

# Formation of molecular clouds, filaments and prestellar condensations

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# Overview

**Formation of molecular clouds from diffuse gas**

**-observations**

**-2-phase turbulence**

**-formation of molecular clouds from diffuse gas**

**-statistics**

**-star formation**

**Formation of filaments and cores within molecular clouds**

**-by pure MHD turbulence**

**-by turbulence but selected by gravity**

**-by pure gravity**

**-a fully gravo-turbulent picture**

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## Formation of filaments and cores within molecular clouds:

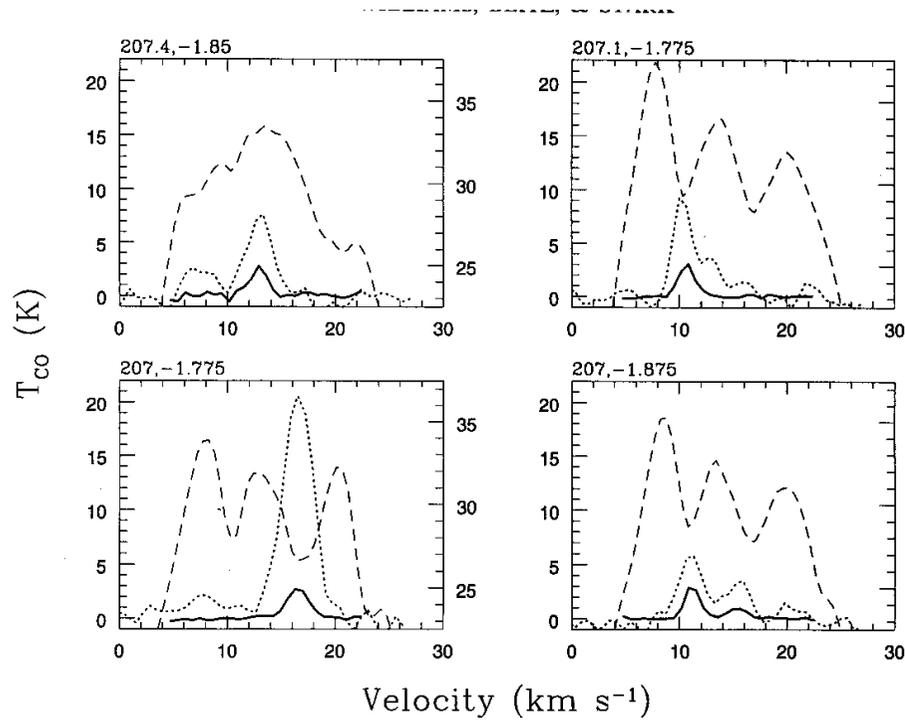
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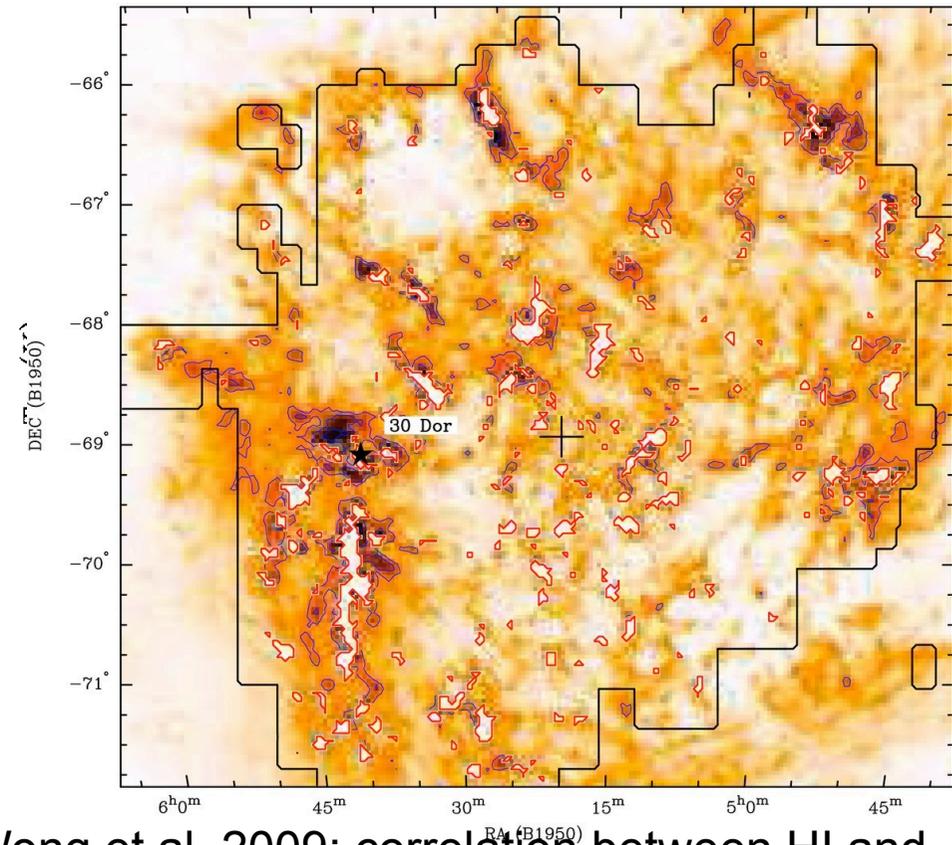
-by pure gravity

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# Tight correlation between HI and CO



Williams, Blitz and Stark 1994  
Infer a close anti-correlation between  
HI and CO emission in the Rosette MC

