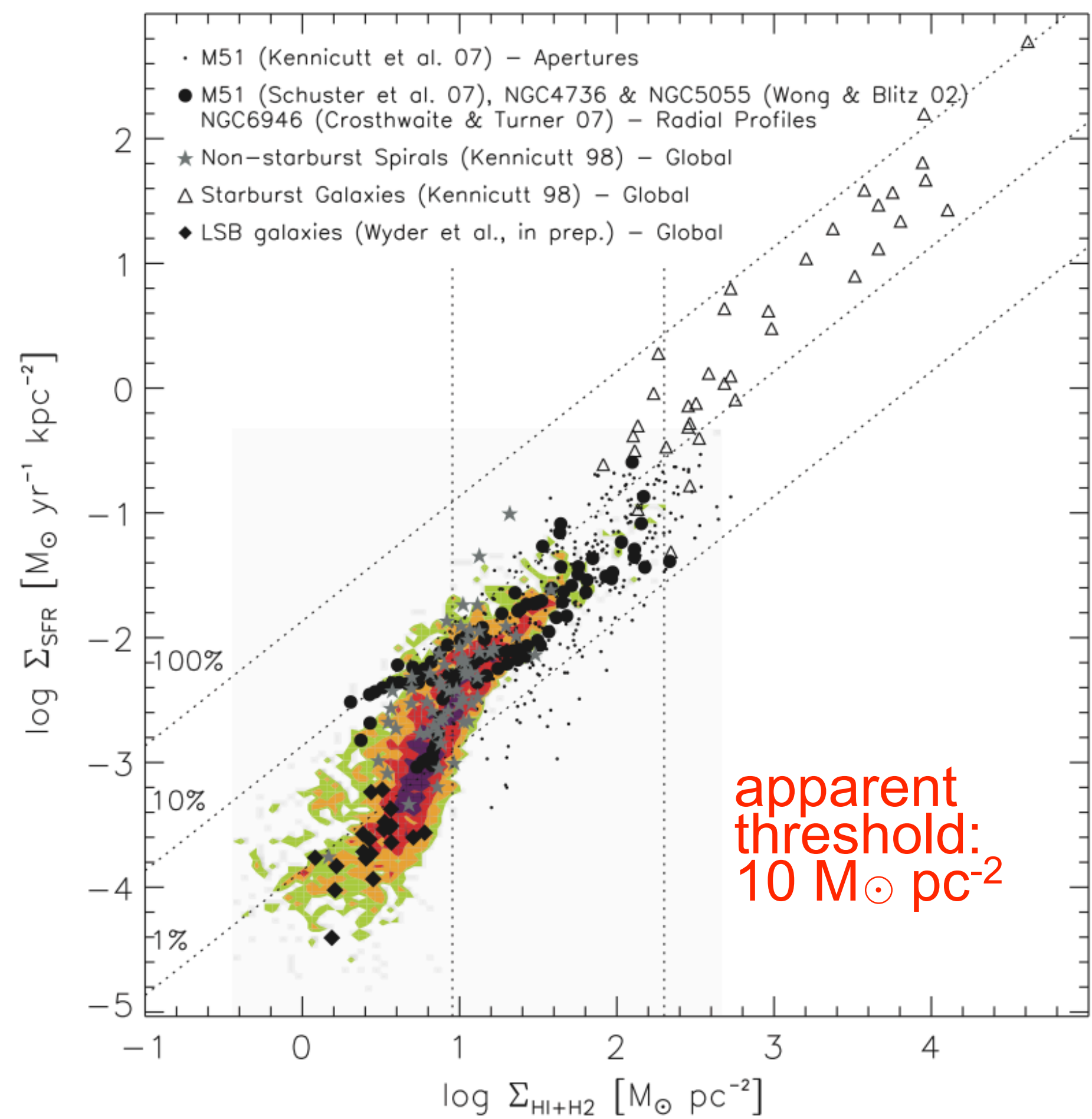
Kennicutt-Schmidt Relation:

Schmidt 1959 ApJ 129 253

Kennicutt 1998 ApJ498 541

Genzel et al. 2010 MNRAS 407 2091 [“SINS(VLT)/IRAM” projects]

e.g., Bigiel+ 2008



$$\Sigma_{\text{SFR}} = \epsilon \frac{f_{\text{H}_2} \Sigma_{\text{gas}}}{\tau_d}$$

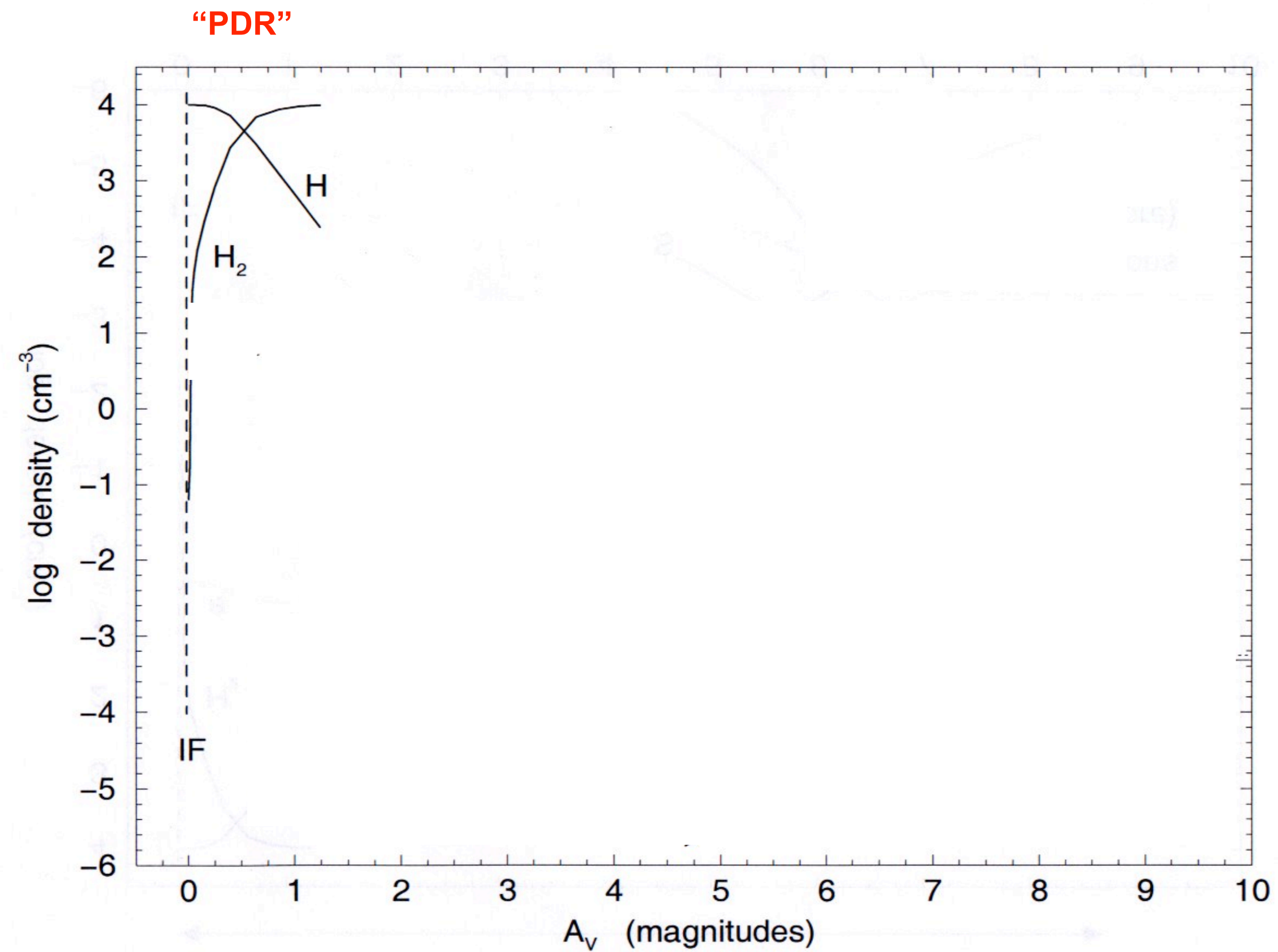
I am going to be juggling many parameters
- keep your eye on them!



HI to H₂ Transition in Dense Star-Forming Molecular Clouds:

H₂ formation (by grain catalysis) versus far-UV photodissociation.

Shielding required.

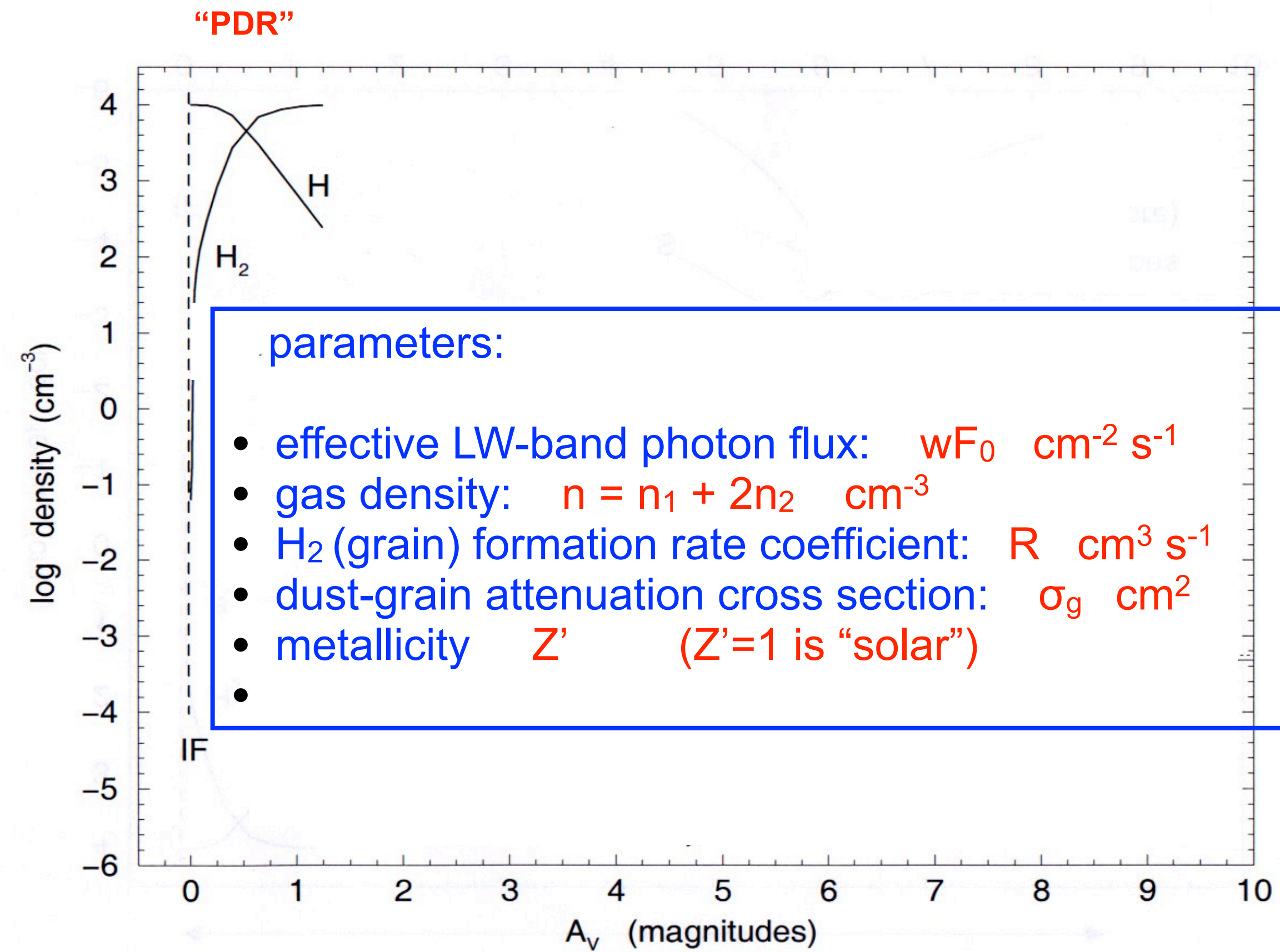


Stellar ultraviolet
“Lyman-Werner” radiation
11.2 - 13.6 eV

HI to H₂ Transition in Dense Star-Forming Molecular Clouds:

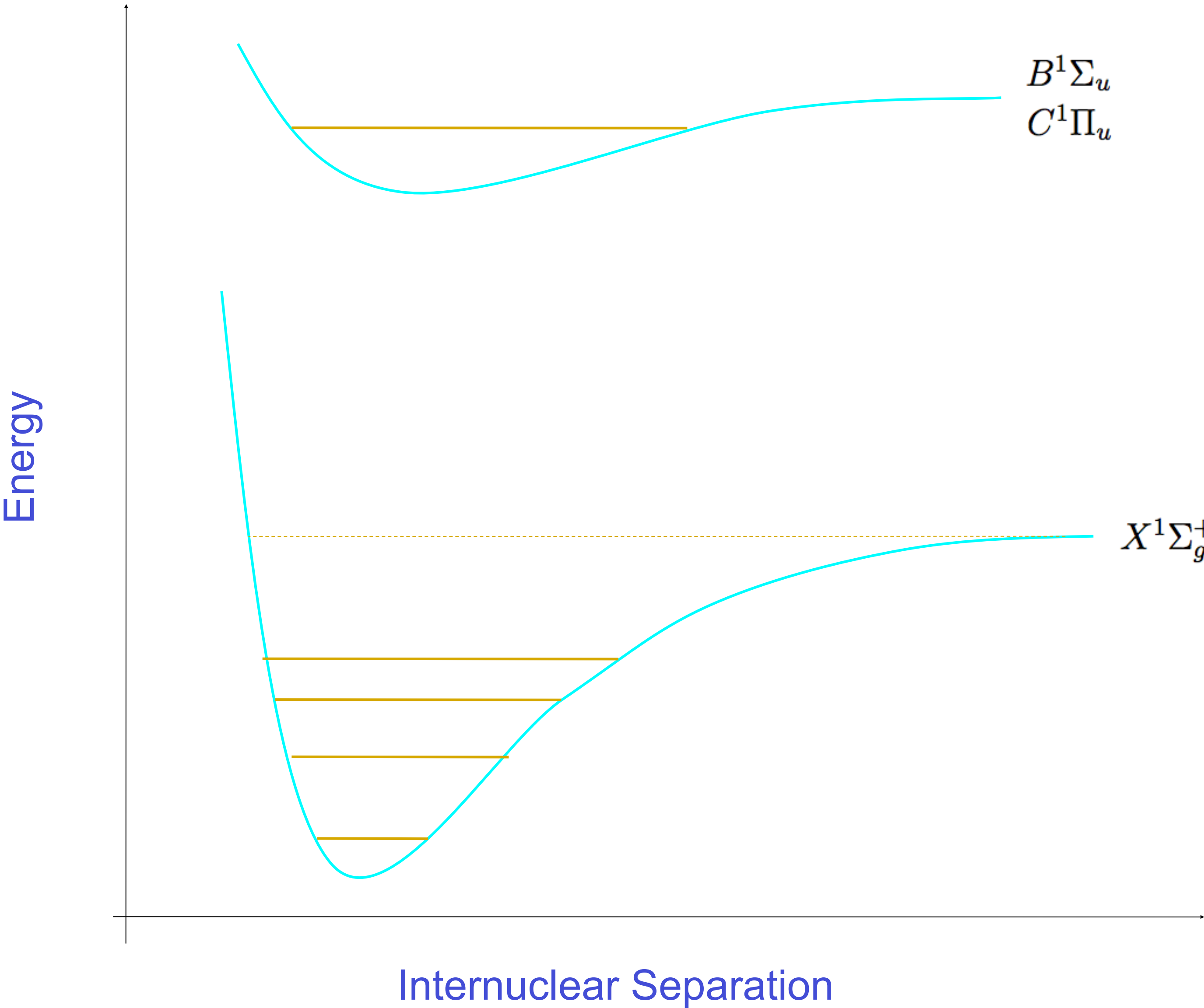
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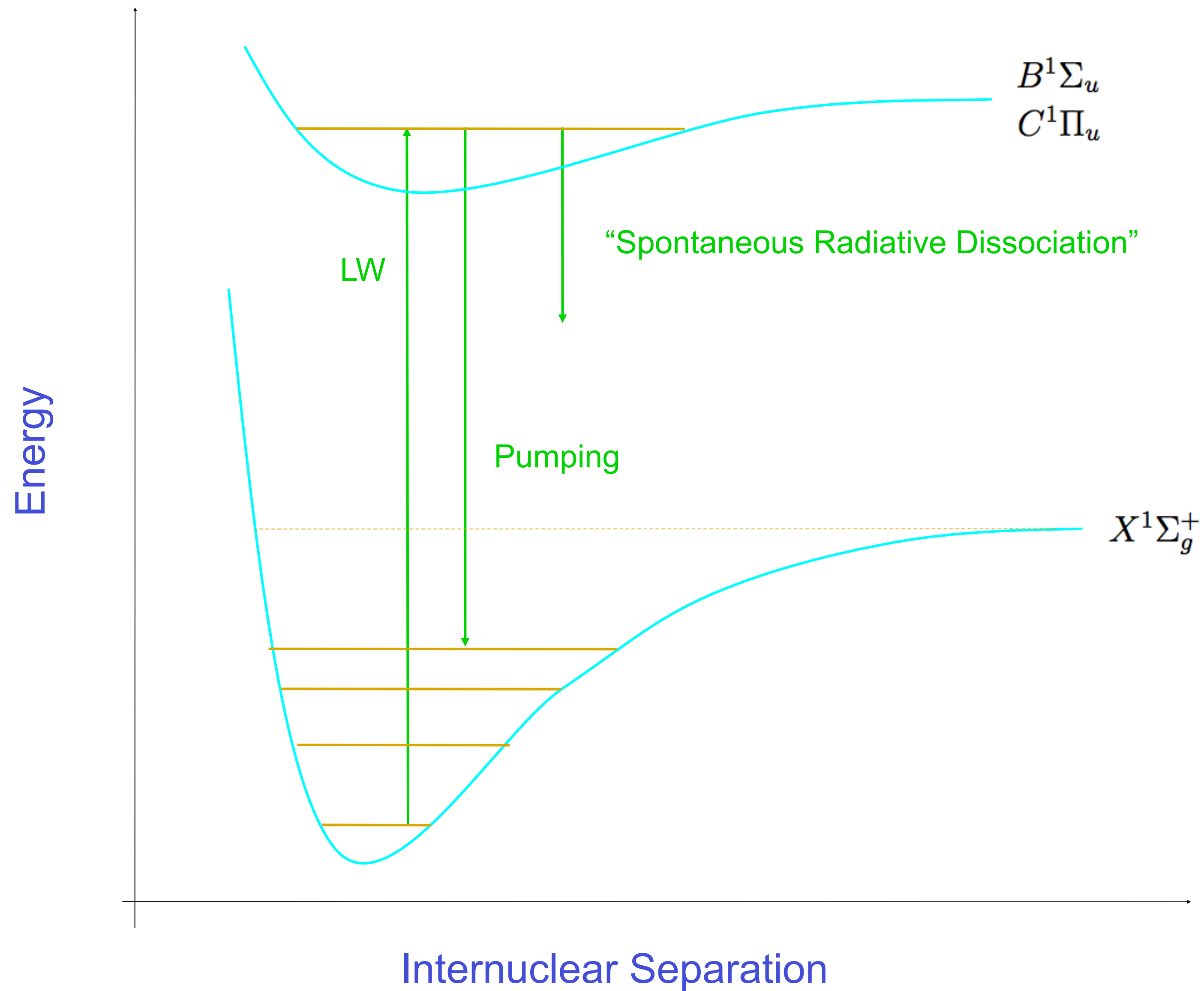