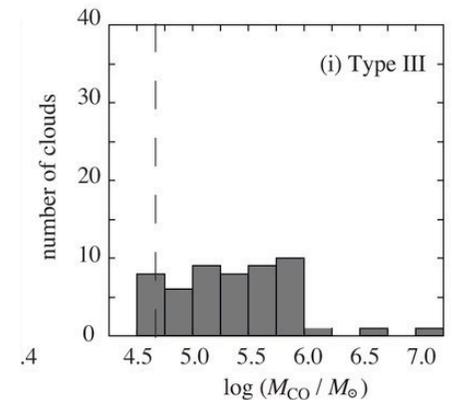
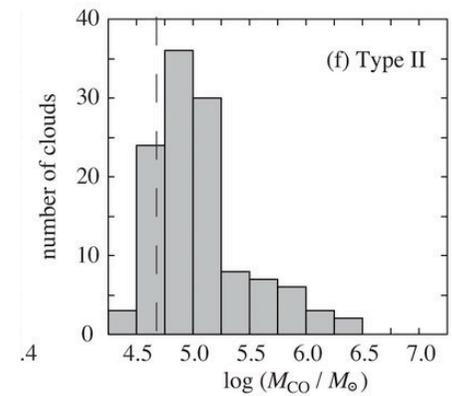
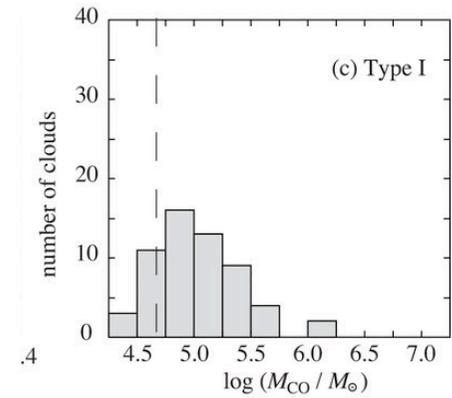
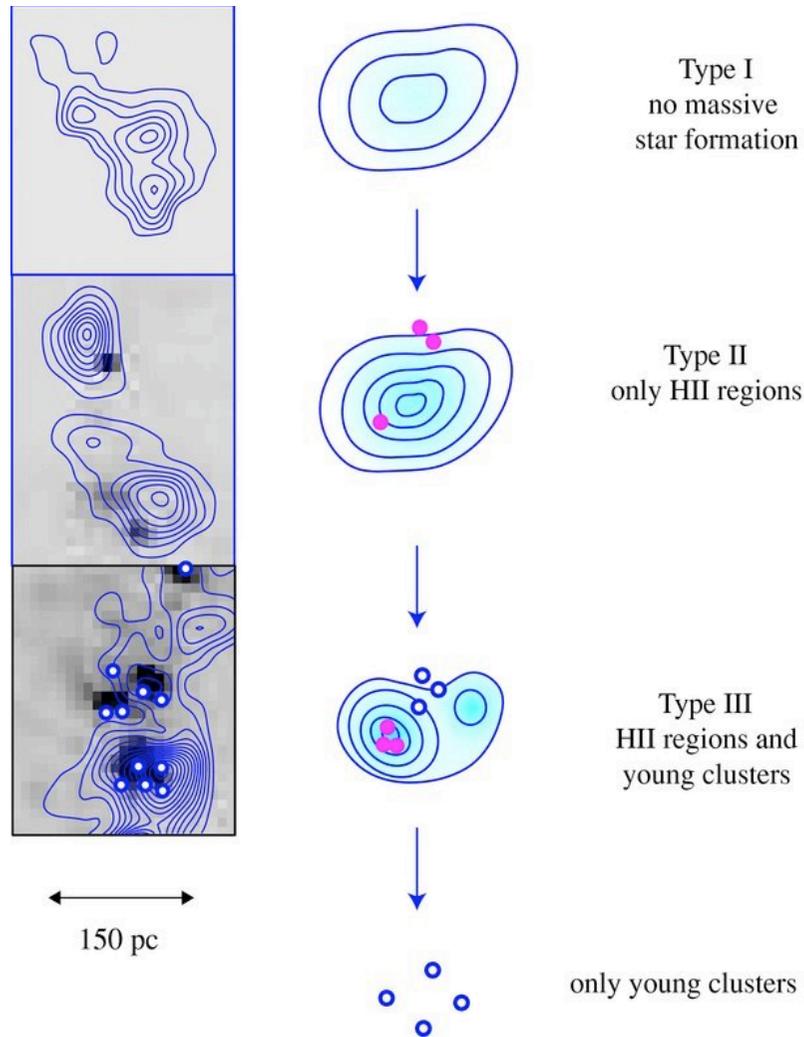


Wong et al. 2009: correlation between HI and  
CO in the LMC (second Nanten survey)

CO peak always associated with HI but HI not  
always associated to CO.

# Molecular clouds in the LMC (Blitz et al. 07, Kawamura et al. 09, Fukui & Kawamura 2010)

## An evolutionary sequence ?



=> accretion rate onto GMC: few times  $10^{-2} M_{\odot} / \text{yr}$  ?

# Formation of molecular clouds from diffuse HI

Molecular clouds form out of the HI and are surrounded by an HI halo

=>Suggest that connecting MC and HI spatially and temporally could be important

Attempt to form MC starting from atomic gas is important :

-self-consistent way of generating structures within the cloud

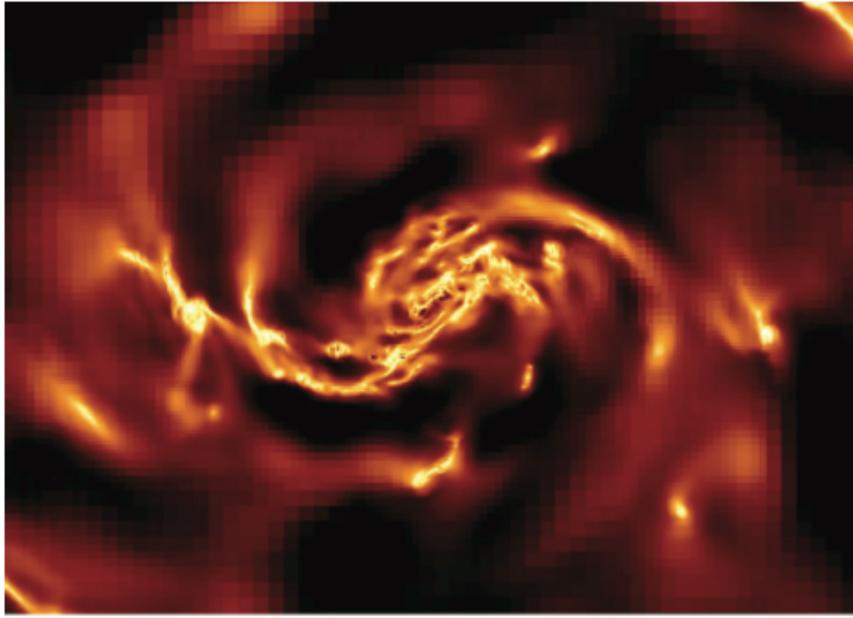
-self-consistent energy input from the outside

(non star forming cloud have a significant amount of turbulence)

At large scales, from the galactic disk: [de Avillez & Breitschwert 05](#), [Young & MacLow 06](#), [Dobbs et al. 06](#), [08](#), [Tasker & Tan 09](#), [Bournaud et al. 08](#)