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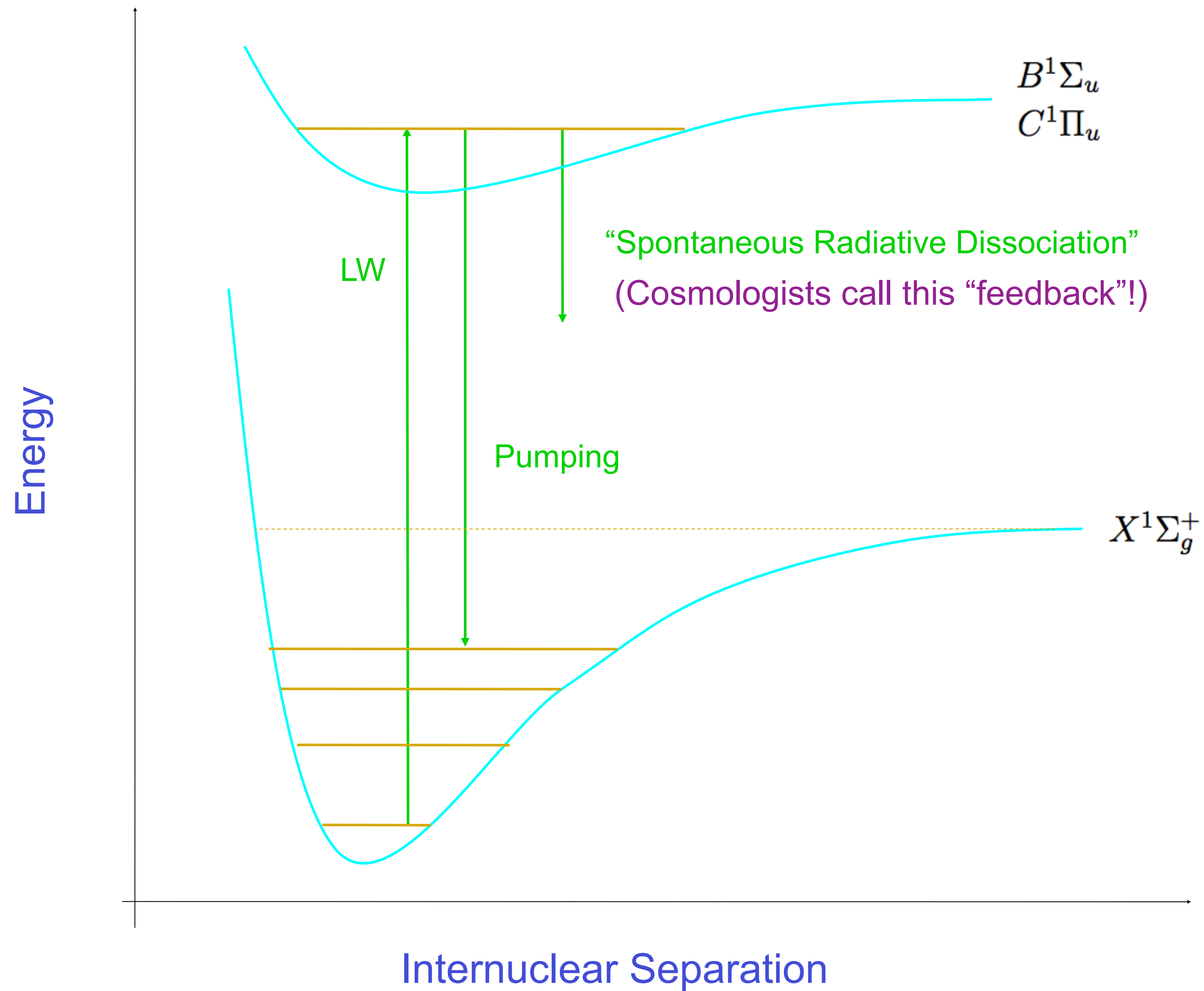
H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



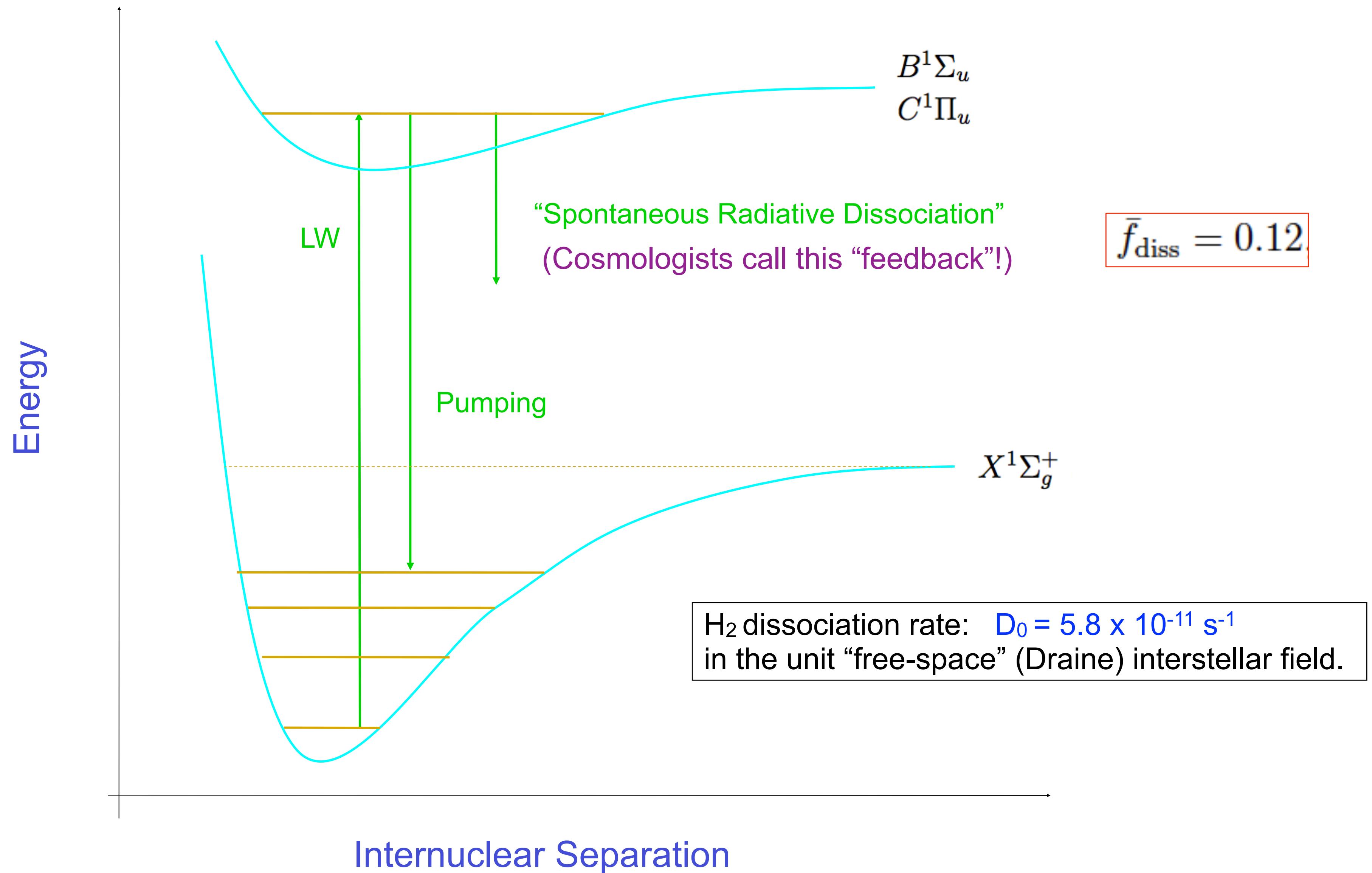
H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



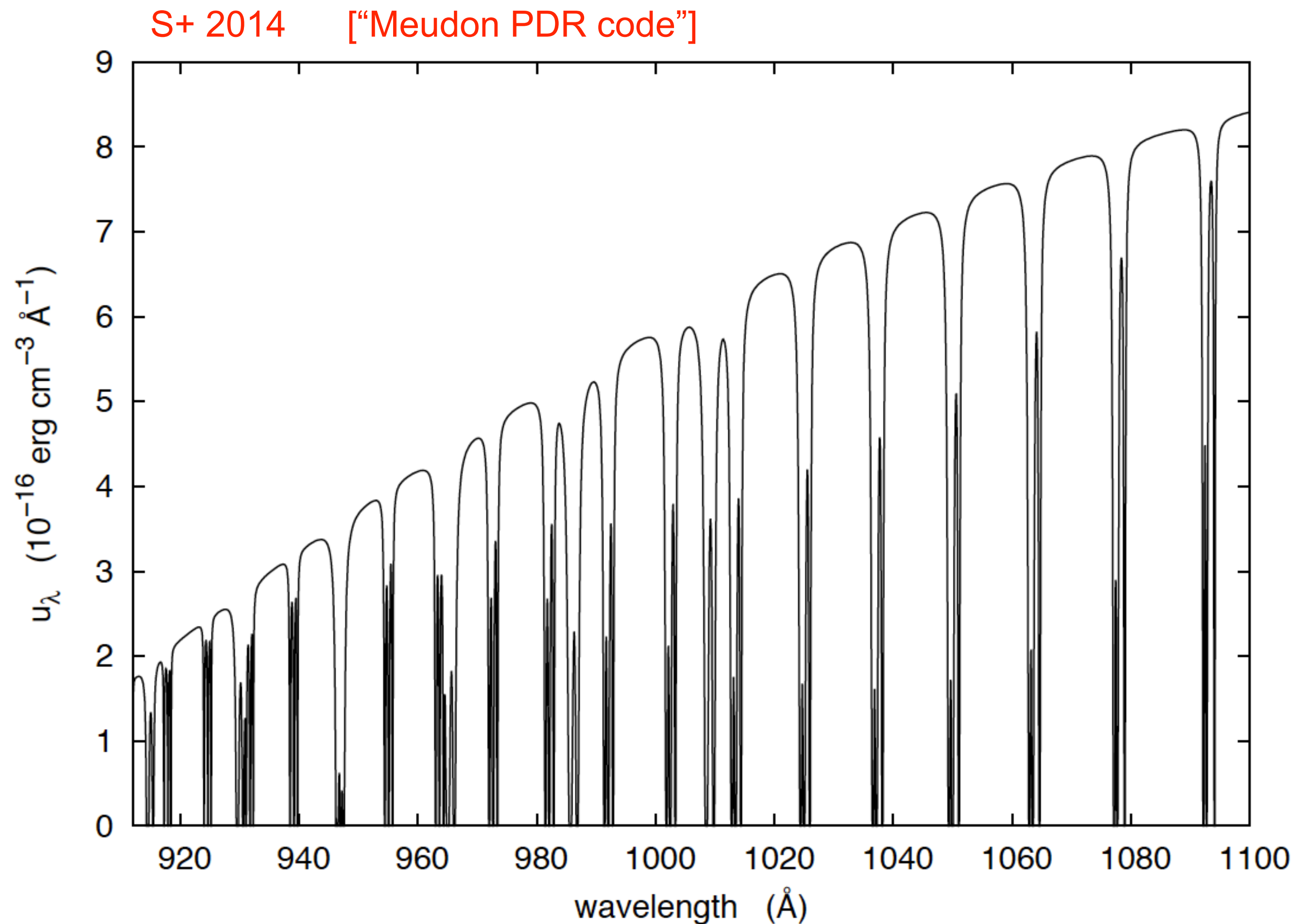
H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



Lyman-Werner Radiative Transfer:



Characteristic multi-line H₂ absorption spectrum, and “self-shielding”.

Dust absorption cross-section per hydrogen nucleus:

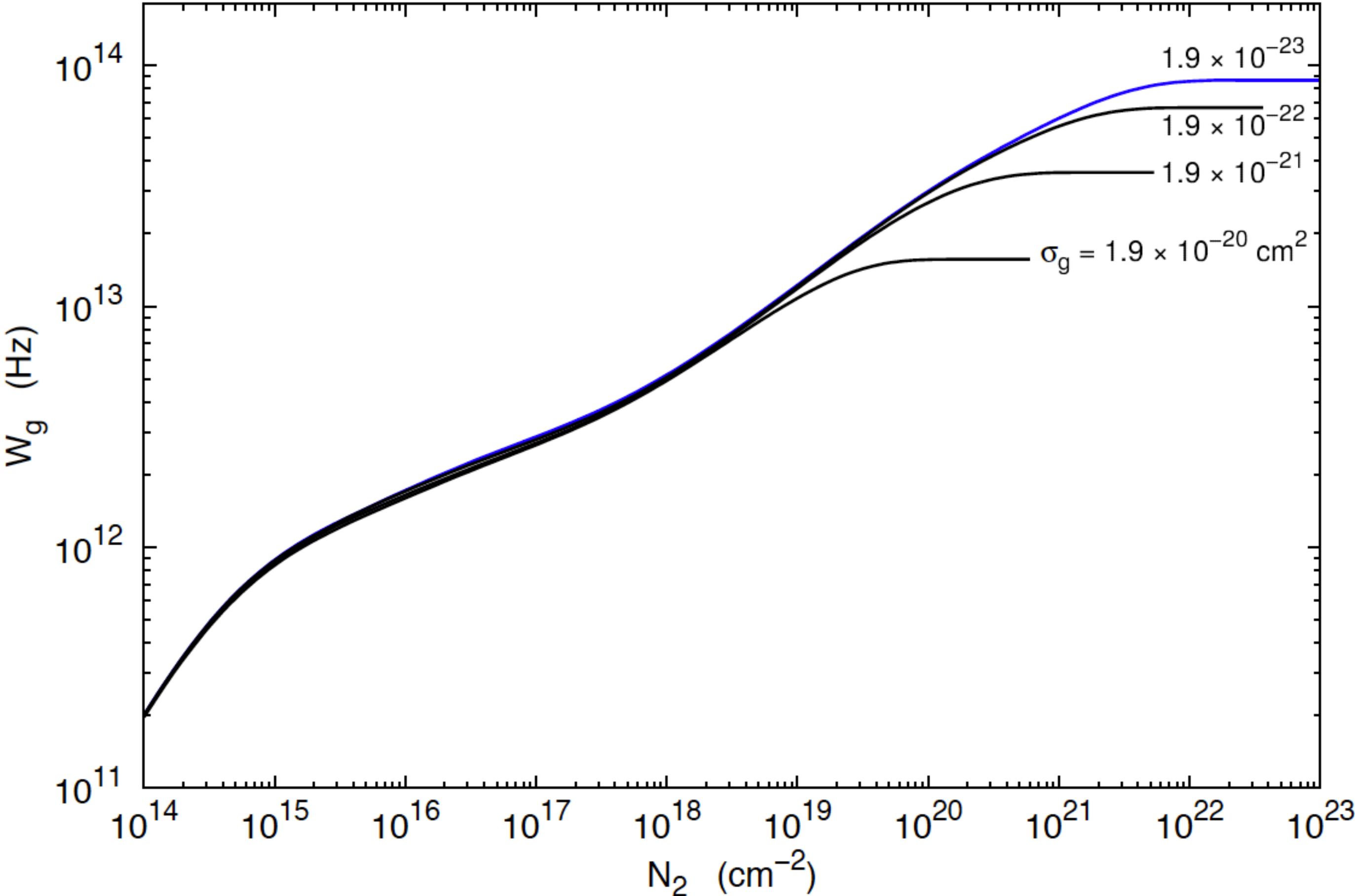
$$\sigma_g = 1.9 \times 10^{-21} \phi_g Z' \text{ cm}^2$$

Numerical radiative transfer on a fine frequency grid with a spectral resolution $\sim 10^5$.

Curve-of-Growth for the “H₂ Dust-Limited Dissociation Bandwidth”:

[integrated over all LW lines]

Sternberg+ 2014 [“Meudon PDR code”]



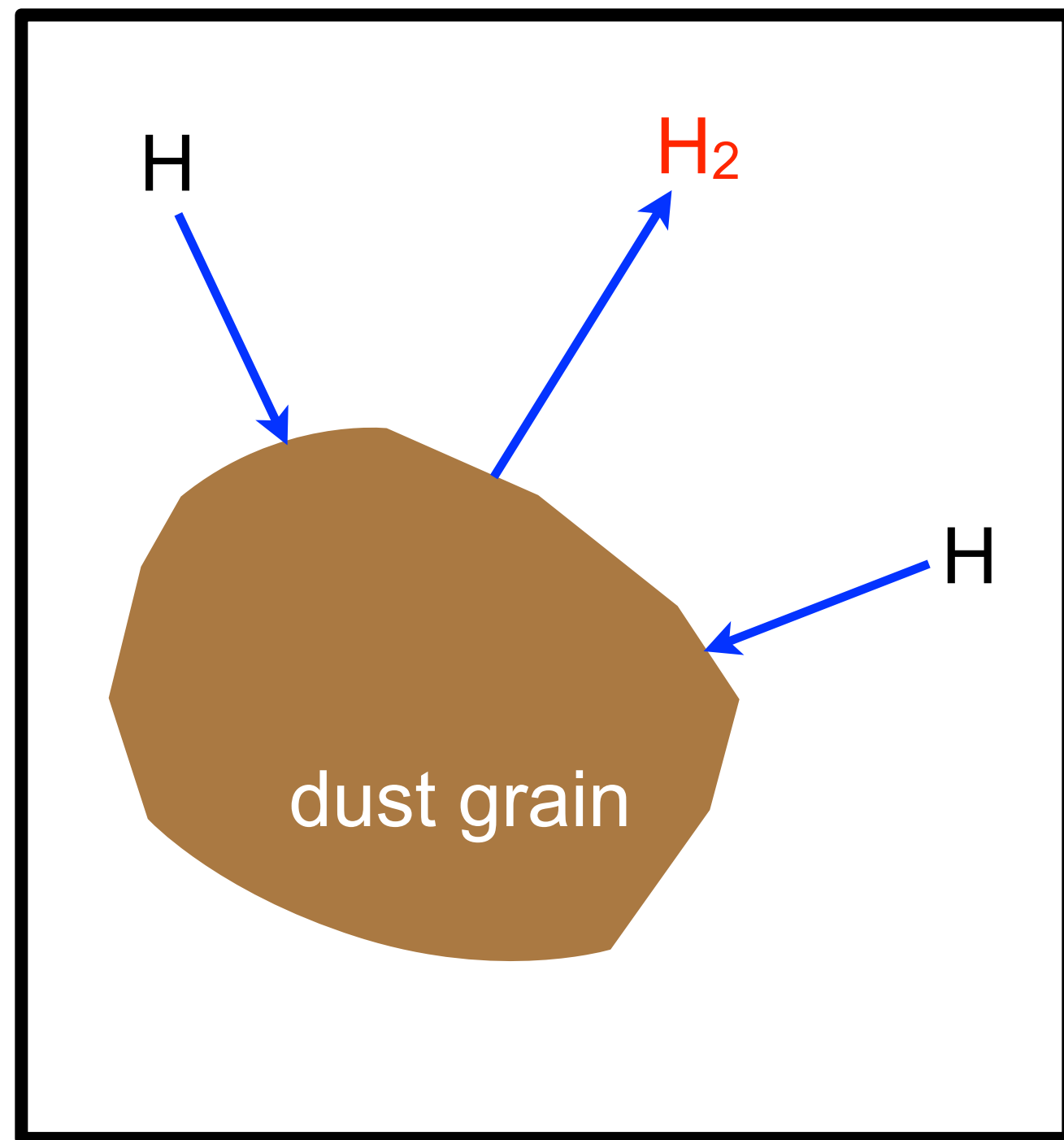
low metallicity
↑
 Z' “little w ”
↓
high metallicity

The bandwidth (Hz) of radiation absorbed in H₂ line dissociations in a dusty and fully molecular cloud.

“H₂ dust” versus “H₂ lines”

Universal: independent of radiation field intensity, or cloud gas density, etc.

H₂ Formation:

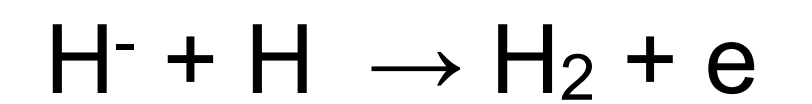
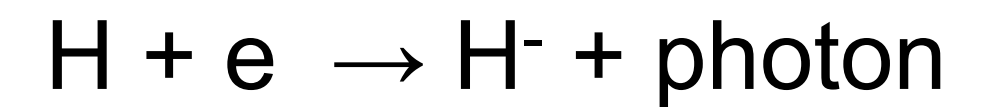


$$R = 3 \times 10^{-17} \left(\frac{T}{100 \text{ K}} \right)^{1/2} Z' \text{ cm}^3 \text{ s}^{-1}$$

$$t_{\text{eq}} = \frac{1}{Rn} = \frac{10^9}{Z'n} \text{ yr}$$

time scale for equilibrium

In the absence of dust:



Basic Theory Question:

What is the total HI column density (cm^{-2})
or HI mass surface density ($M_{\odot} \text{ pc}^{-2}$)
in far-UV irradiated systems?