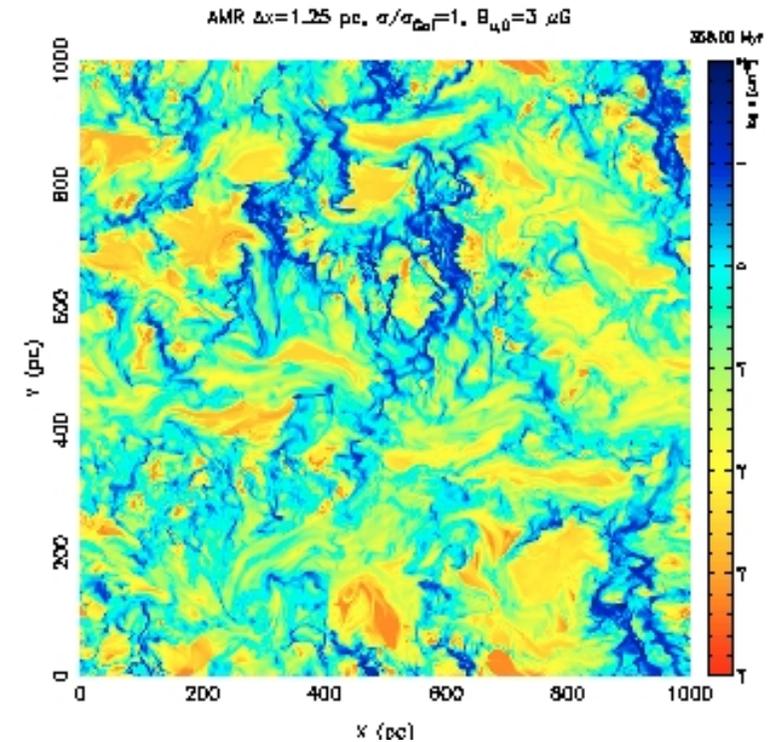
Focussing on a single cloud: [Vazquez-Semadeni et al. 2007](#), [2011](#), [Hennebelle et al. 2008](#), [Banerjee et al. 2009](#), [Heitsch et al. 2008](#), [Inoue et al. 2009](#)

## Simulating whole galaxies



Bournaud et al. 2010

## Simulating parts of galaxies



de Avillez 2005

In all cases the dense form by condensation of the diffuse gas

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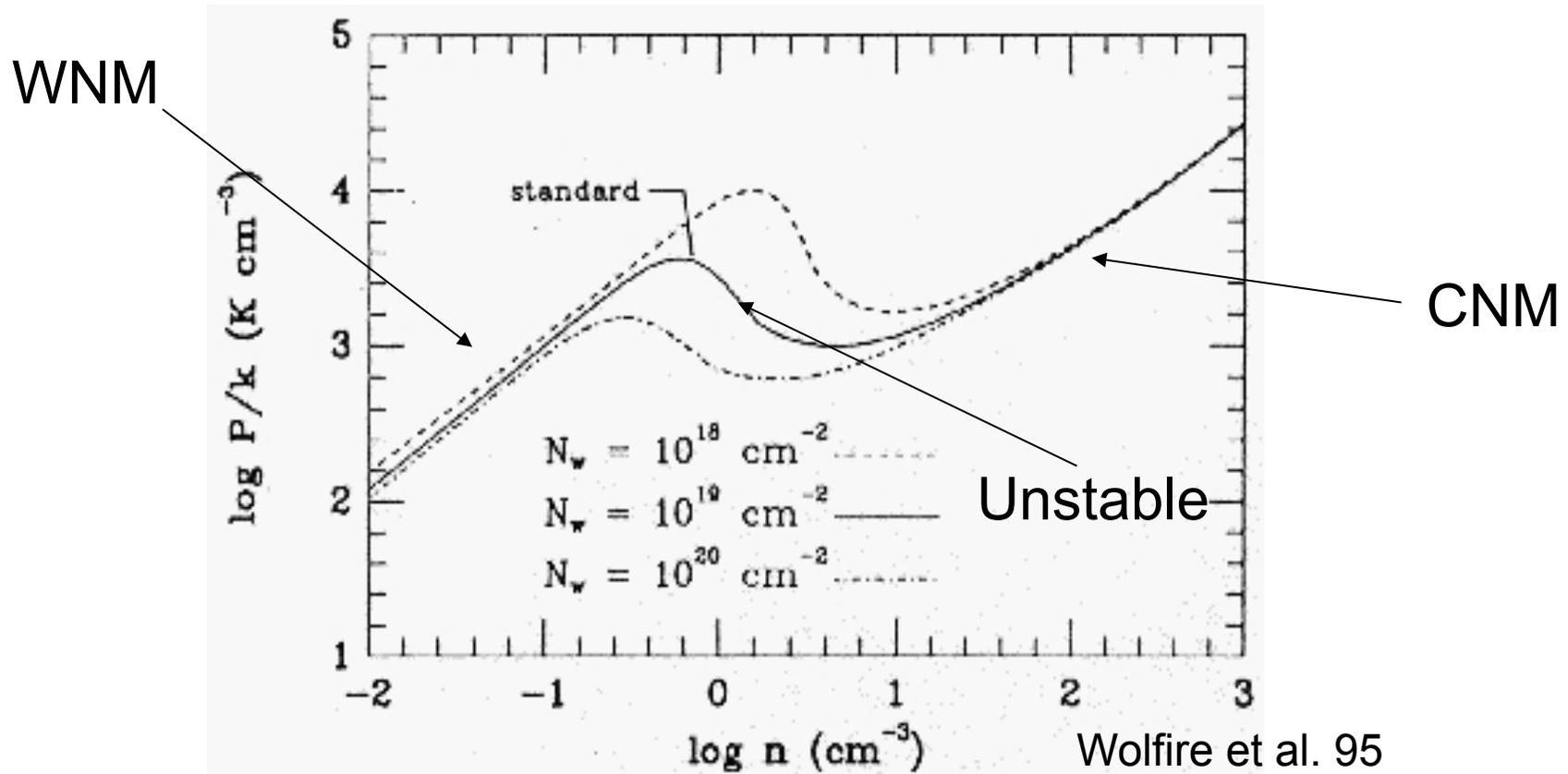
-by turbulence but selected by gravity

-by pure gravity

-a fully gravo-turbulent picture

## 2-phase structure of the ISM

Thermal equilibrium curve (Field et al. 69, Wolfire et al. 95)