Dimensionless Parameter:

Sternberg 1988; McKee & Krumholz 2010; Sternberg+ 2014

$$\alpha G \equiv \bar{f}_{\text{diss}} \frac{\sigma_g w F_0}{Rn}$$

Physical Meaning:

self-shielded H₂ dissociation rate

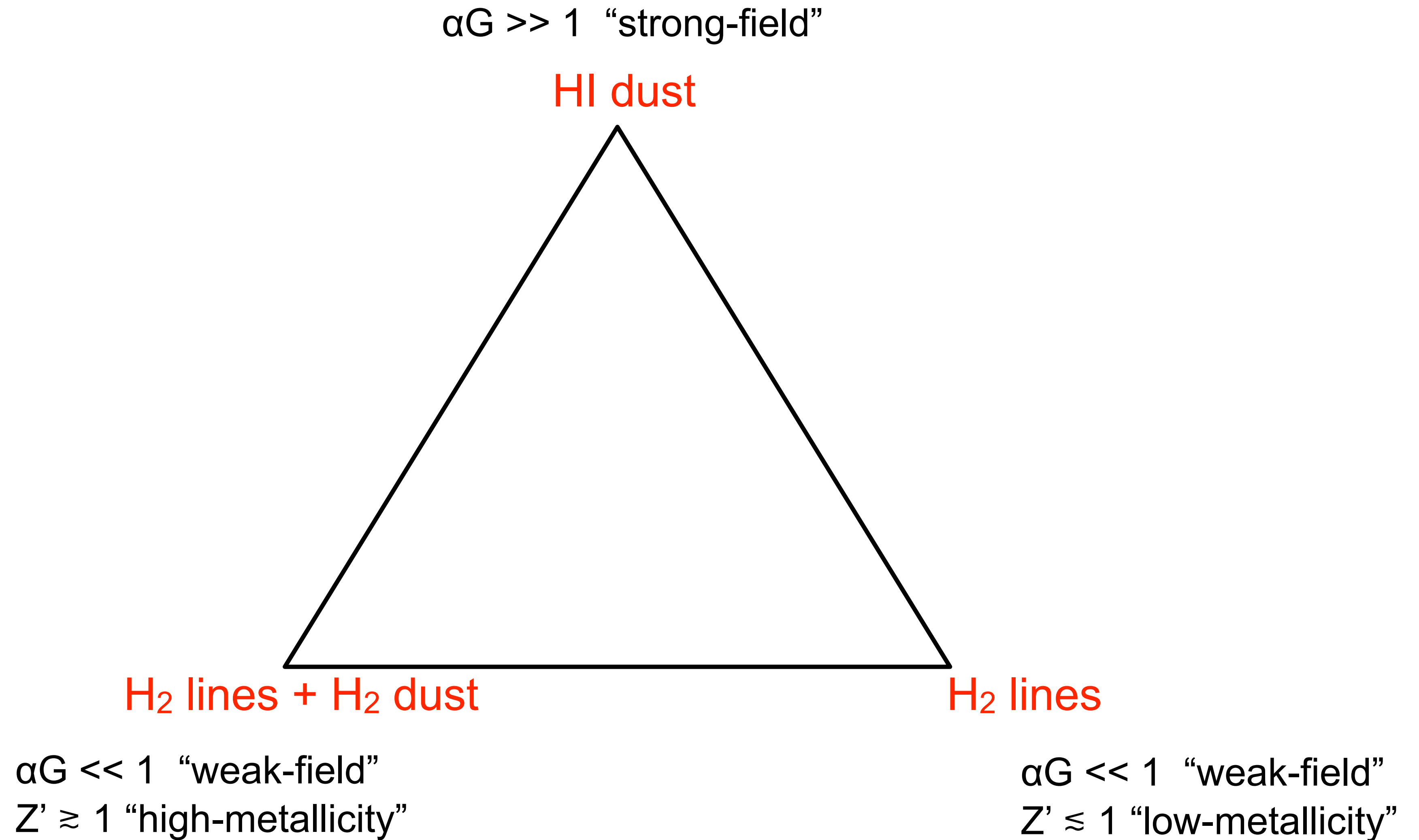
H₂ rate formation rate

or:

HI-dust absorption rate of the effective dissociation flux

free space H₂ photodissociation rate

Three-Way Competition for the FUV Absorption:



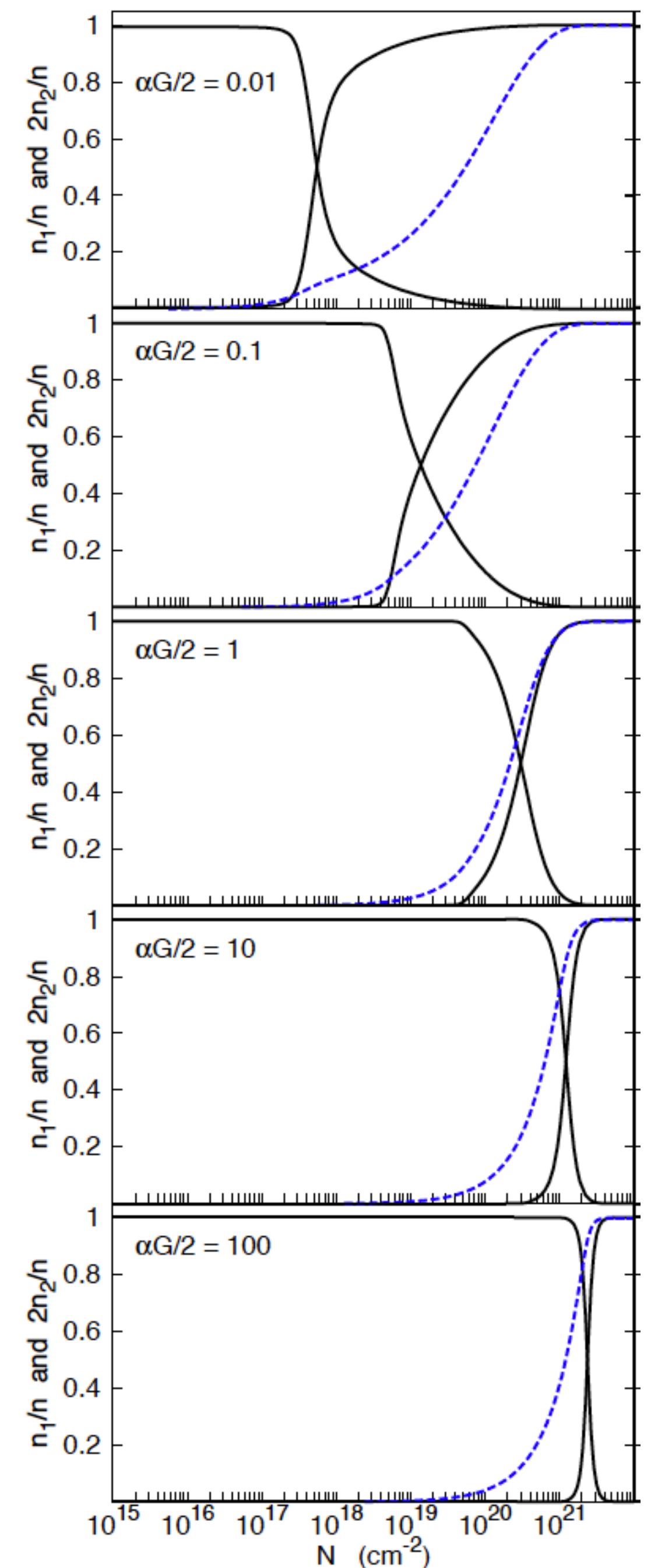
HI-to-H₂ Transition Profiles: Z'=1 (solar metallicity)

weak-field: most of the HI built up inside the H₂ zone,
“gradual profiles”

FUV attenuation dominated by
H₂ lines plus “H₂ dust”

strong-field: most of the HI built up in an outer layer,
“sharp profiles”

FUV attenuation dominated by “HI-dust”



HI-to-H₂ Transition Profiles: $Z'=1$ (solar metallicity)

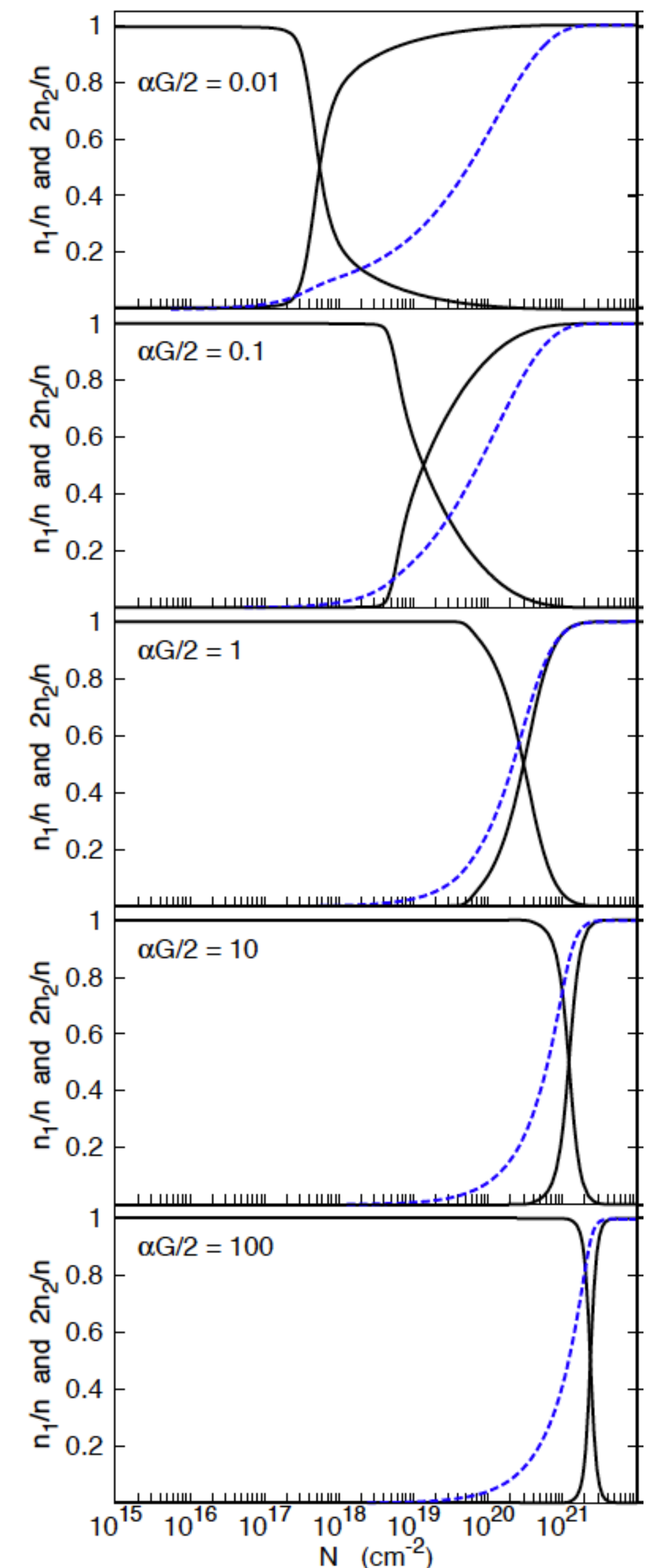
weak-field: most of the HI built up inside the H₂ zone,
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FUV attenuation dominated by
H₂ lines plus “H₂ dust”

**For a given Z' , the profile shapes depend
on the dimensionless parameter αG .**

strong-field: most of the HI built up in an outer layer,
“sharp profiles”

FUV attenuation dominated by “HI-dust”

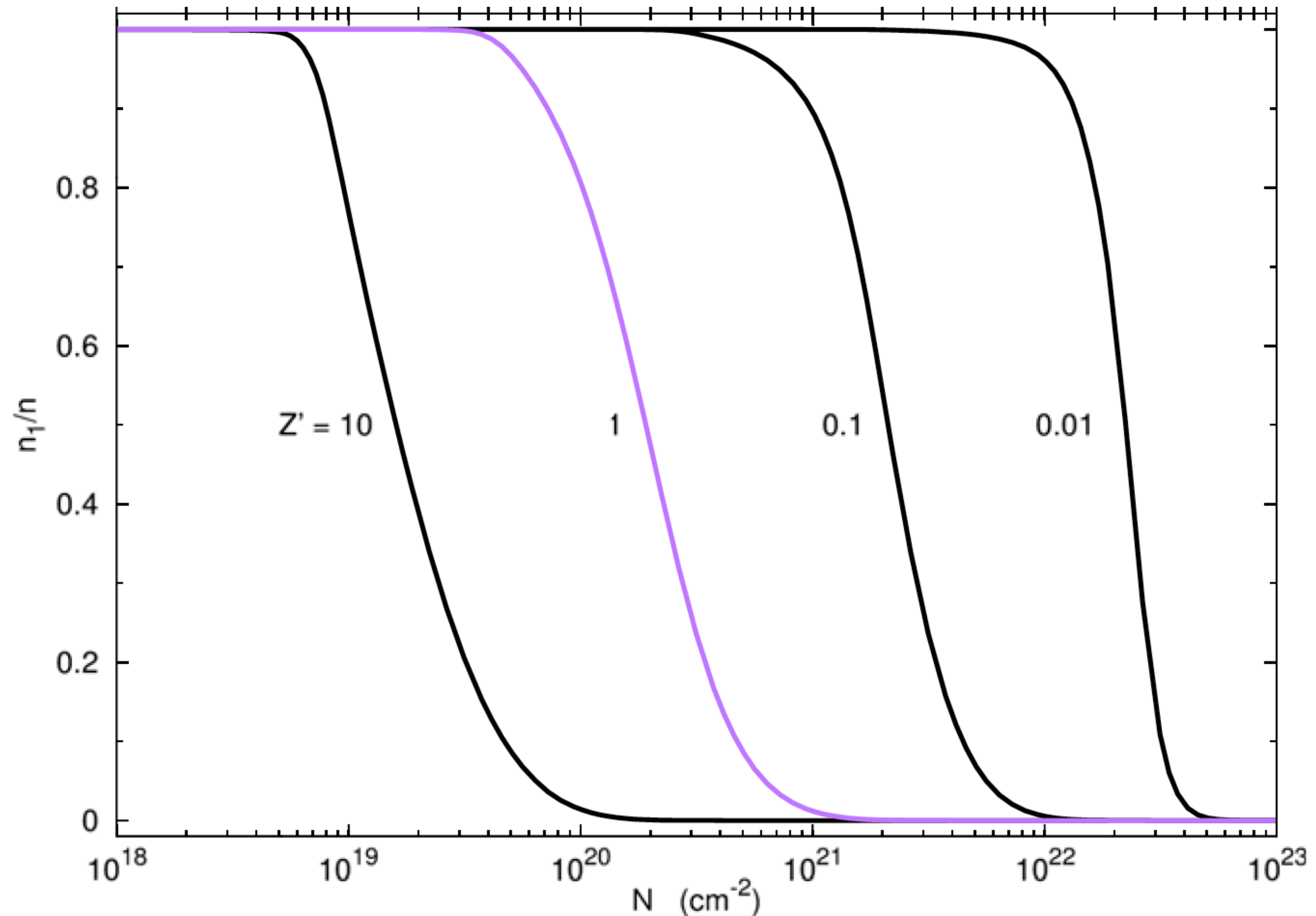


For a given αG the profile “scale lengths” are determined by Z' .

$$\sigma_g = 1.9 \times 10^{-21} \phi_g Z' \text{ cm}^2$$

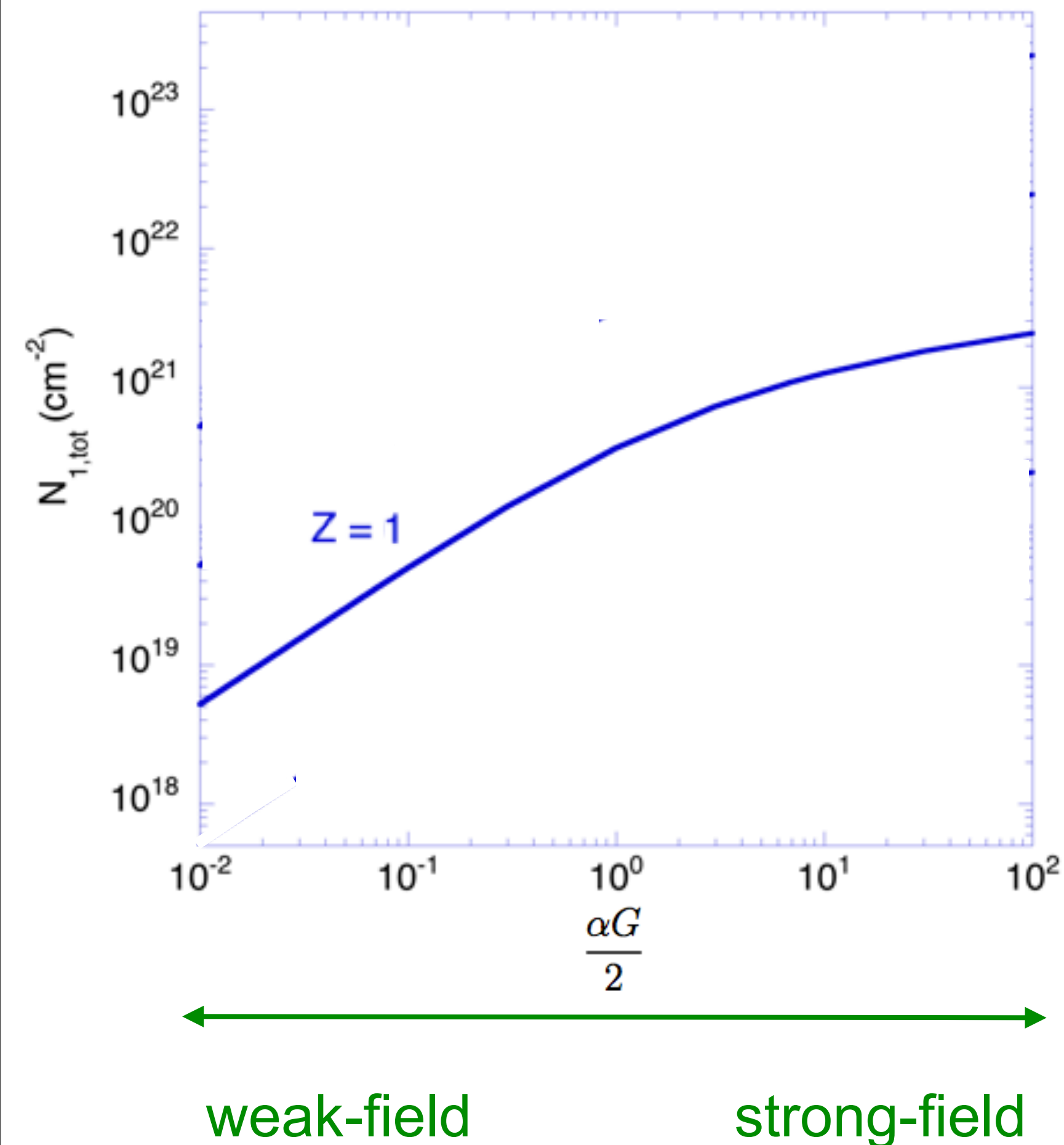
$$R = 3 \times 10^{-17} \left(\frac{T}{100 \text{ K}} \right)^{1/2} Z' \text{ cm}^3 \text{ s}^{-1}$$

E.g., HI profiles for $\alpha G/2 \approx 1$



General Purpose Analytic Formula for the Total HI Column Density:

$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln\left[\frac{\alpha G}{4} + 1\right] = \frac{1}{\sigma_g} \ln\left[\frac{1}{4} \frac{\bar{f}_{\text{diss}} \sigma_g w F_0}{Rn} + 1\right]$$

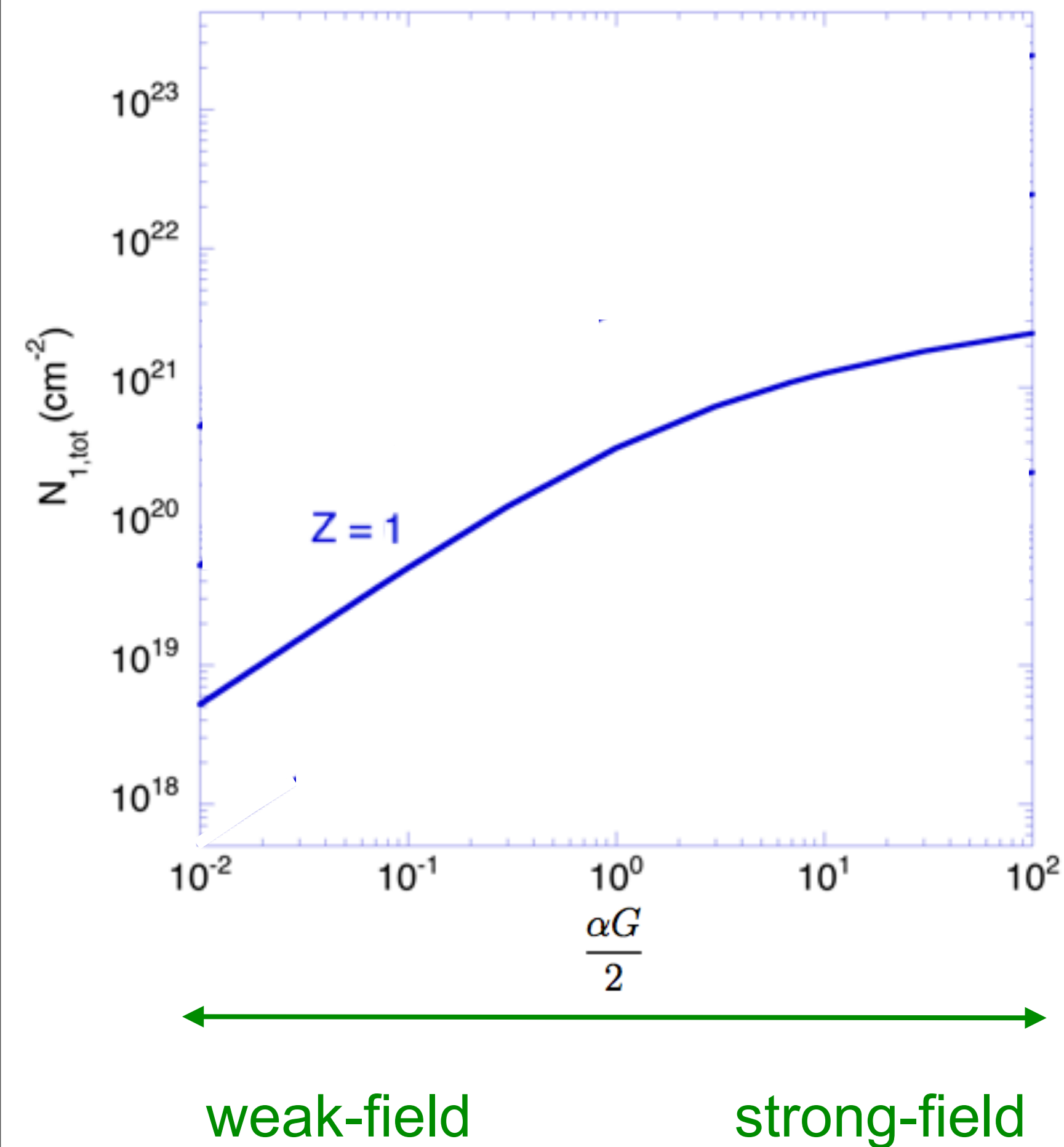


Valid for all regimes:

- weak and strong fields
- gradual to sharp transitions
- arbitrary metallicity

[note: no reference to the H₂ line photodissociation cross sections!]

Weak-Field Limit:

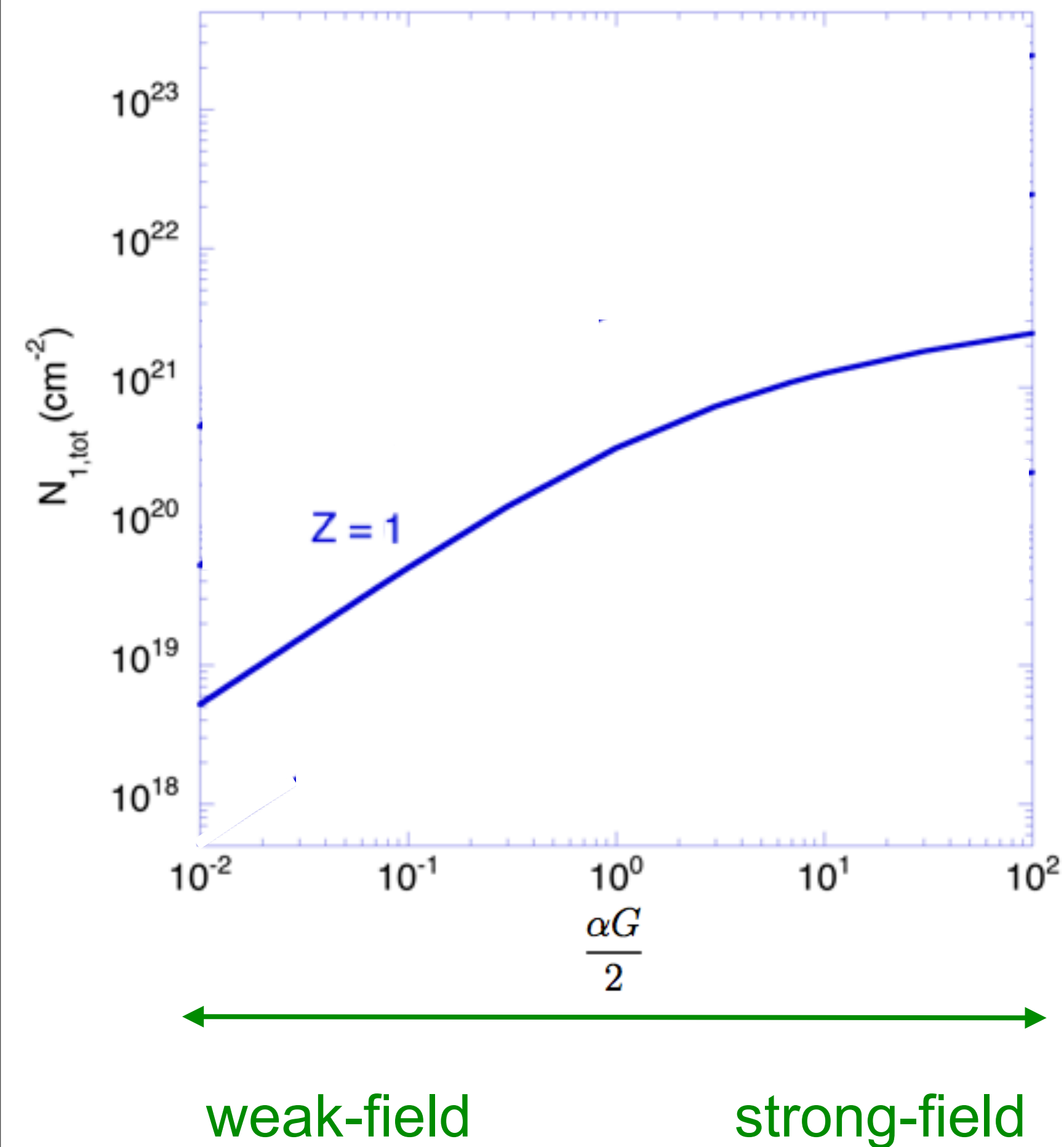


$$N_{1,\text{tot}} = \frac{1}{4} \frac{\bar{f}_{\text{diss}} w F_0}{Rn}$$

$$Rn N_{1,\text{tot}} = \frac{1}{4} \bar{f}_{\text{diss}} w F_0$$

formation rate per unit area = effective dissociation flux
(a “Strömgren Relation”)

Strong-Field Limit:



$$N_{1,\text{tot}} \approx \frac{1}{\sigma_g}$$

(neglecting the logarithmic term)

makes sense: When HI-dust dominates the attenuation of the far-UV field, the HI-column is “self-limited” and

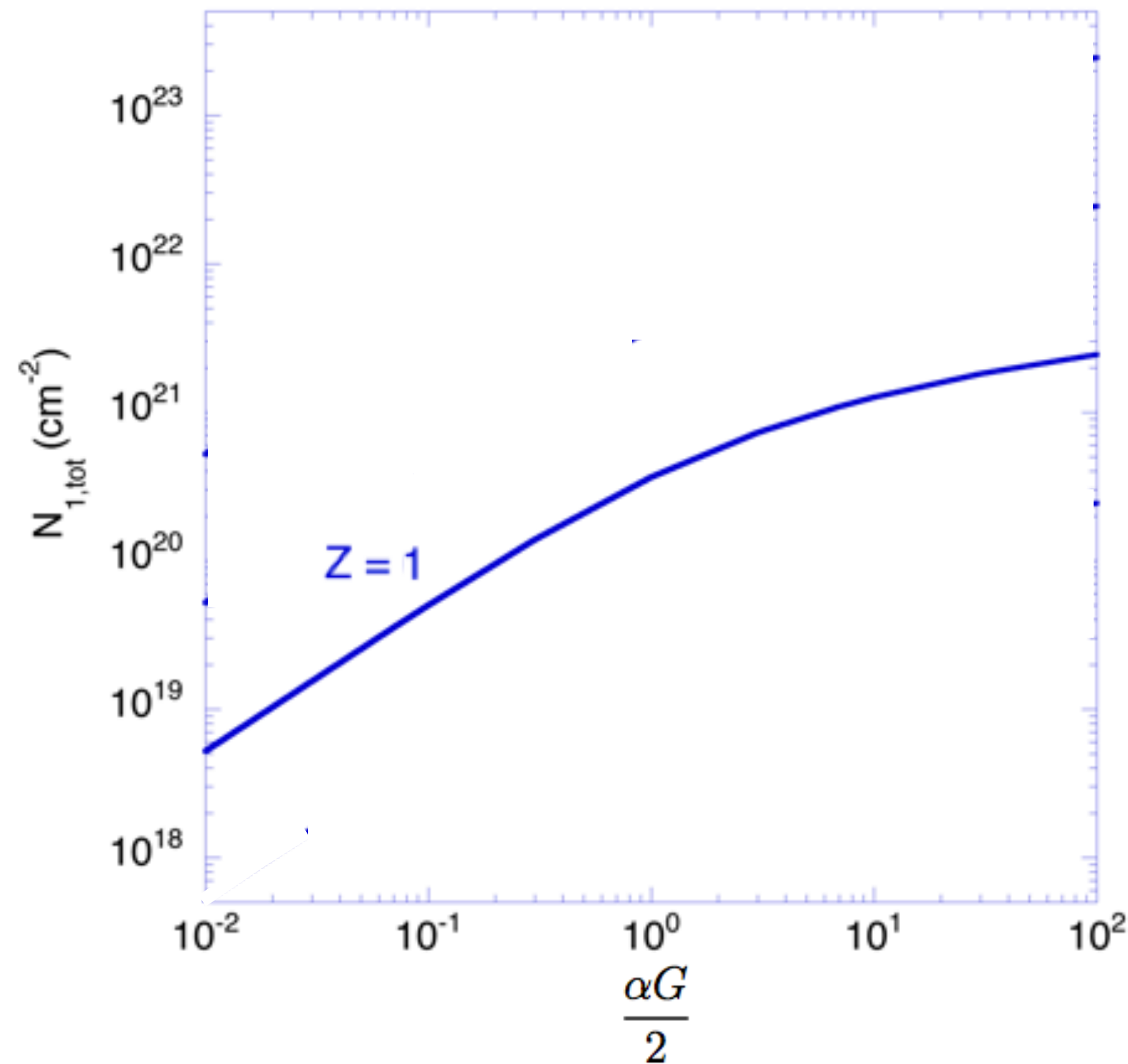
$$\tau_{\text{HI dust}} = \sigma_g N_{1,\text{tot}} \approx 1$$

Heavy-Element Abundances “Metallicity”:

Z'

$$R \propto Z' \quad \sigma_g \propto Z'$$

H_2 formation rate coefficient
and dust absorption cross-section
both proportional to metallicity.



$$N_{1,\text{tot}} = \frac{1}{4} \frac{\bar{f}_{\text{diss}} w F_0}{R n} \propto \frac{1}{Z'}$$

weak-field

$$N_{1,\text{tot}} \approx \frac{1}{\sigma_g} \propto \frac{1}{Z'}$$

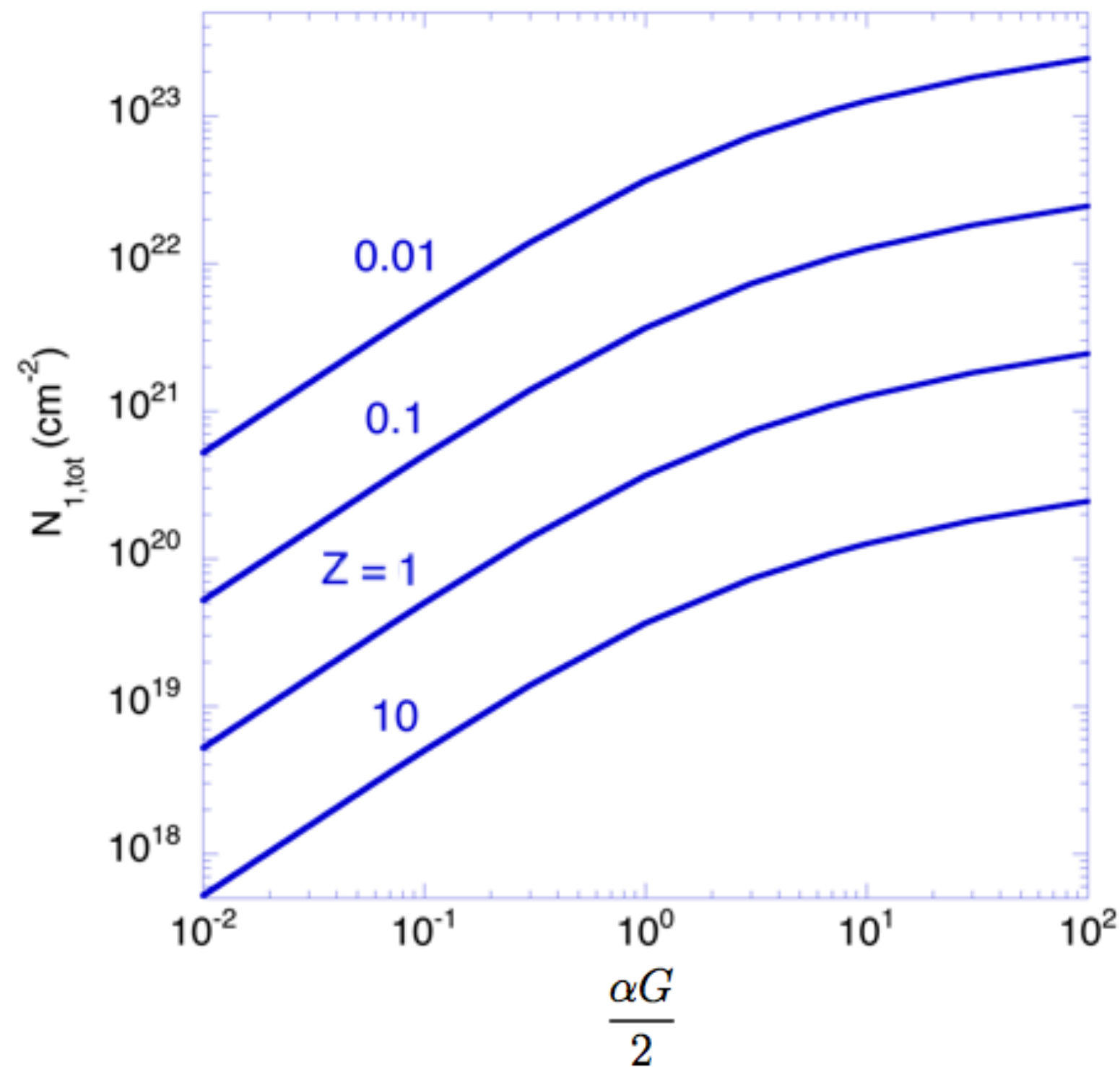
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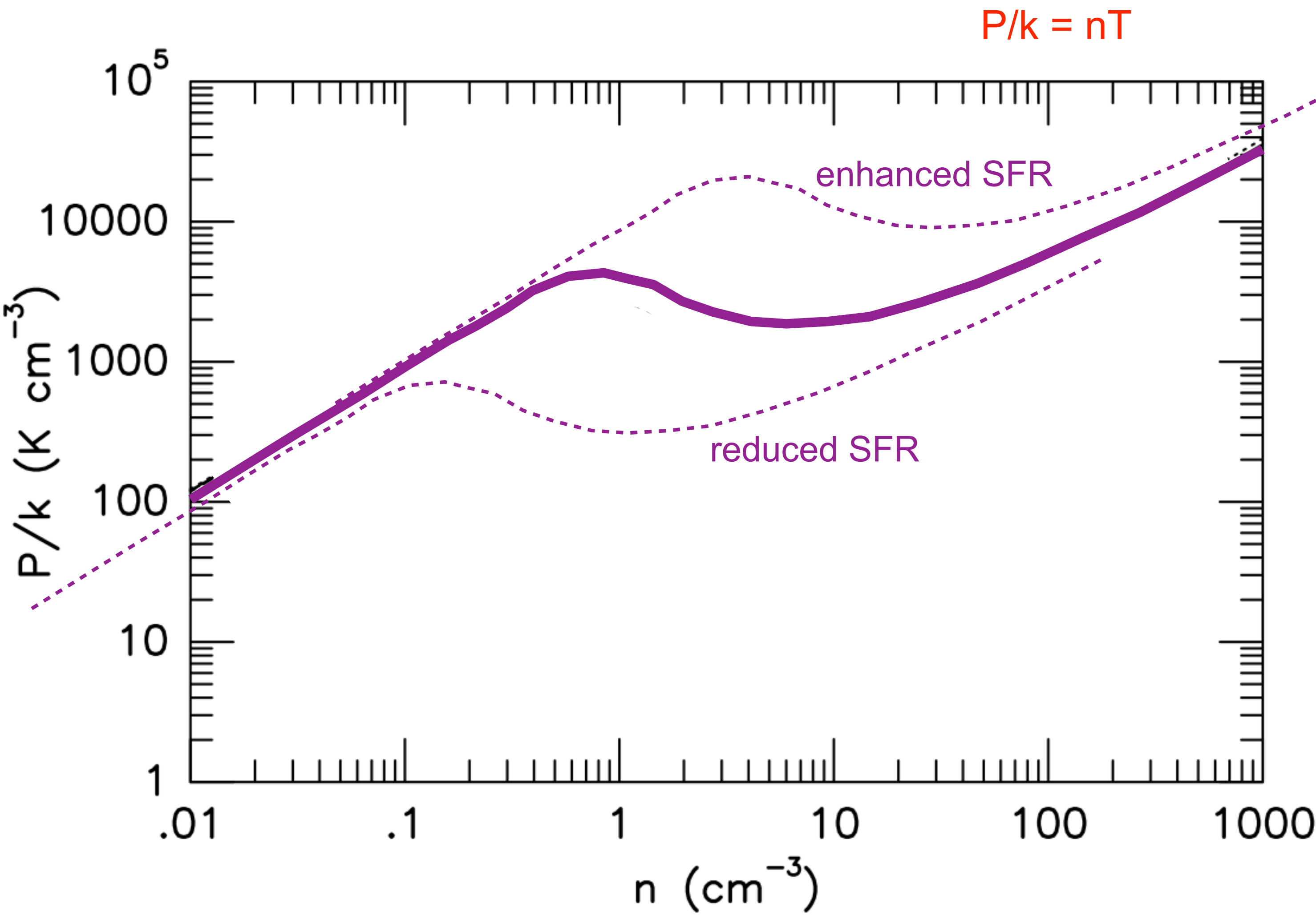
strong-field