Field 65: performs linear stability analysis of the radiatively cooling fluid equations. Obtains the isobaric criteria for instability:

$$\left. \frac{\partial P}{\partial \rho} \right)_{L=0} \leq 0$$

# Thermal transition induced by the propagation of a shock wave

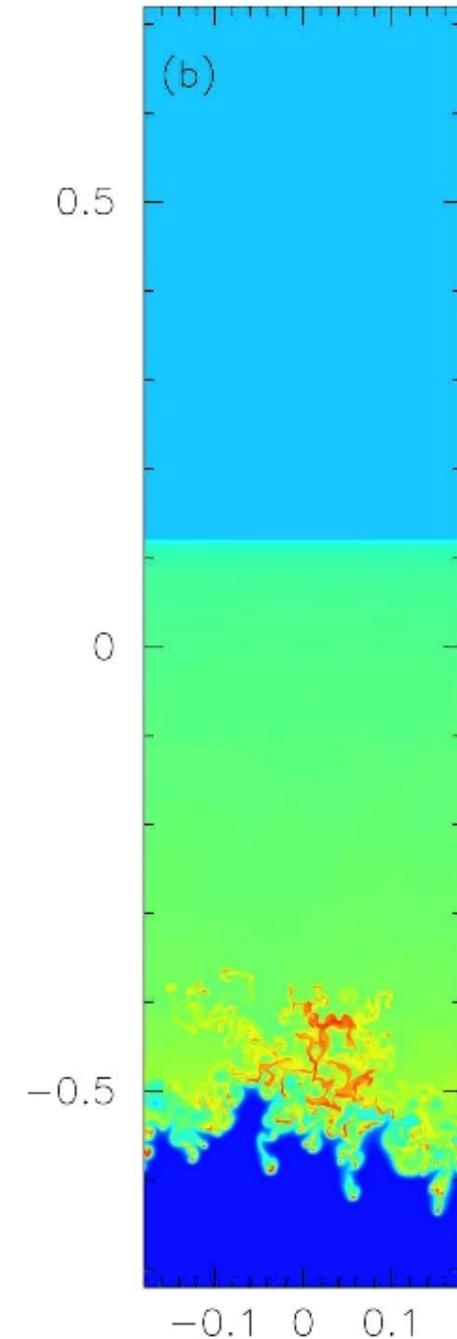
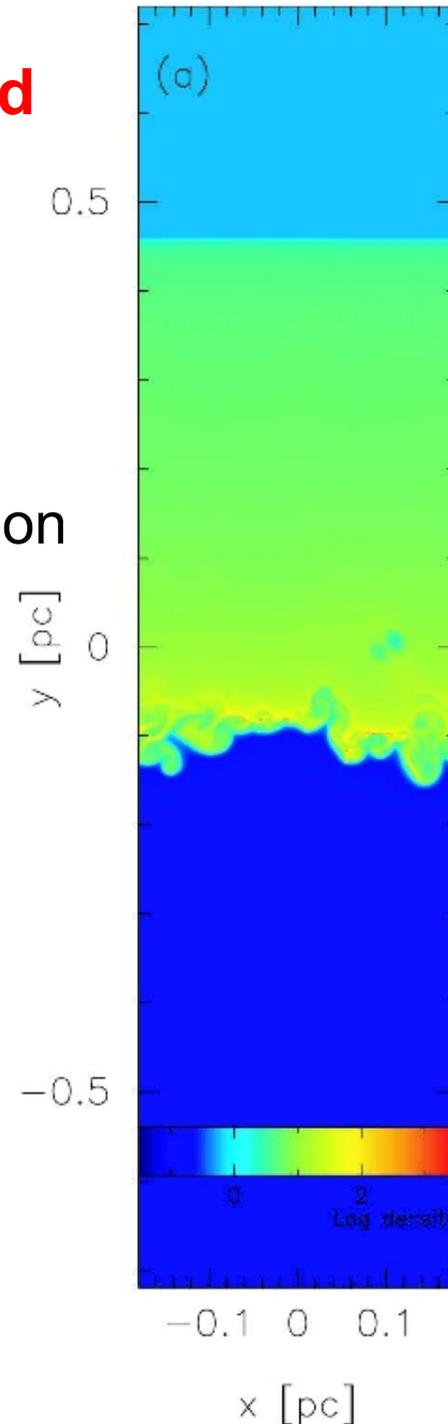
(Koyama & Inutsuka 02)

2D, cooling and thermal diffusion

The shock is unstable and thermal fragmentation occurs.

**The flow is very fragmented**  
**Complex 2-phase structure**

The velocity dispersion of the fragments is a fraction of the WNM sound speed.



# **Turbulence within a bistable fluid**

(Koyama & Inutsuka 02,04, Kritsuk & Norman 02, Gazol et al. 02, Audit & Hennebelle 05, 07, 10, Heitsch et al. 05, 06, 08, Vazquez-Semadeni et al. 06, 07)