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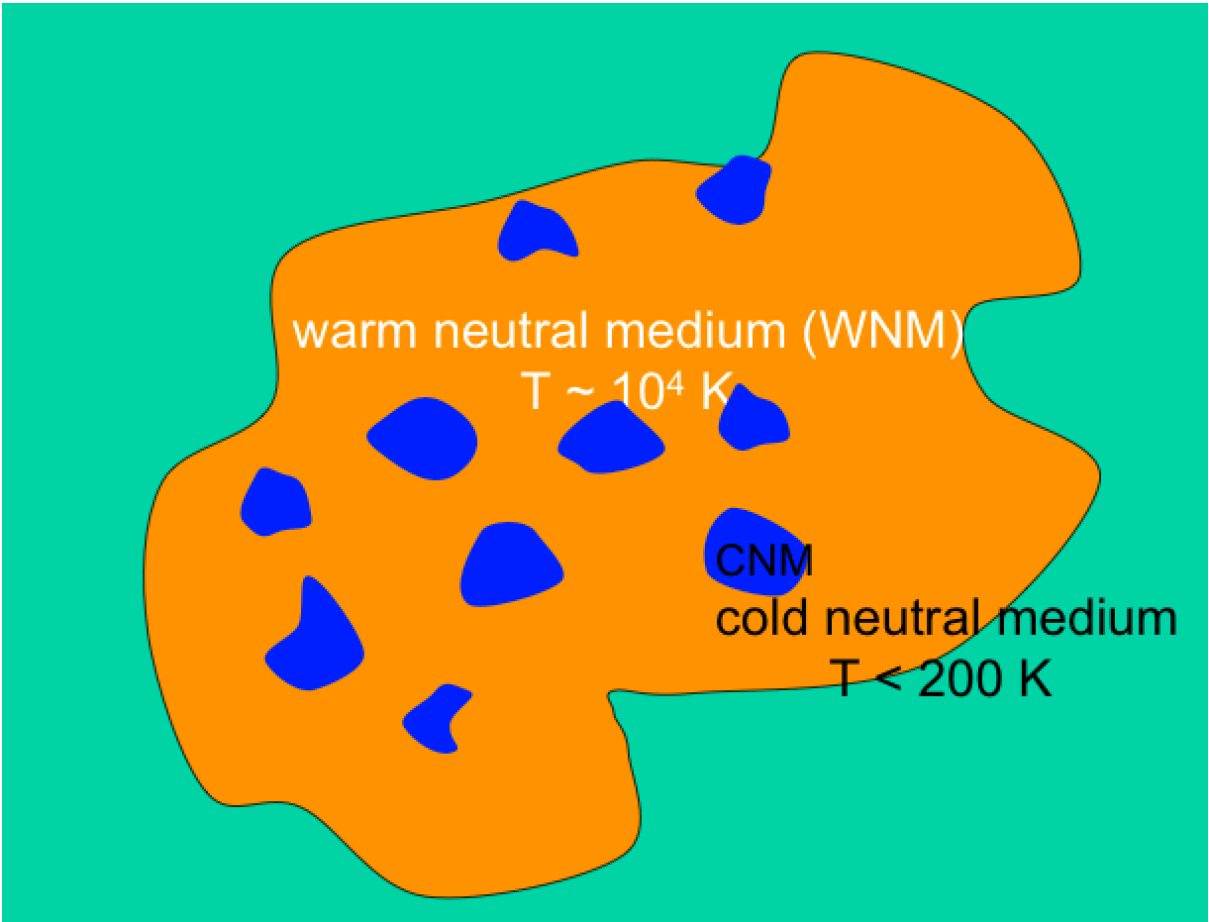
- useful for interpreting 21cm observations
- incorporation into hydrodynamics simulations
- application to “self-regulated” media

HI Thermal Phases in Self-Regulated Media:

Ansatz:
Krumholz, McKee & Tumlinson 2009



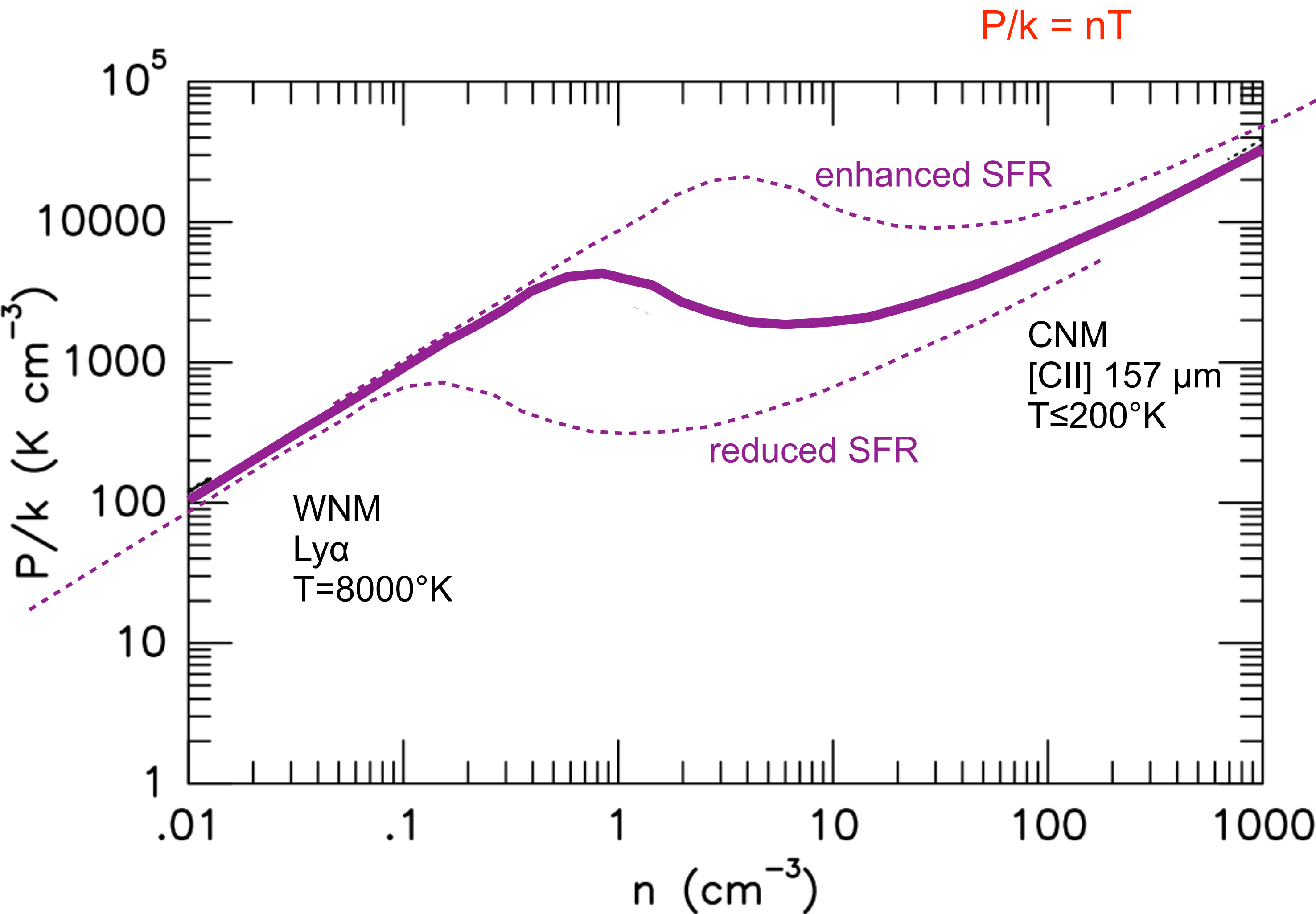
Wolfire, McKee & Hollenbach 2003
Sternberg, McKee & Wolfire 2002



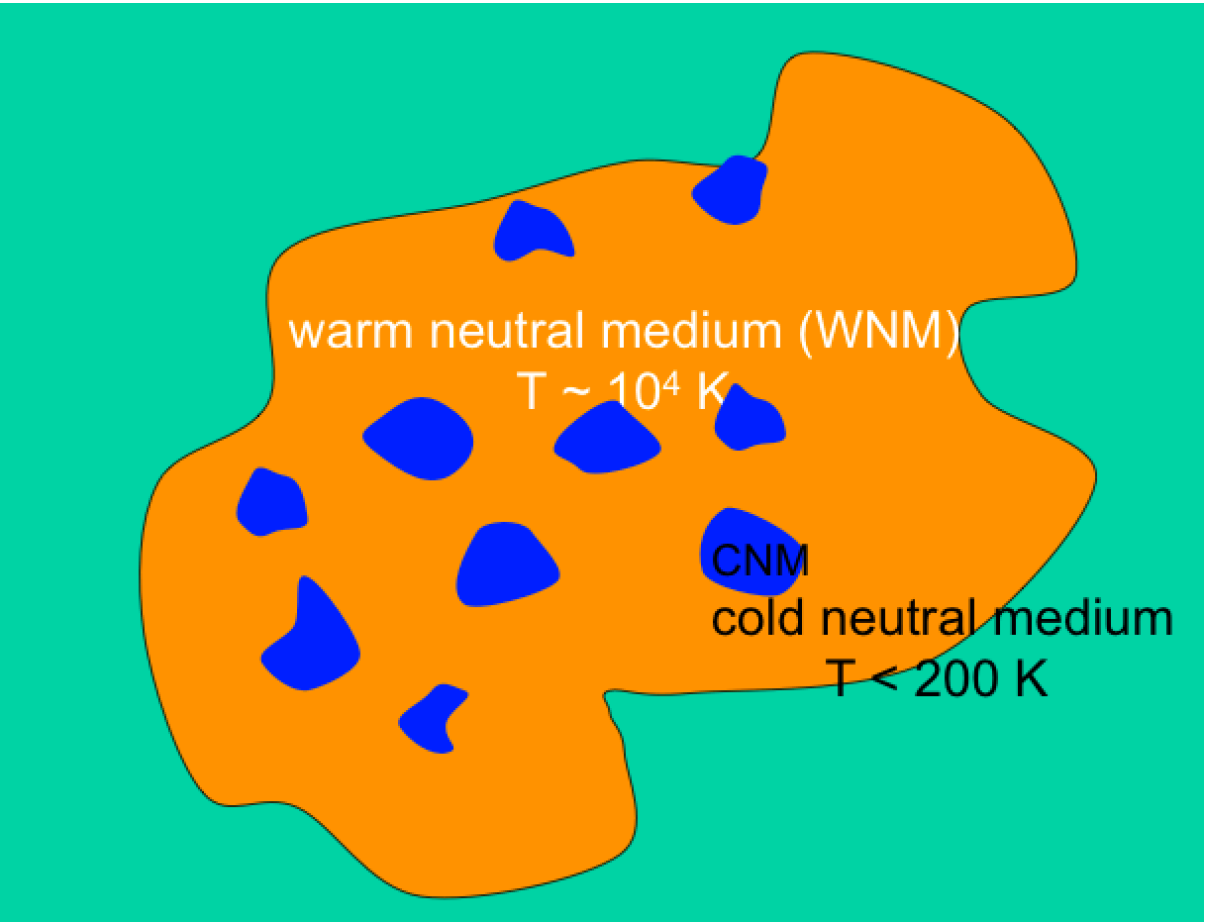
Field, Goldsmith & Habing 1969 ApJ 155 149

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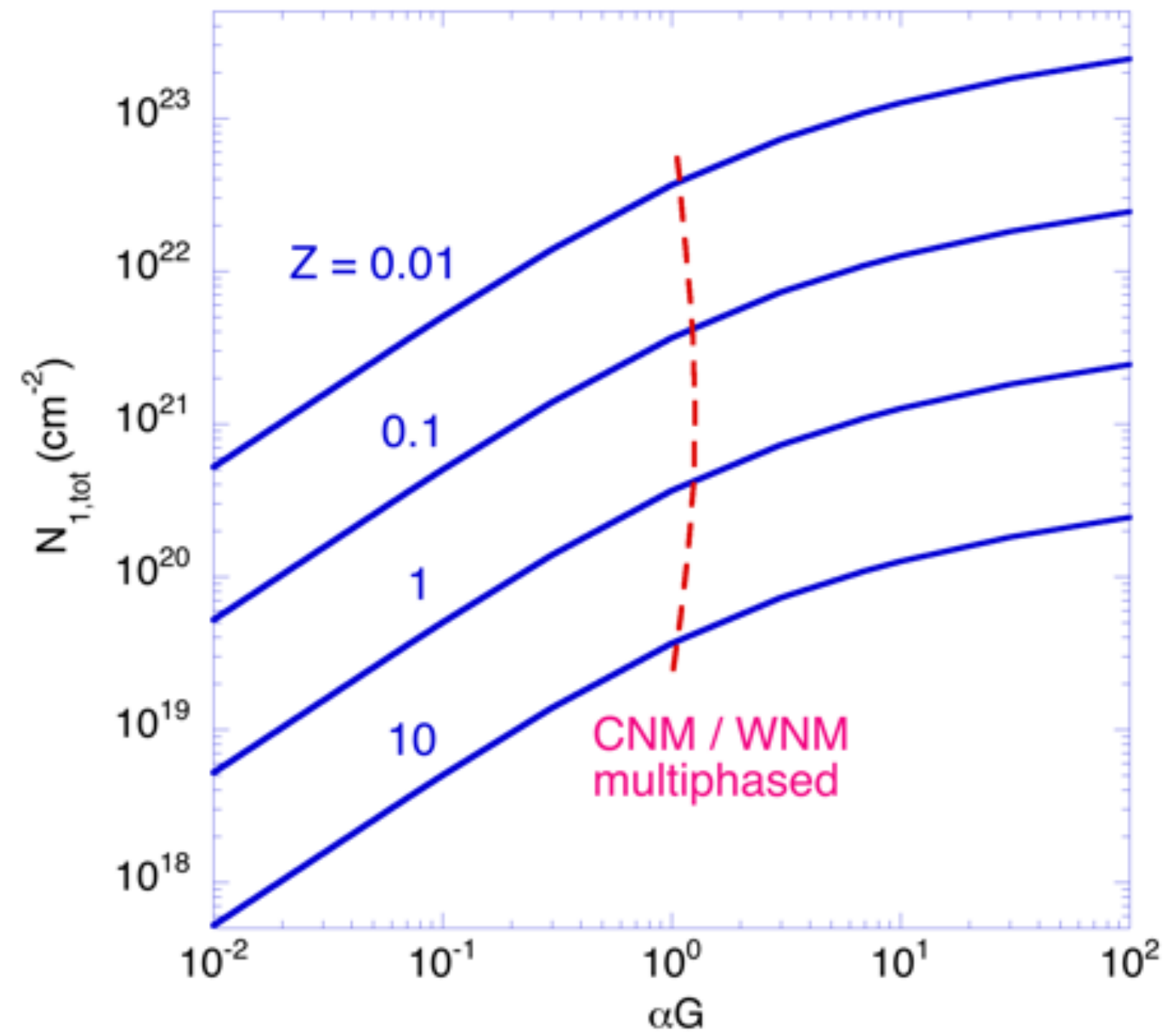


Field, Goldsmith & Habing 1969 ApJ 155 149

HI Column Density for Self-Regulated Media:

$$\frac{(\alpha G)_{\text{CNM}}}{2} \approx 1$$

remarkable!



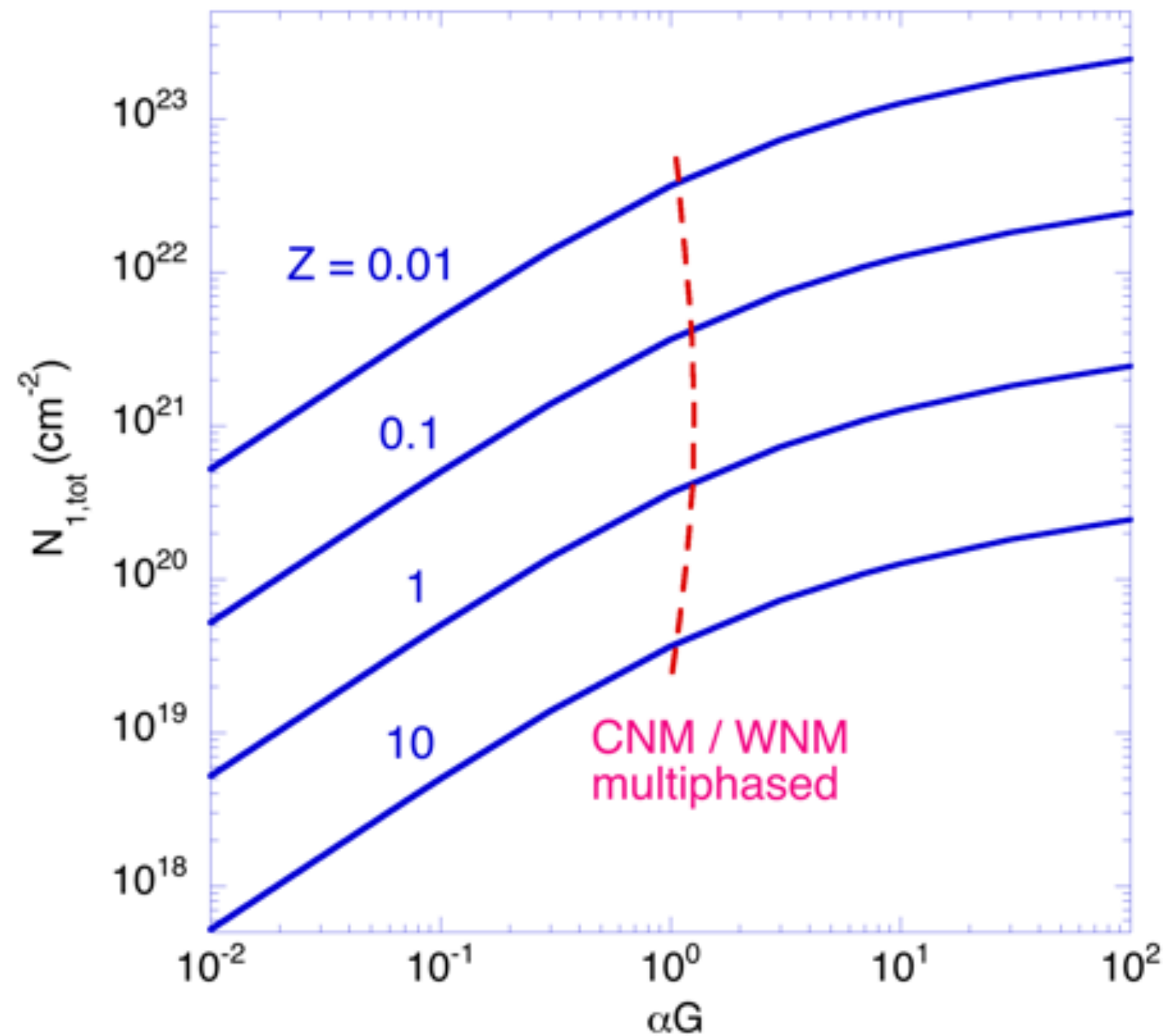
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remarkable!

$$\Sigma_{\text{HI}} \approx \frac{6}{\phi_g Z'} \text{ M}_{\odot} \text{ pc}^{-2}$$

characteristic HI photodissociation mass surface density in self-regulated systems

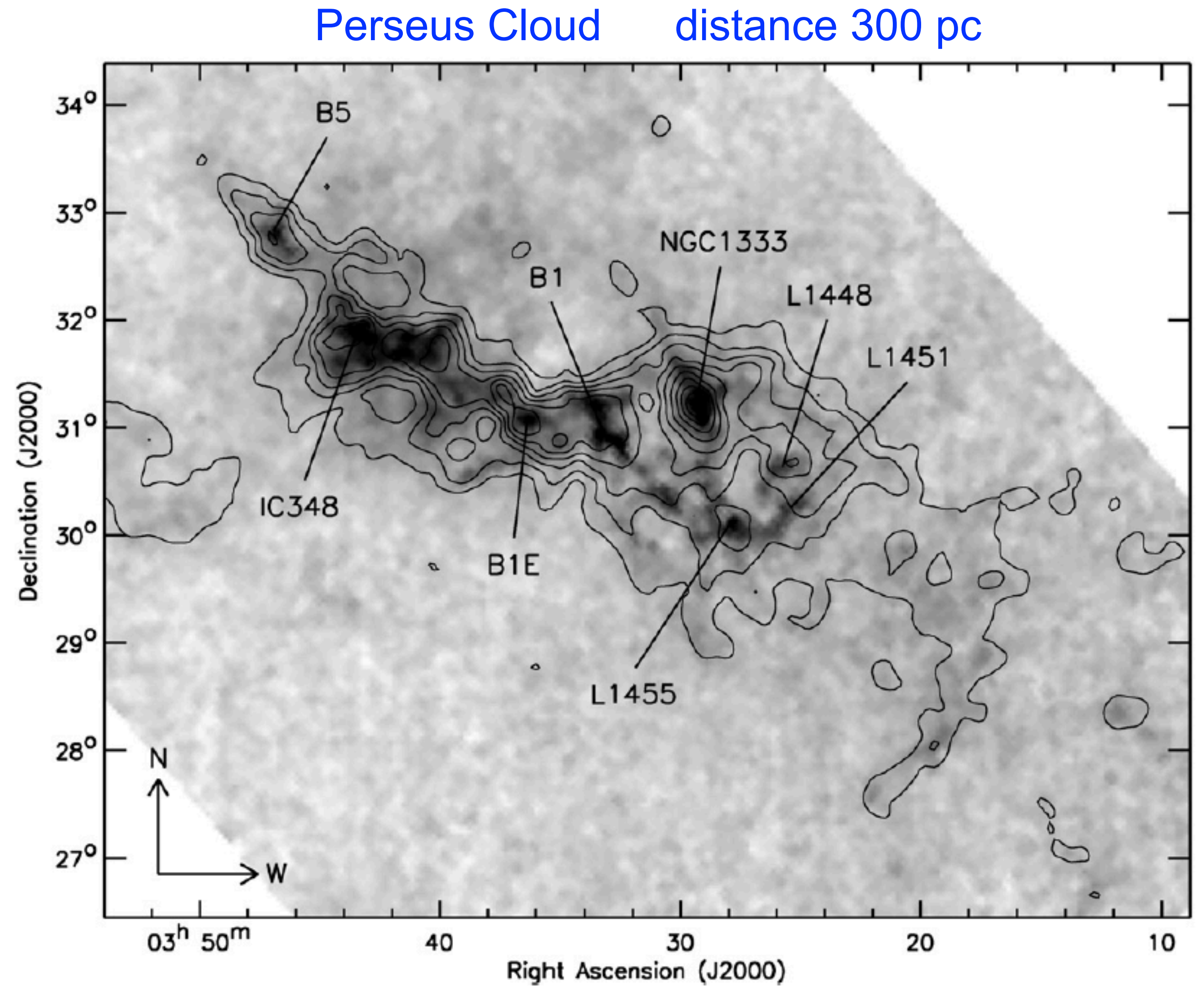


$$\Sigma_{\text{gas},*}(Z') \equiv 2 \times \Sigma_{\text{HI}} \approx \frac{12}{\phi_g Z'} \text{ M}_{\odot} \text{ pc}^{-2}$$

“transition” total gas mass surface density... star-formation threshold...galaxies.

independent of radiation field intensity and/or gas density.