**-Forcing from the boundary**

-Statistical stationarity reached

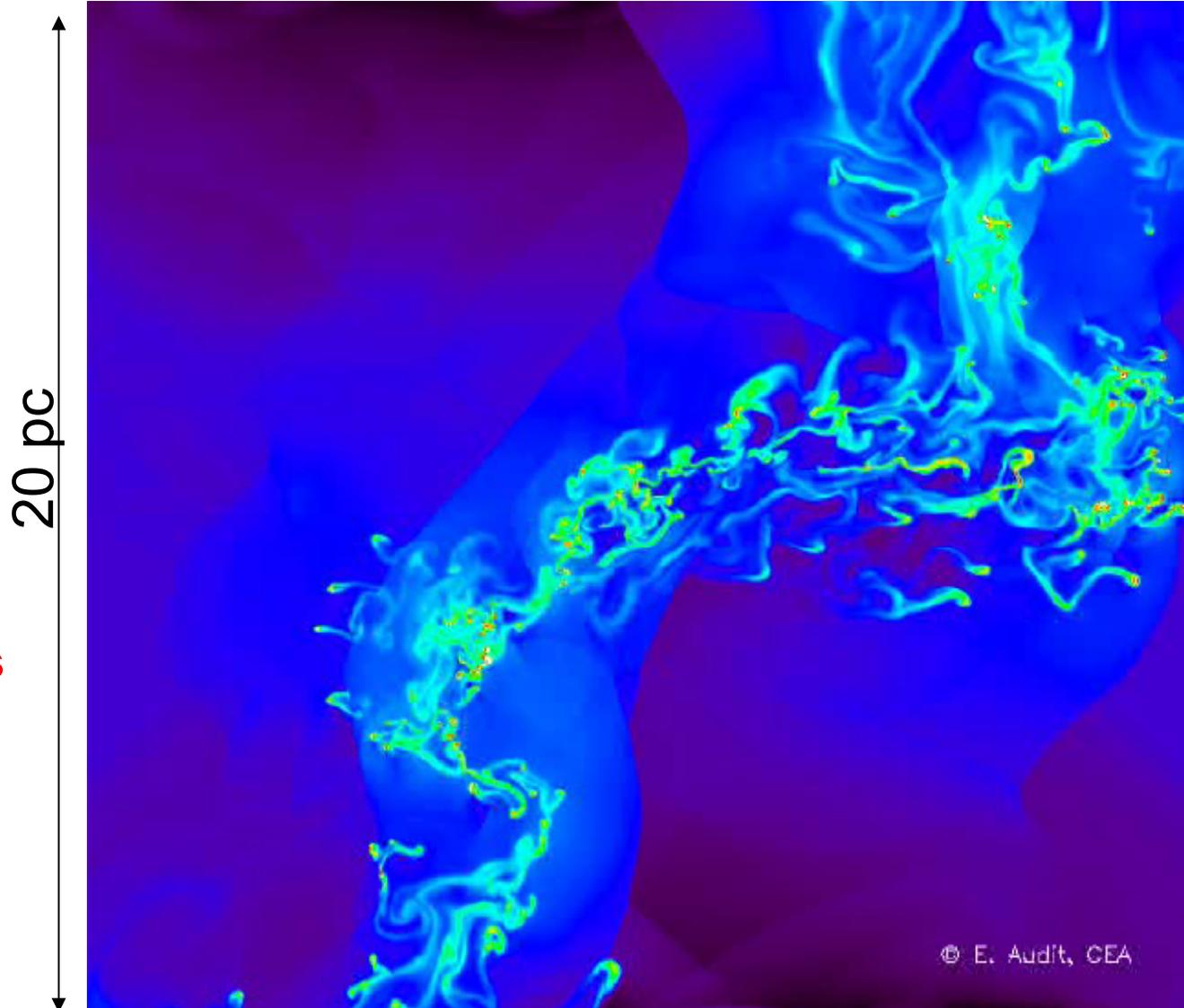
-complex 2-phase structure

-cnm very fragmented

**-turbulence in CNM is maintained by interaction with WNM**

2500<sup>2</sup>

Audit & Hennebelle 05



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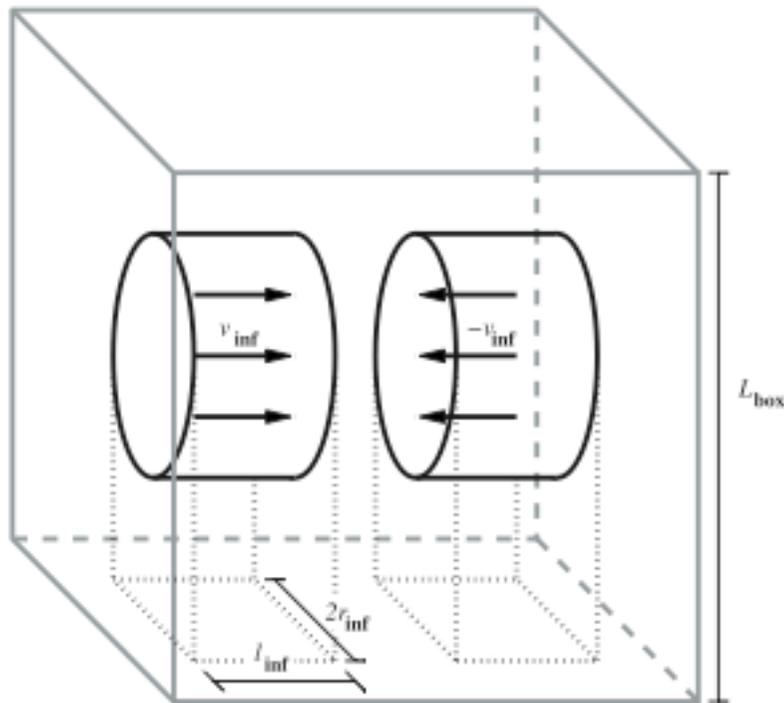
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# Formation of a *molecular clouds* from HI

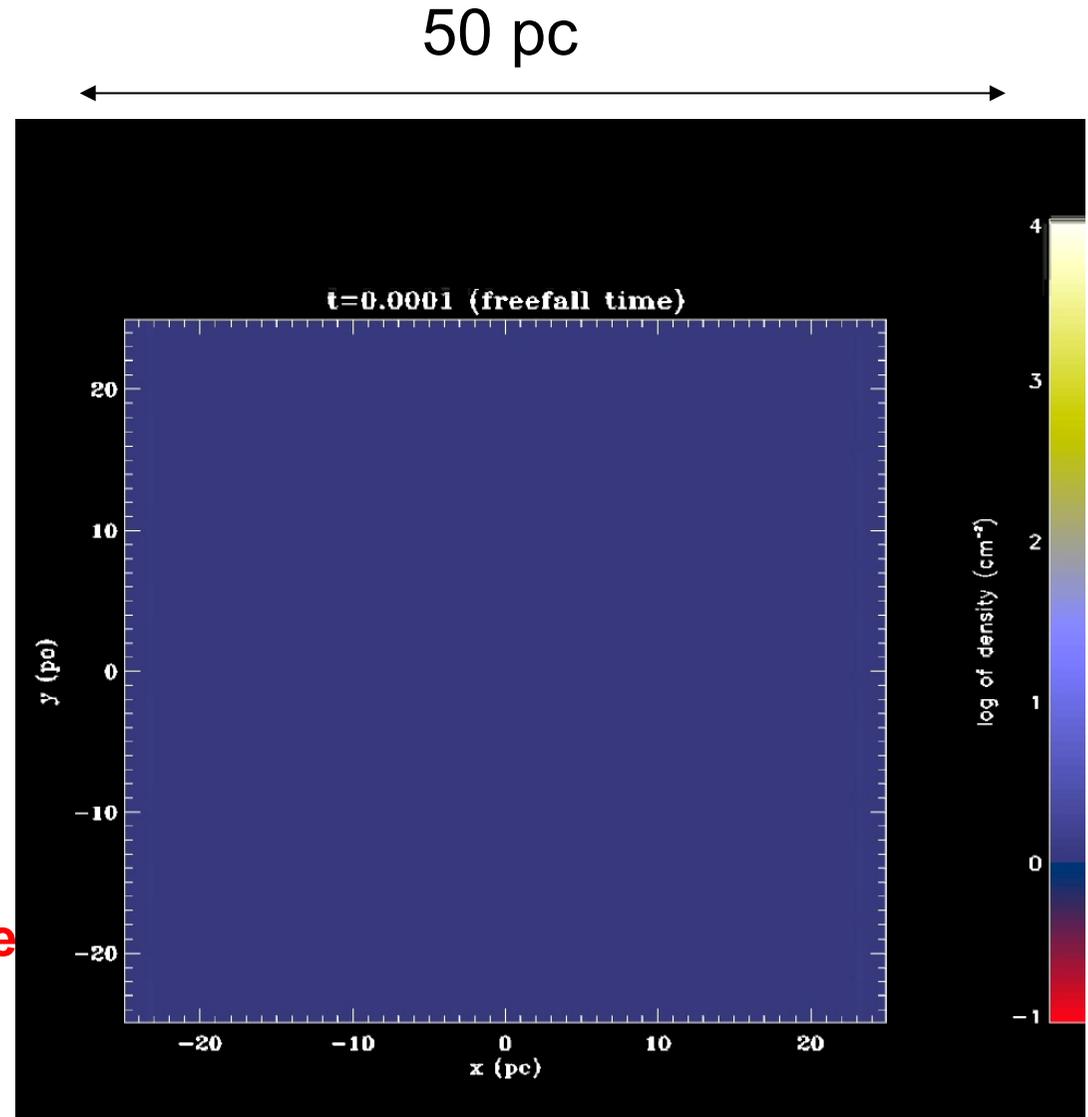
(Vazquez-Semadeni et al. 07, Hennebelle et al. 08, Heitsch et al. 08, Banerjee et al. 09)

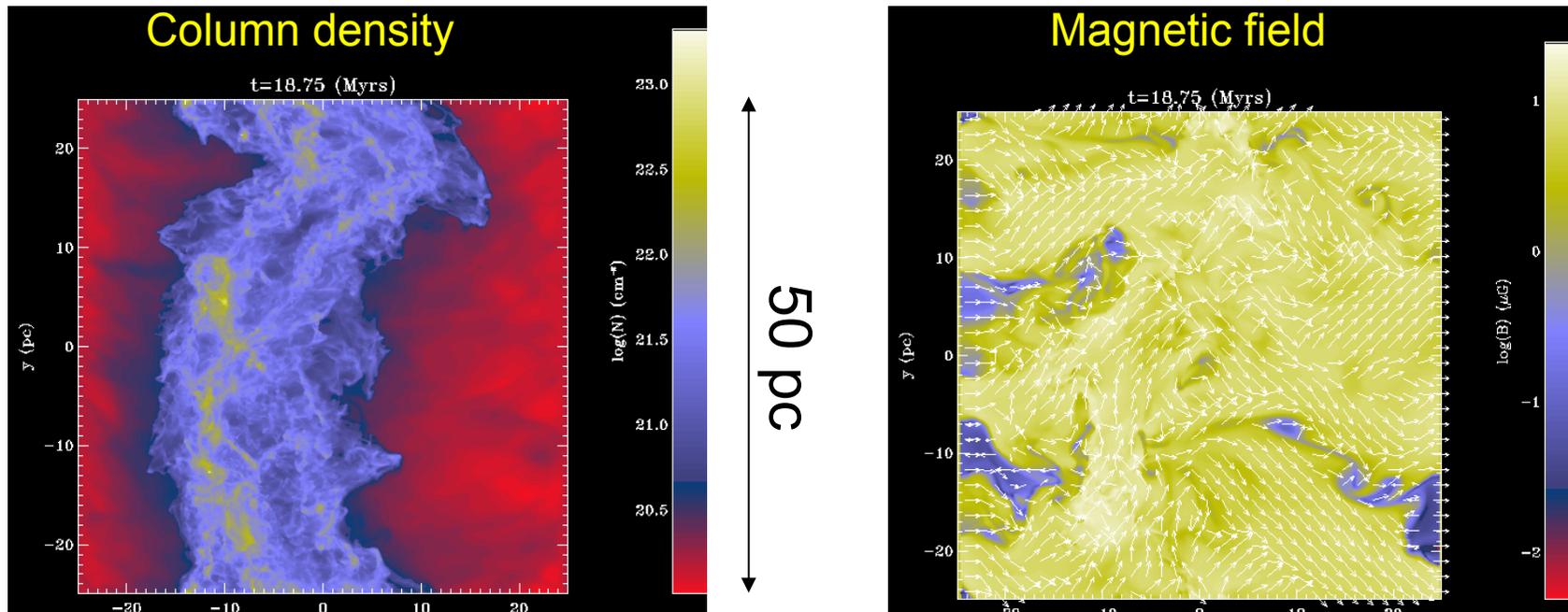
Flow of WNM (density 1cc), velocity 20km/s each side, initial magnetic field 5 $\mu$ G

Colliding flows...

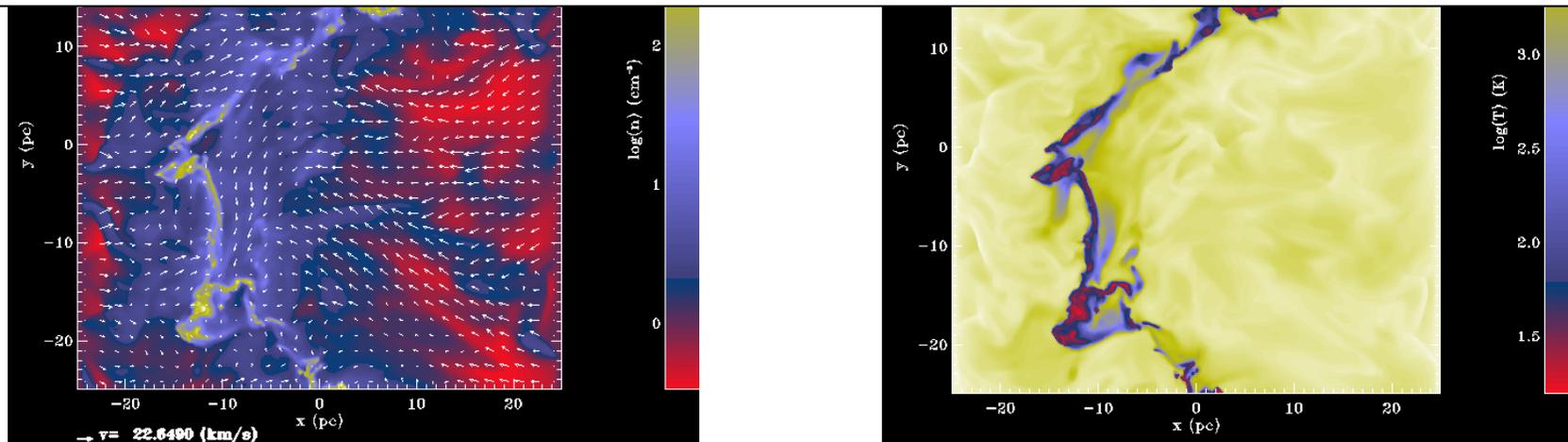


...are a theorist simplistic view. Better picture: large scale compressible turbulence.