HI-to-H₂ in Perseus:



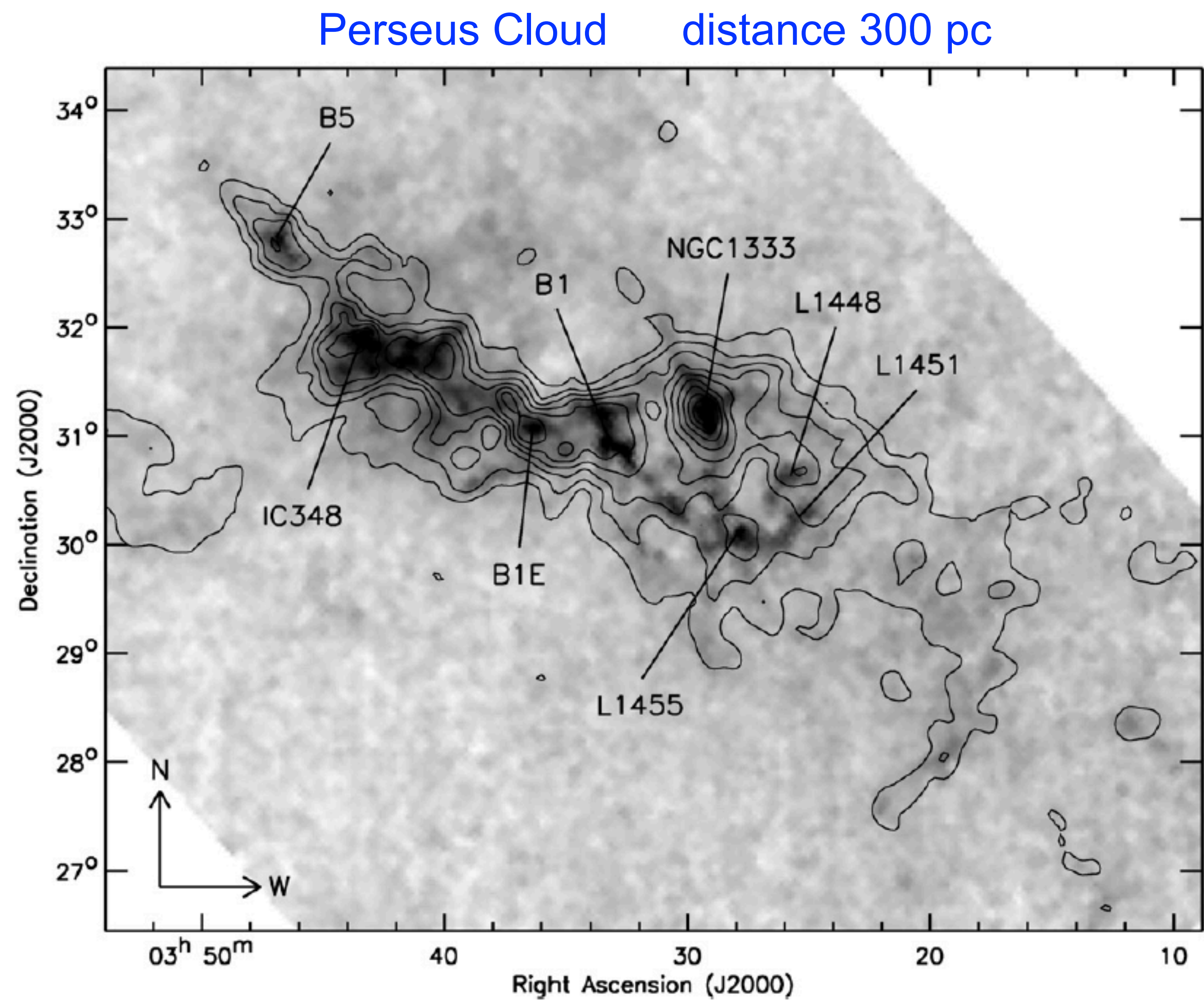
2MASS A_V and I_{CO} CfA & COMPLETE surveys

Dame+ 2001 Ridge+ 2006

HI-to-H₂ in Perseus:

dark clouds &
low-mass star-forming regions:

B1
B1E
B5
NGC1333
IC348



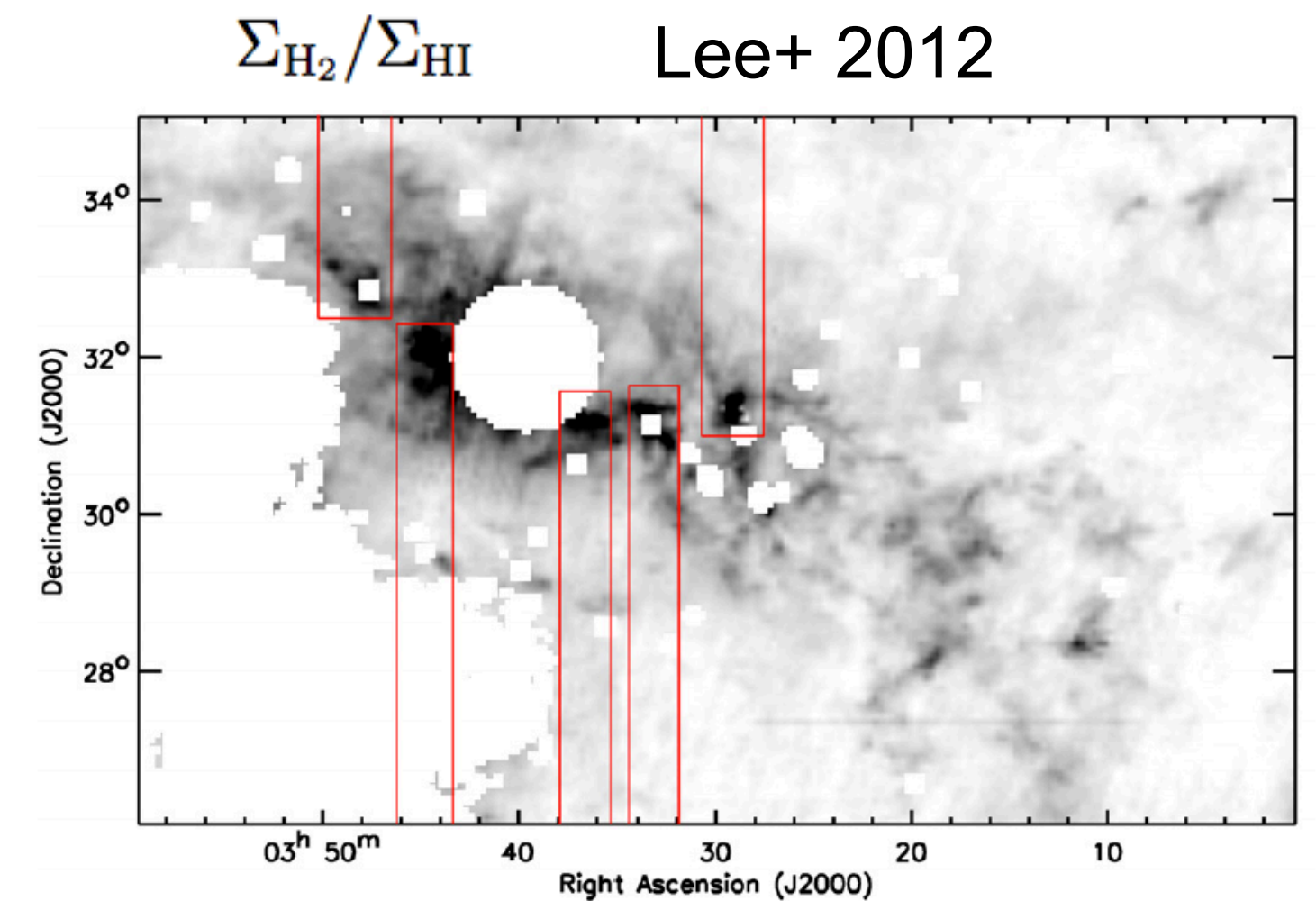
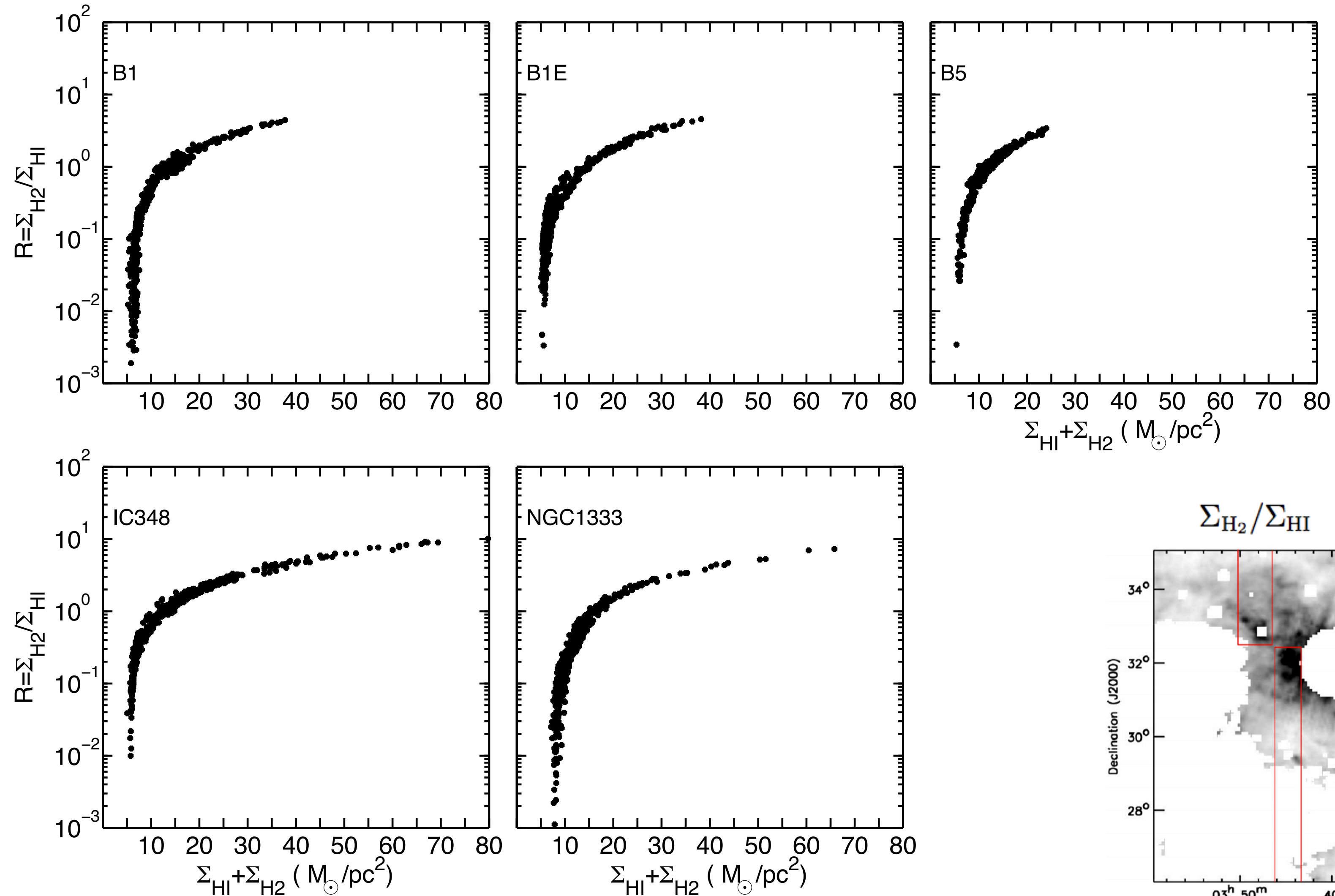
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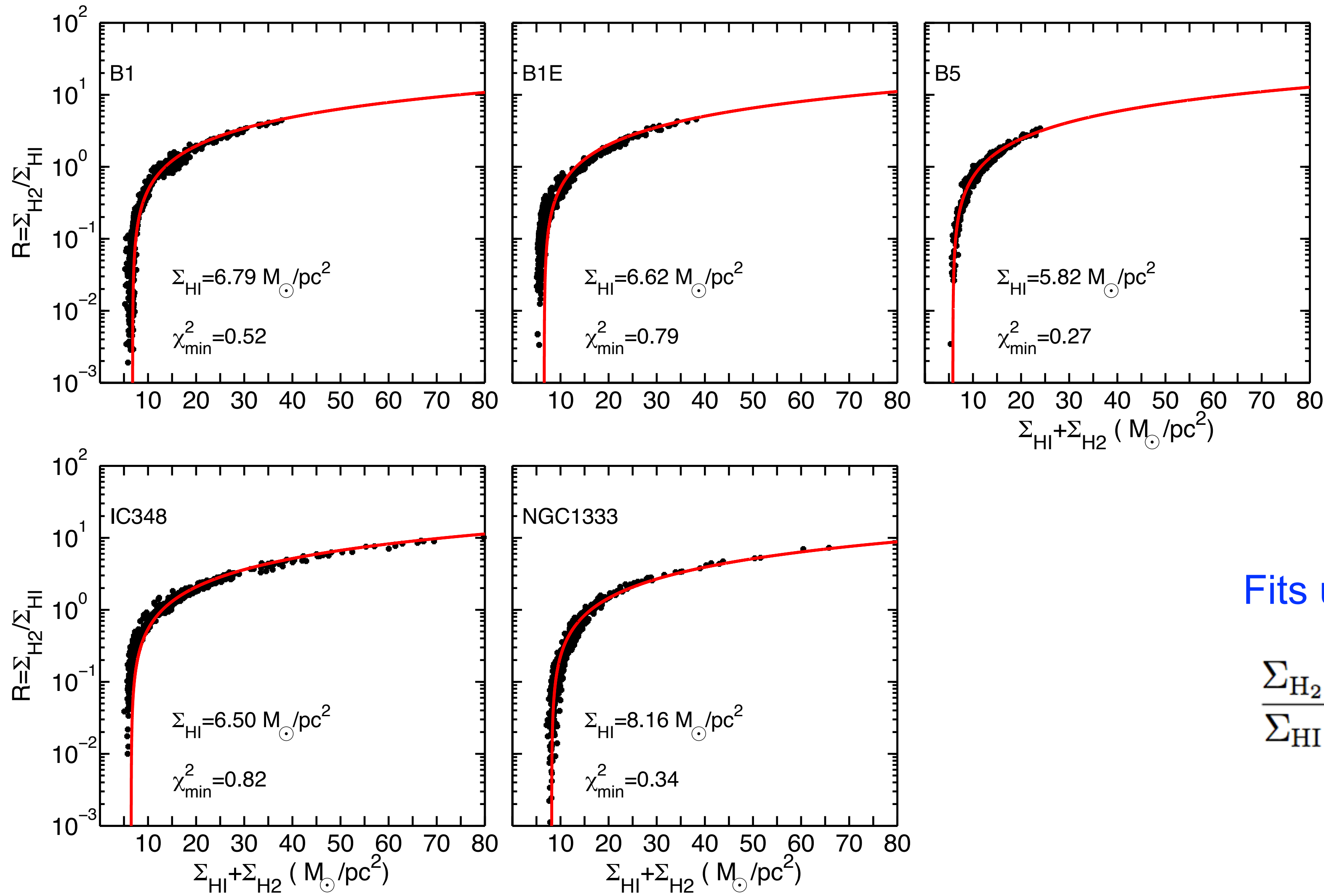
Lee+ 2012 Peek+ 2011 GALFA HI Survey (Arecibo 4arcmin)

$$\frac{\Sigma_{\text{H}_2}}{\Sigma_{\text{HI}}} \text{ versus } \Sigma_{\text{gas}} \equiv \Sigma_{\text{HI}} + \Sigma_{\text{H}_2}$$



HI-to-H₂ in Perseus:

$\frac{\Sigma_{\text{H}_2}}{\Sigma_{\text{HI}}}$ versus $\Sigma \equiv \Sigma_{\text{HI}} + \Sigma_{\text{H}_2}$

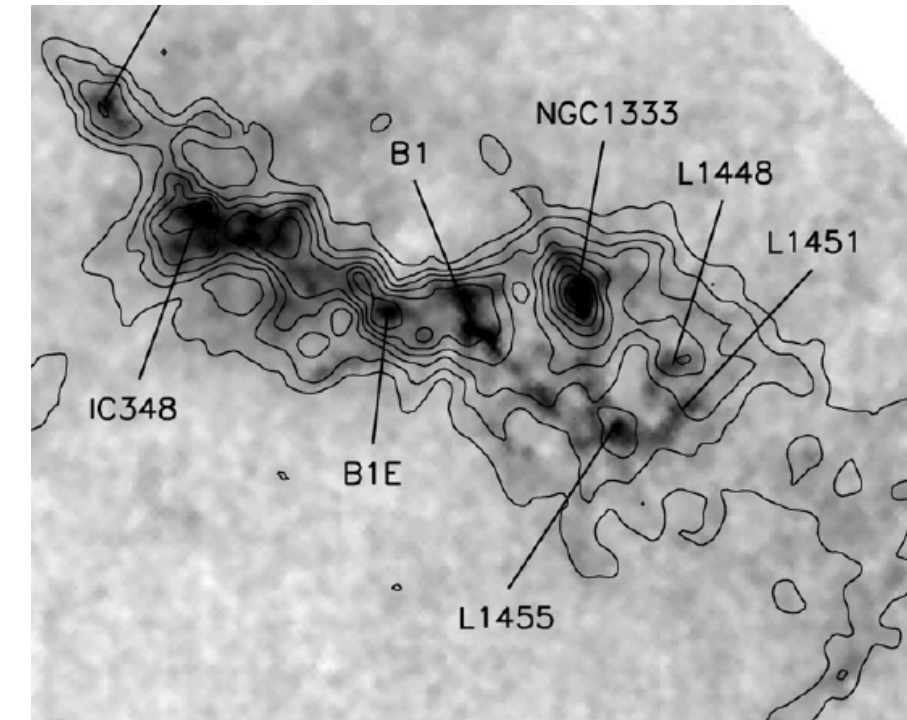
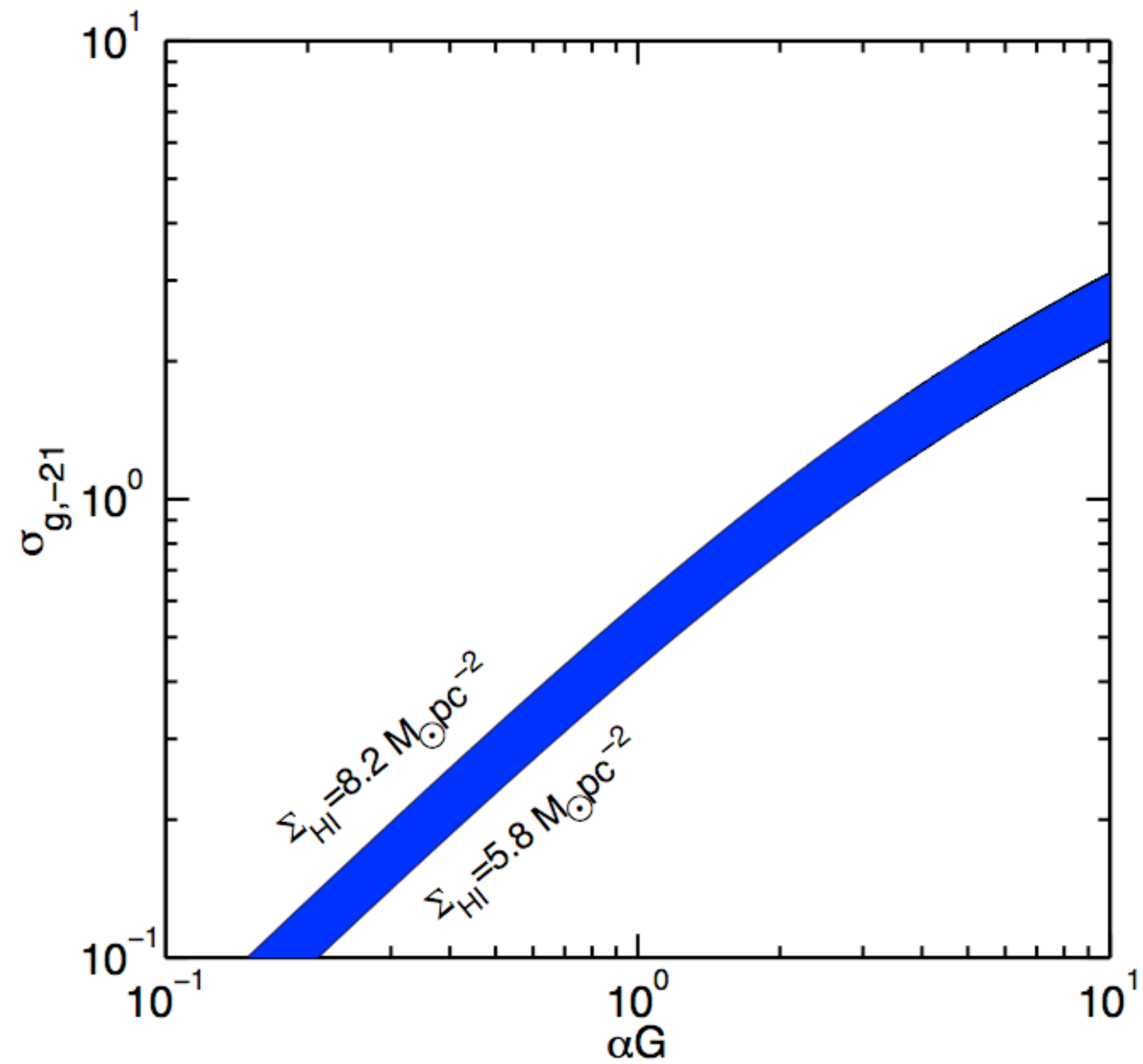


Fits using S+14:

$$\frac{\Sigma_{\text{H}_2}}{\Sigma_{\text{HI}}} = \frac{\Sigma_{\text{gas}}}{\Sigma_{\text{HI}}} - 1$$

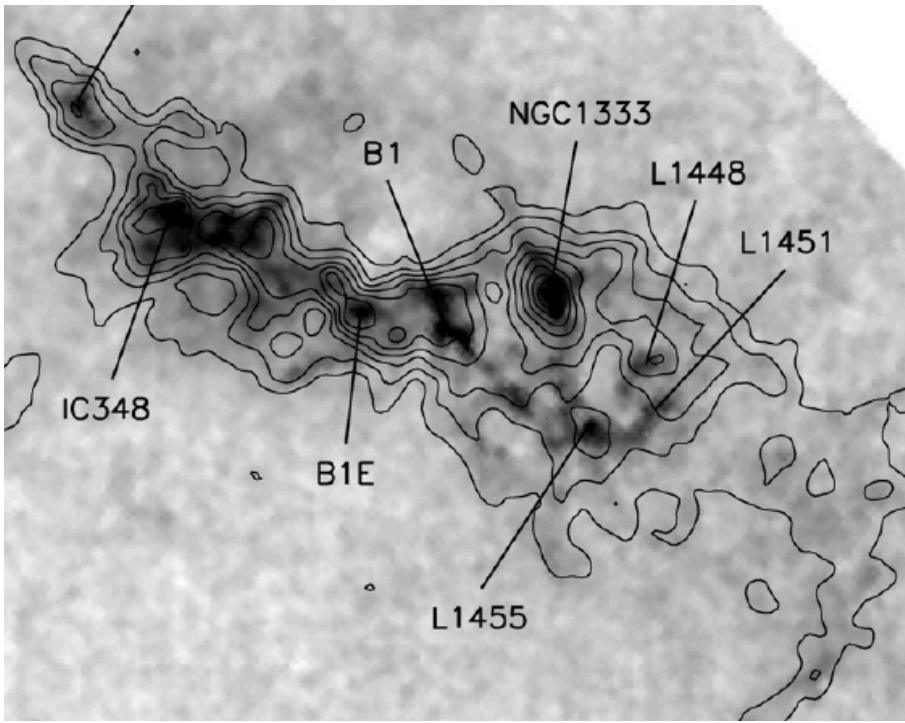
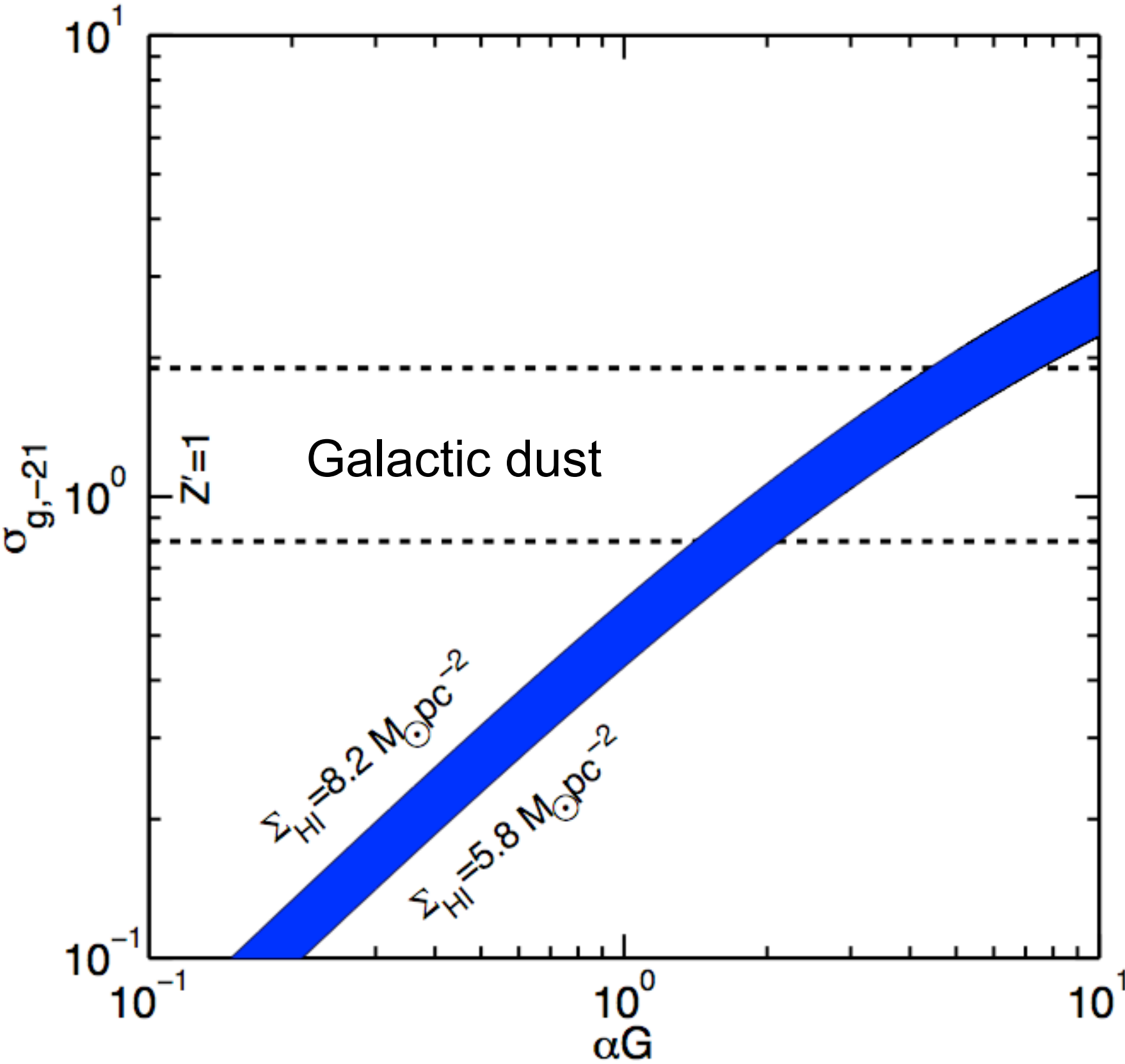
HI-to-H₂ in Perseus: Analysis

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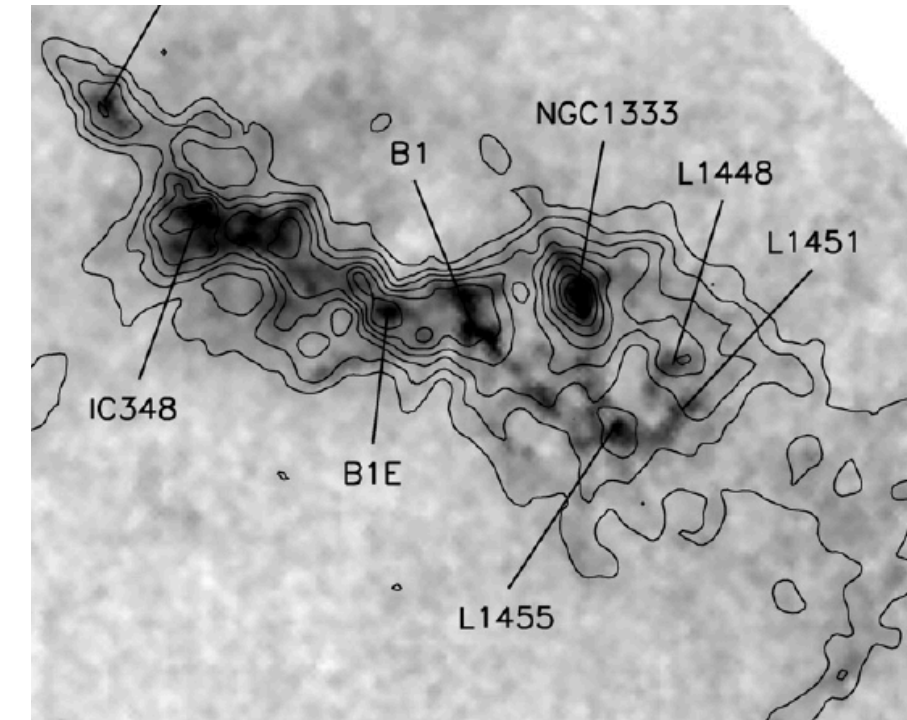
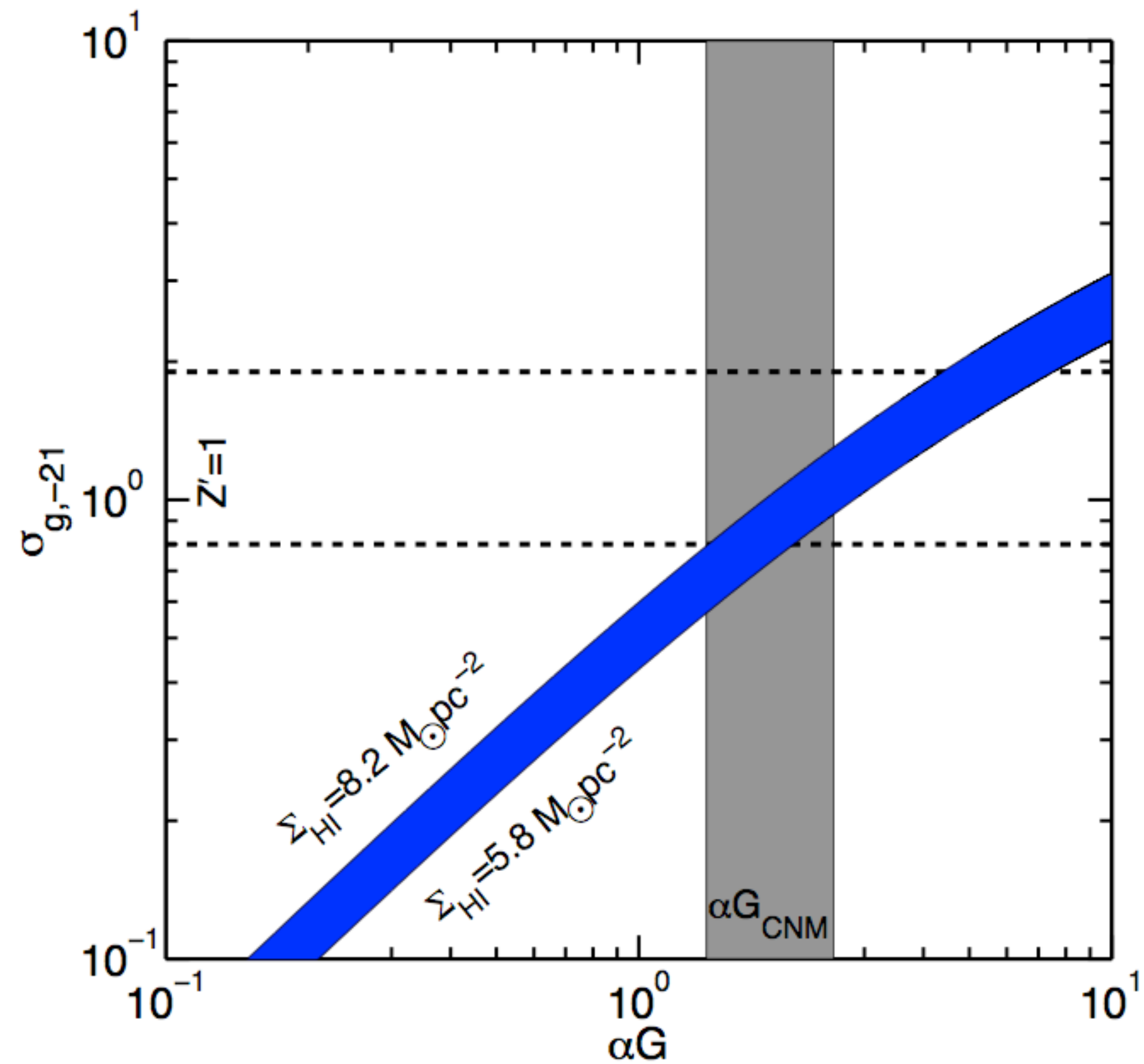
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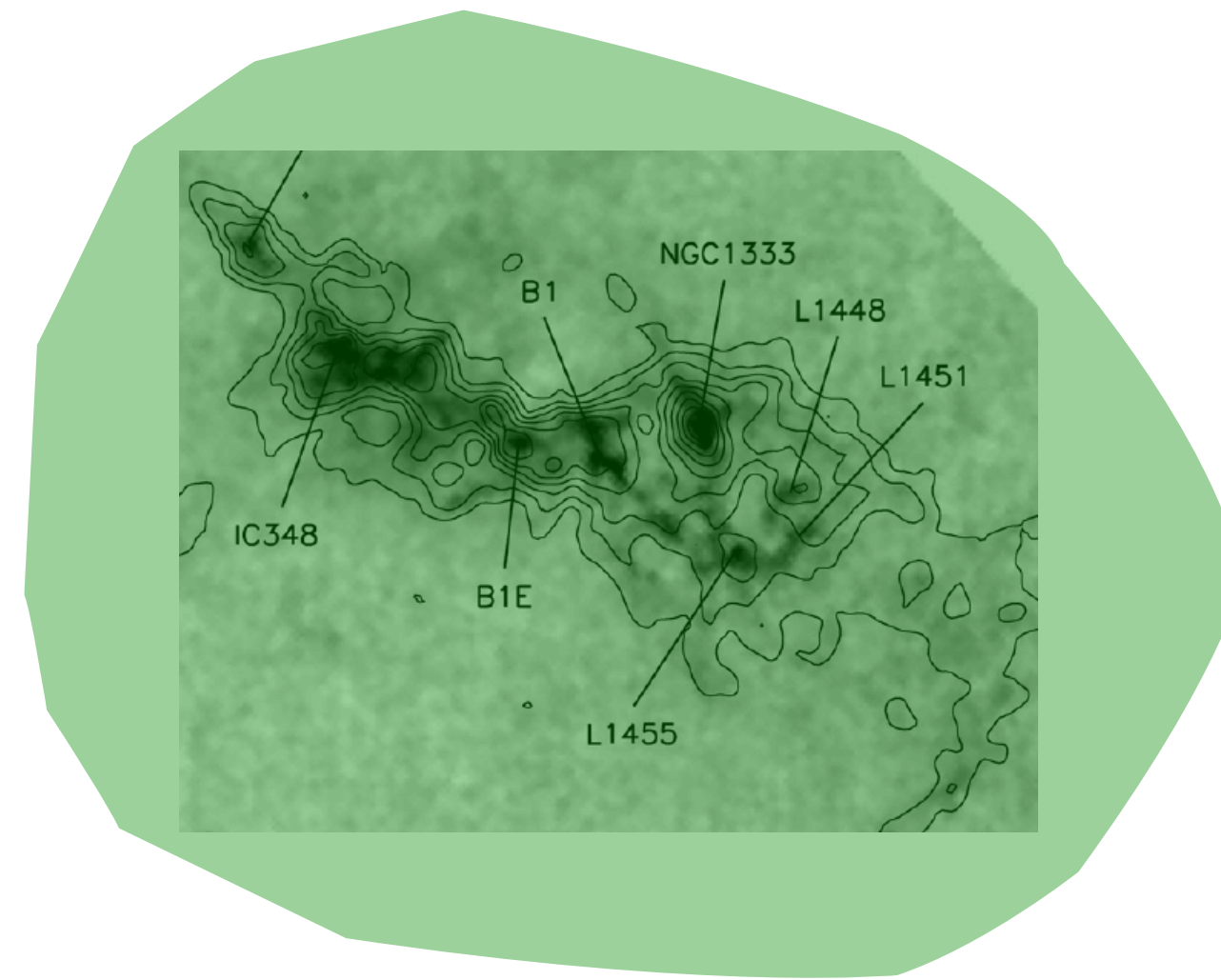
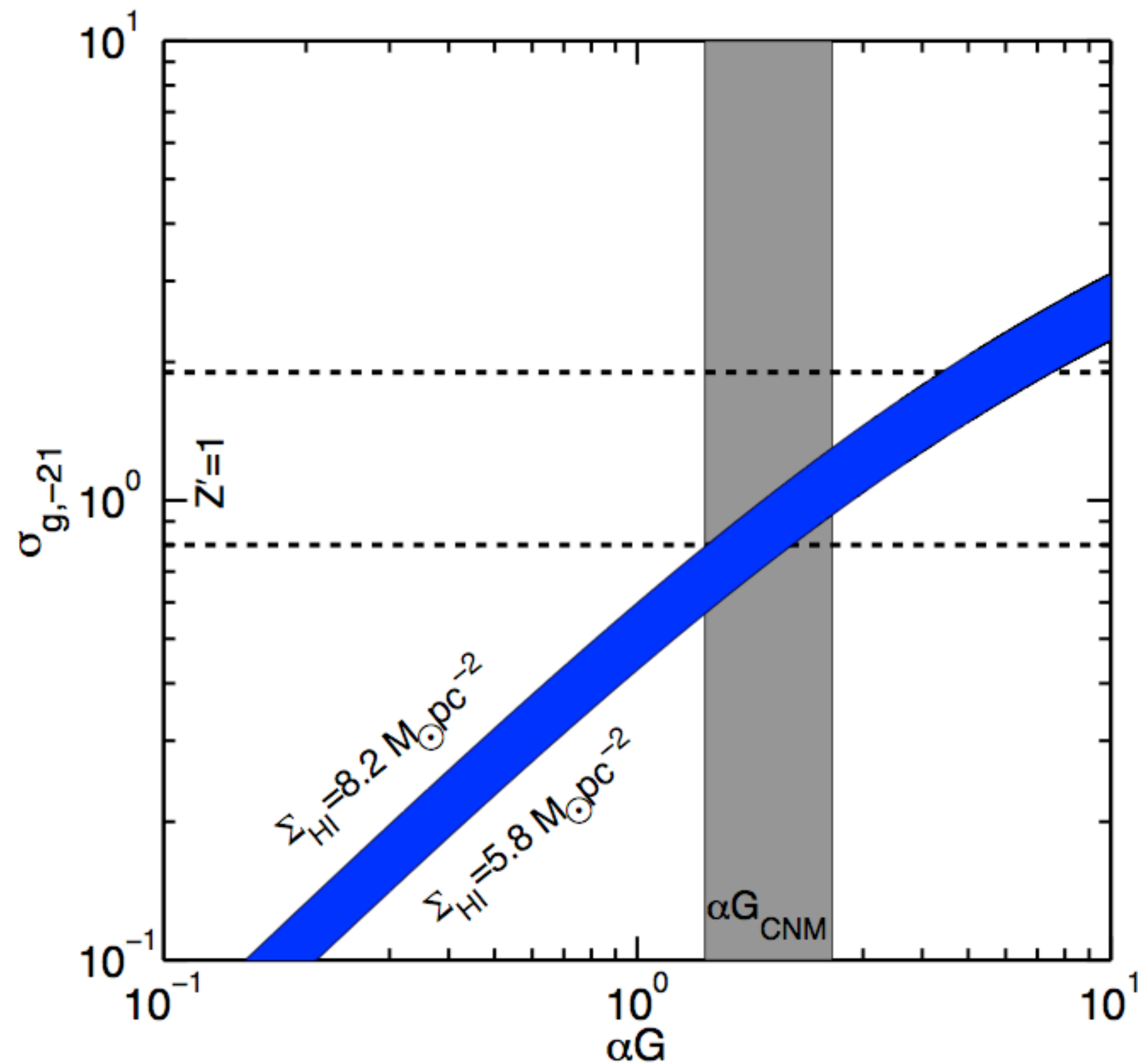
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HI-to-H₂ in Perseus: Analysis