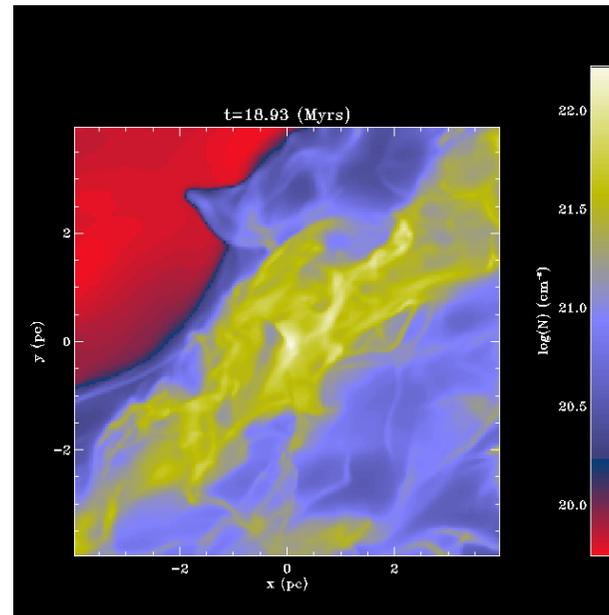




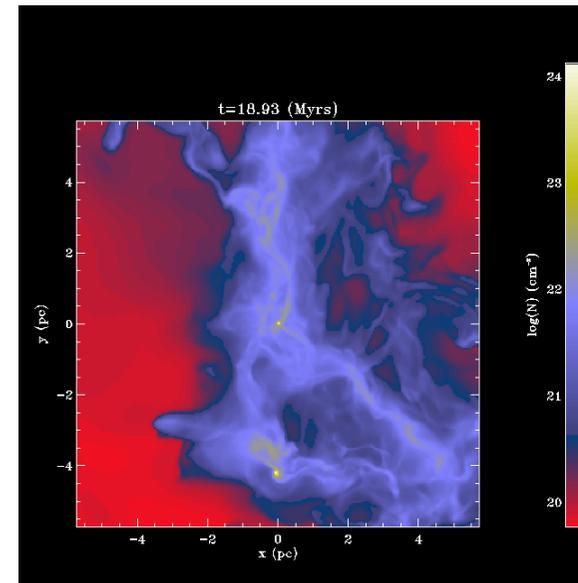
Although the cloud appears as a single phase entity in projection, its structure is not very different from the CNM/WNM structure. Clumps are bounded by WNM which provides them a confining pressure.



# Few examples of clumps

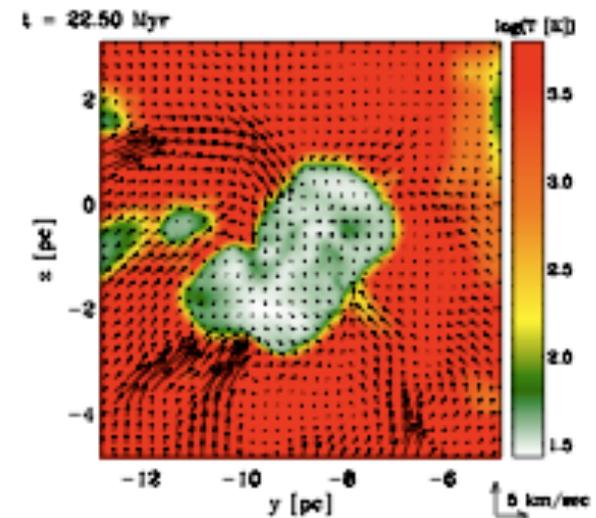
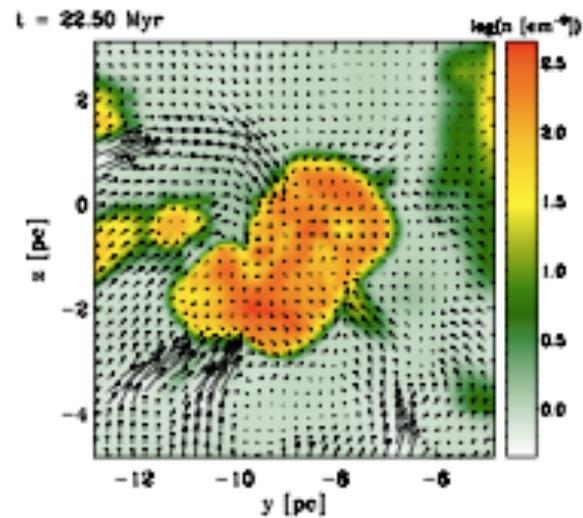