$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln \left[\frac{\alpha G}{4} + 1 \right]$$



Galactic interstellar LW radiation field:
 $F_0 \approx 2 \times 10^7 \text{ photons cm}^{-2} \text{ s}^{-1}$

Conclusions: $\alpha G \approx 2 \text{ to } 6$

- FUV absorption dominated by HI-dust
- $n_{\text{HI}} \approx 20 \text{ to } 3 \text{ cm}^{-3}$
- consistent with CNM/WNM mixture

Galaxies:

e.g. Bigiel+ 08

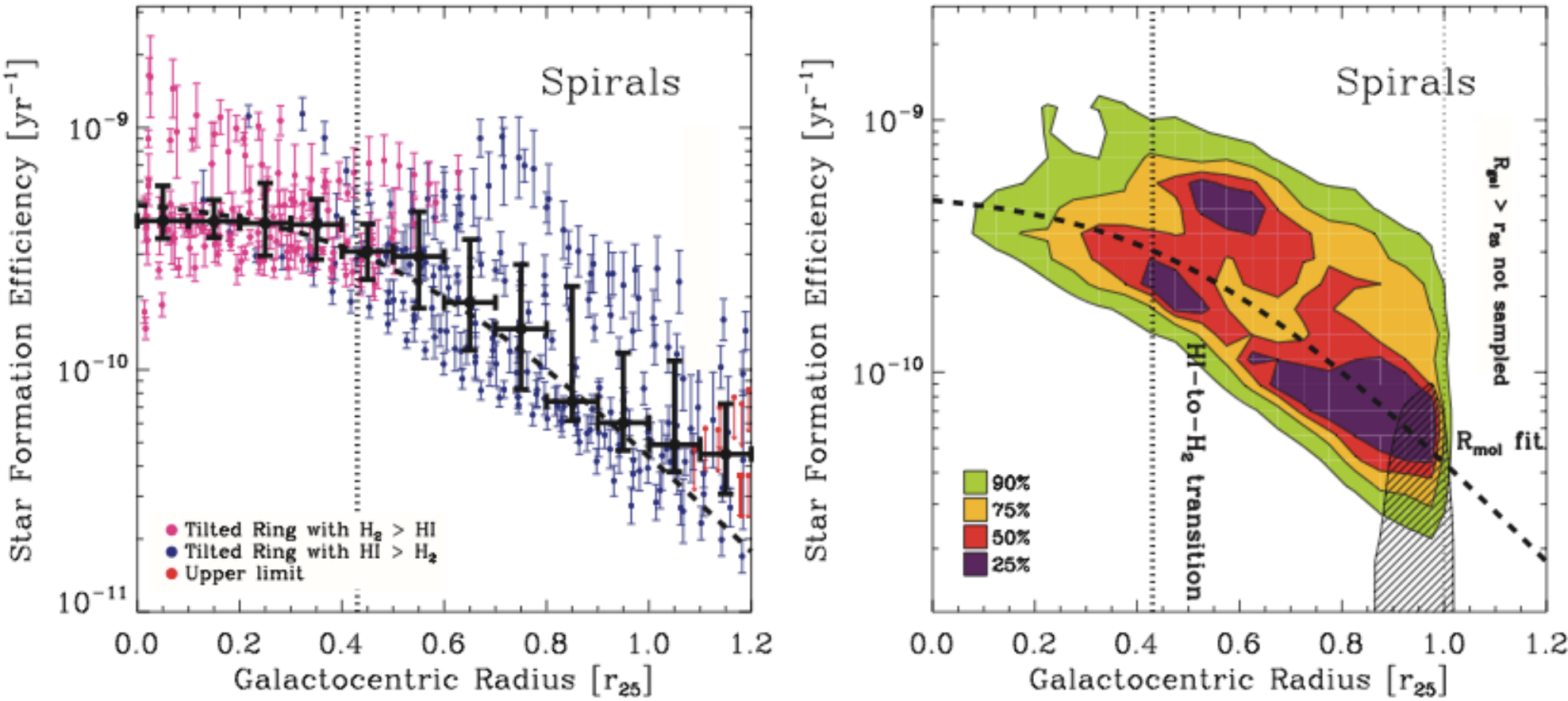
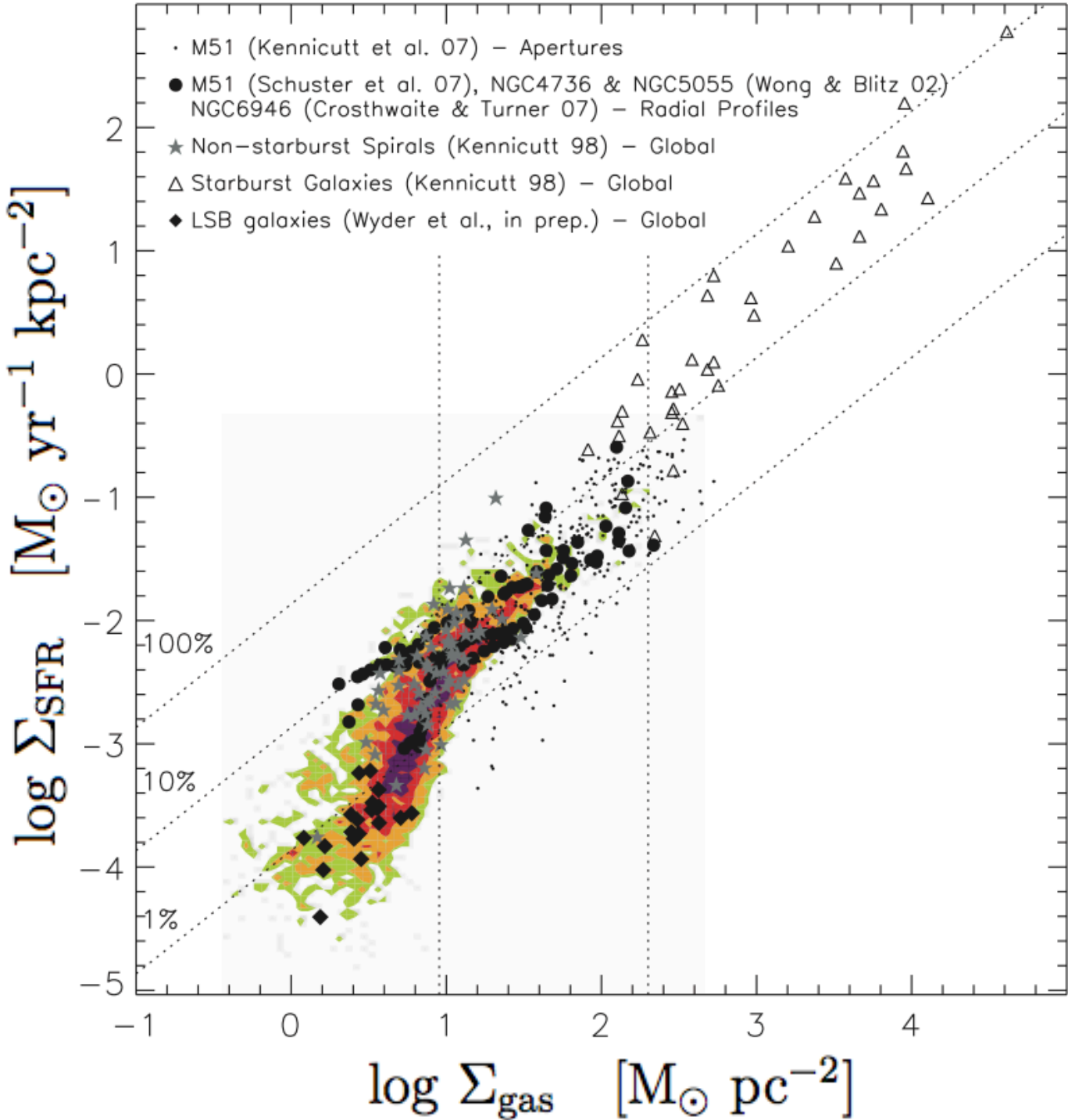


Table 5
Conditions at the H I-to- H_2 Transition

Quantity	Median Value ^a	Scatter	Scatter in log ₁₀
$r_{\text{gal}} (r_{25})$	0.43	0.18	0.17
$\Sigma_{\star} (M_{\odot} \text{ pc}^{-2})$	81	25	0.15
$\Sigma_{\text{gas}} (M_{\odot} \text{ pc}^{-2})$	14	6	0.18
$P_h/k_B (\text{cm}^{-3} \text{ K})$	2.3×10^4	1.5×10^4	0.26
$\tau_{\text{ff}} (\text{yr})$	4.2×10^7	1.2×10^7	0.14
$\tau_{\text{orb}} (\text{yr})$	1.8×10^8	0.4×10^8	0.09
Q_{gas}	3.8	2.6	0.31
$Q_{\text{stars+gas}}$	1.6	0.4	0.09



Assuming $\alpha G = (\alpha G)_{\text{CNM}}$

$$\Sigma_{\text{gas},*} \approx \frac{12}{\phi_g Z'} M_{\odot} \text{ pc}^{-2}$$

Galaxies:

e.g. Bigiel+ 08

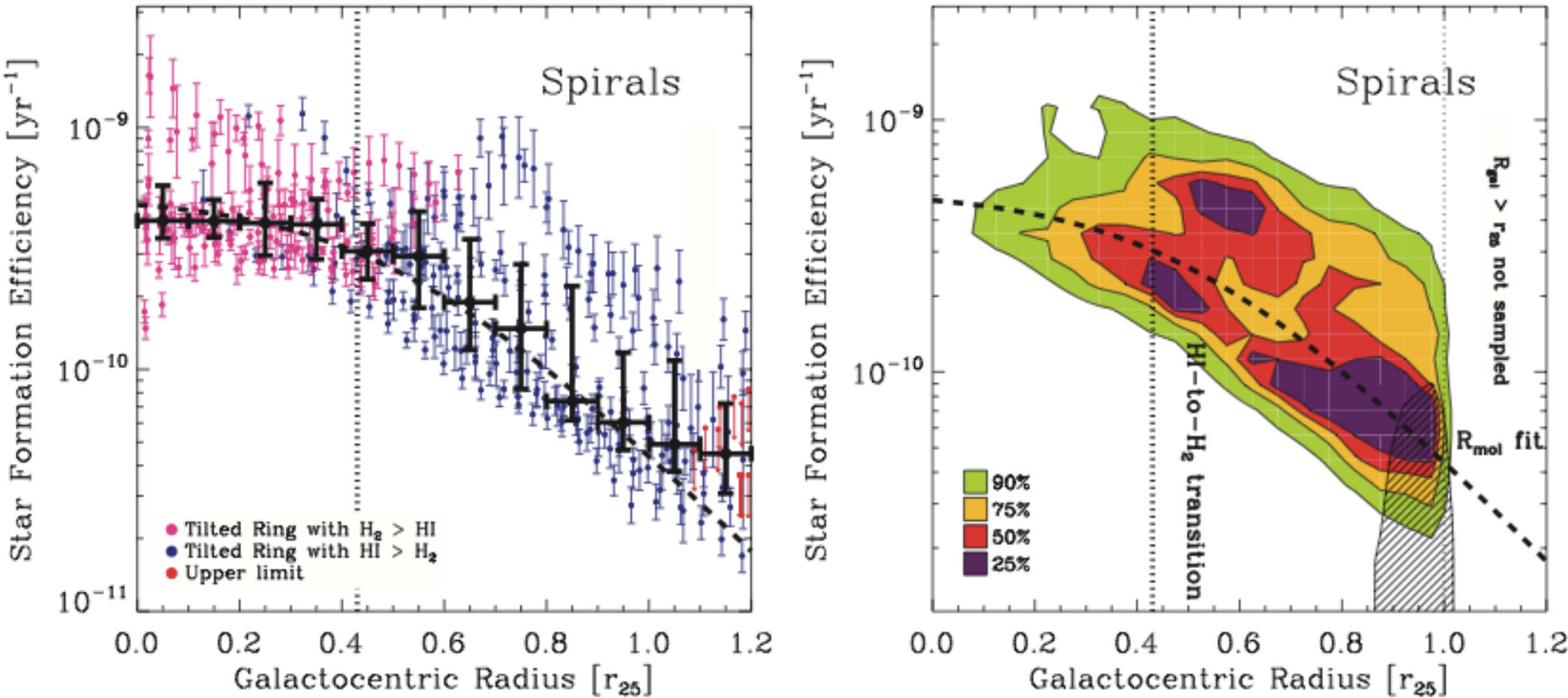
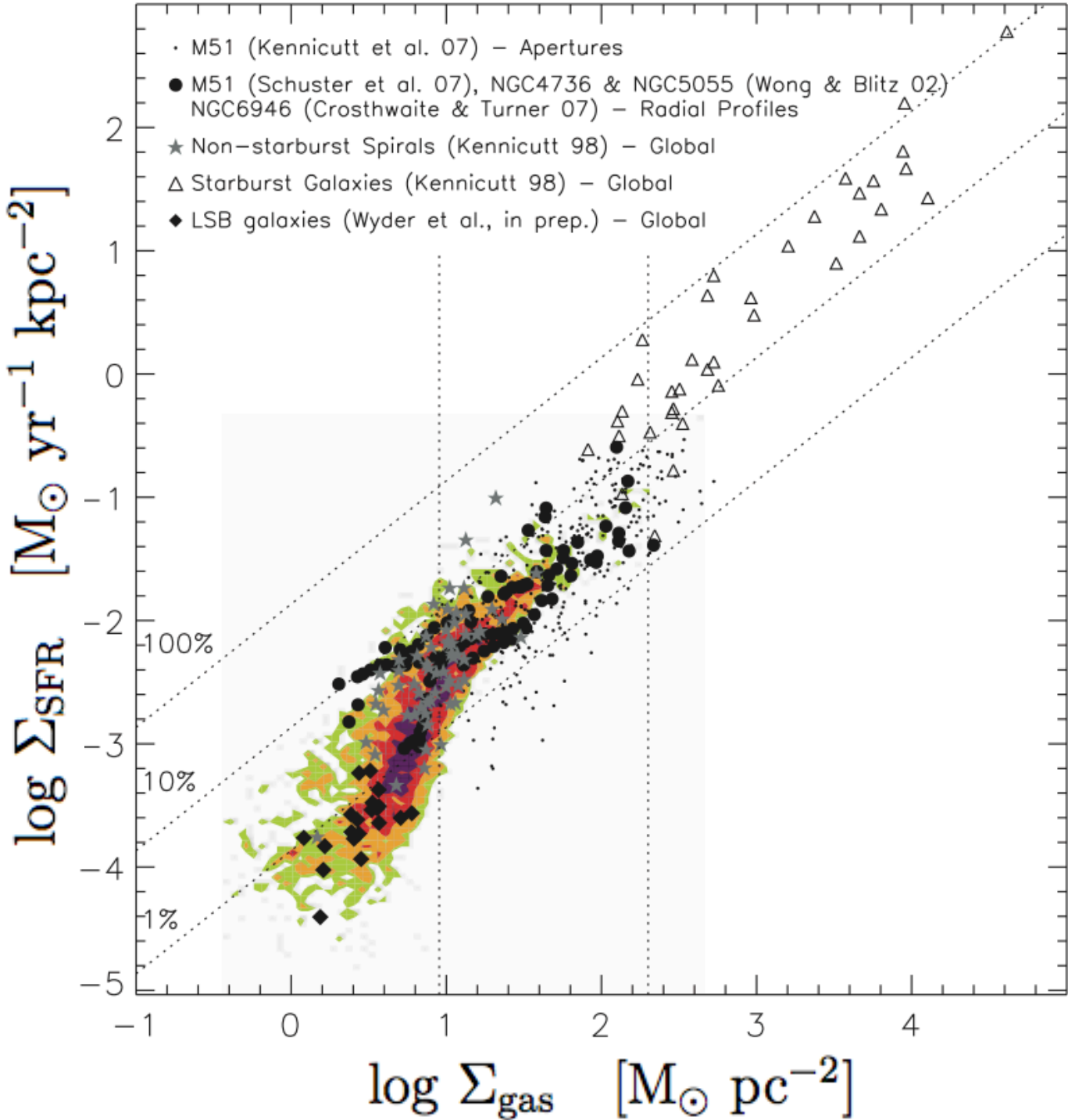


Table 5
Conditions at the H I-to-H₂ Transition

Quantity	Median Value ^a	Scatter	Scatter in log ₁₀
$r_{\text{gal}} (r_{25})$	0.43	0.18	0.17
$\Sigma_{*} (M_{\odot} \text{ pc}^{-2})$	81	25	0.15
$\Sigma_{\text{gas}} (M_{\odot} \text{ pc}^{-2})$	14	6	0.18
$P_h/k_B (\text{cm}^{-3} \text{ K})$	2.3×10^4	1.5×10^4	0.26
$\tau_{\text{ff}} (\text{yr})$	4.2×10^7	1.2×10^7	0.14
$\tau_{\text{orb}} (\text{yr})$	1.8×10^8	0.4×10^8	0.09
\mathcal{Q}_{gas}	3.8	2.6	0.31
$\mathcal{Q}_{\text{stars+gas}}$	1.6	0.4	0.09



Assuming $\alpha G = (\alpha G)_{\text{CNM}}$

$$\Sigma_{\text{gas},*} \approx \frac{12}{\phi_g Z'} \text{ M}_{\odot} \text{ pc}^{-2}$$

Caveat: This interpretation requires typically “one” primary cloud per line-of-sight.

To Conclude:

$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln\left[\frac{\alpha G}{4} + 1\right] = \frac{1}{\sigma_g} \ln\left[\frac{1}{4} \frac{\bar{f}_{\text{diss}} \sigma_g w F_0}{Rn} + 1\right]$$

HI-to-H₂ Transitions and HI Column Densities in Galaxy Star-Forming Regions

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2014 ApJ 790 10 [arXiv:1404.5042](https://arxiv.org/abs/1404.5042)