Starless



Star already formed

Banerjee et al. 09



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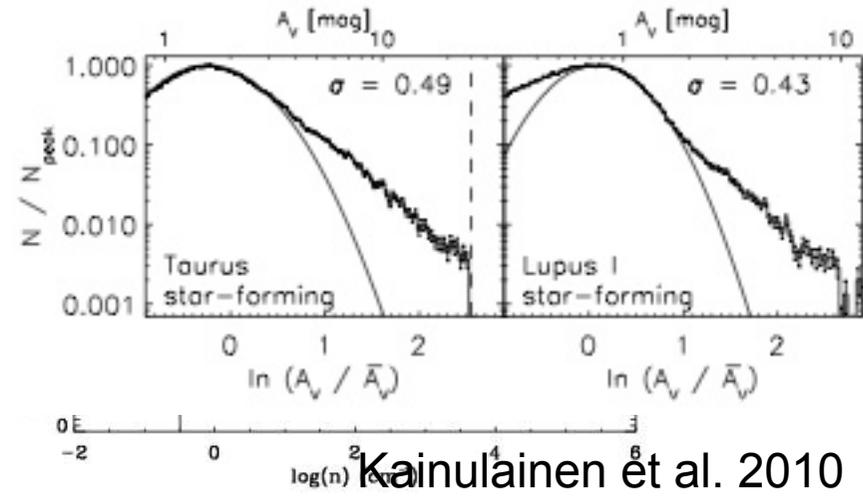
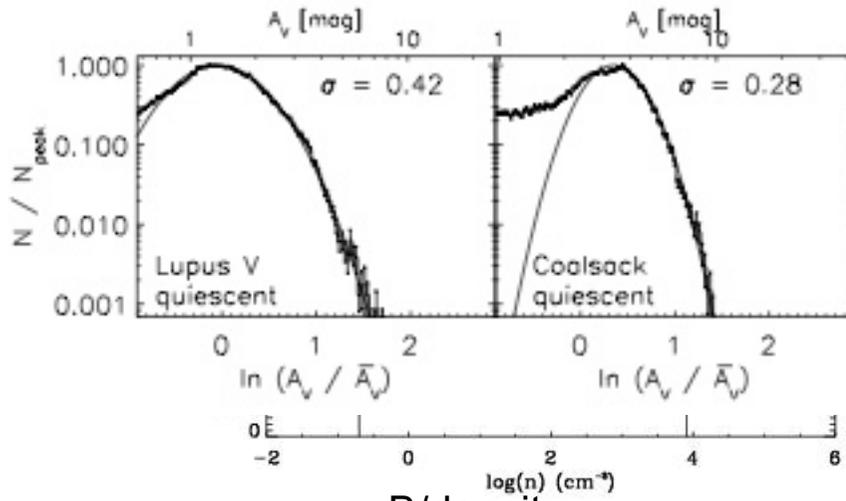
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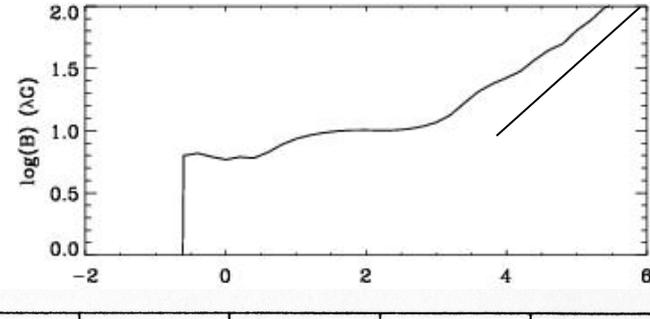
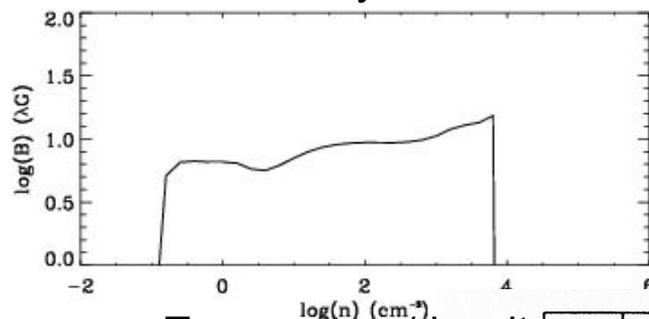
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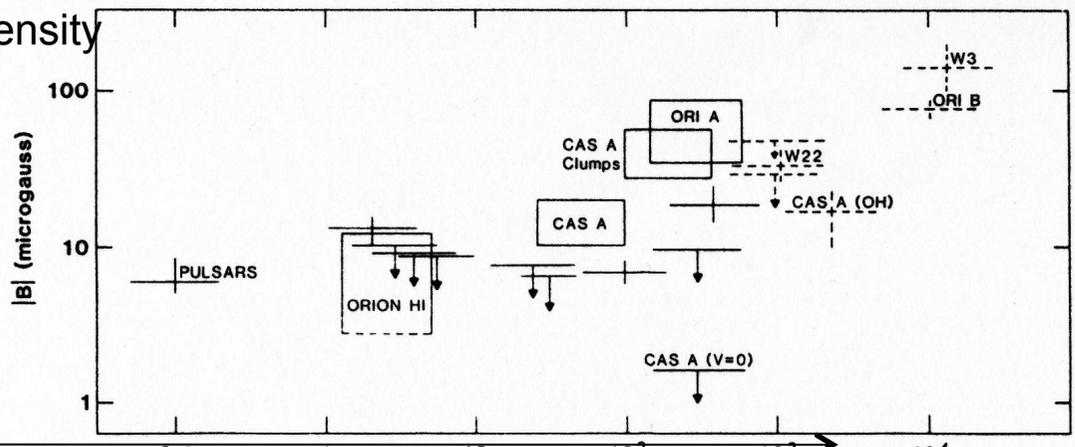
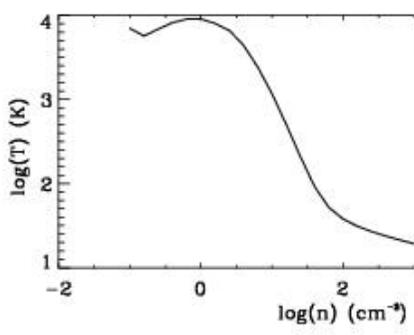
Kainulainen et al. 2010

B/density



$$B \propto \rho^{1/2}$$

Temperature/density



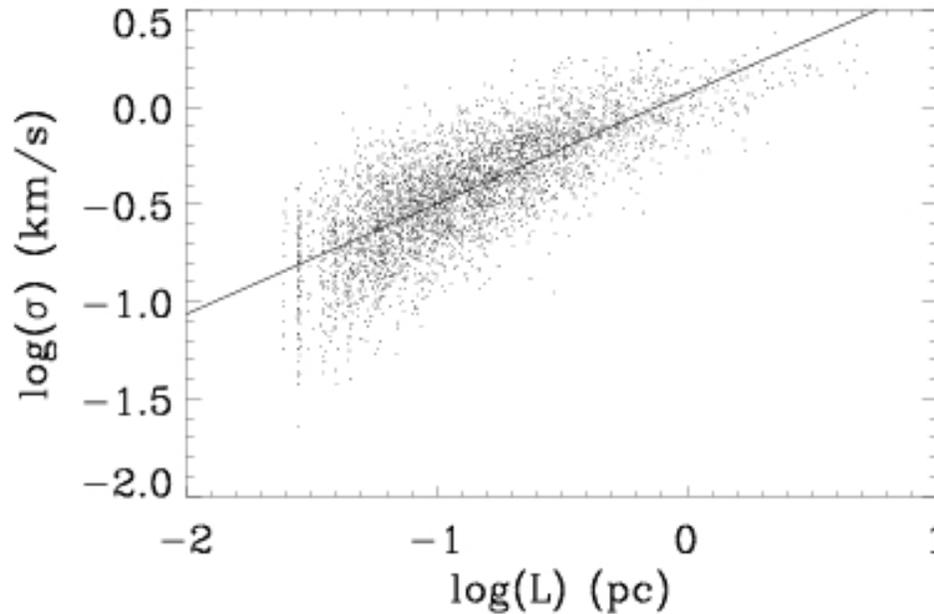
Troland & Heiles 1986

Vazquez-Semadeni 1994, Kritsuk et al. 2007, Hennebelle et al. (2008), Banerjee et al. (2009)

## Internal clump velocity dispersion

(density  $> 2500 \text{ cm}^{-3}$ )

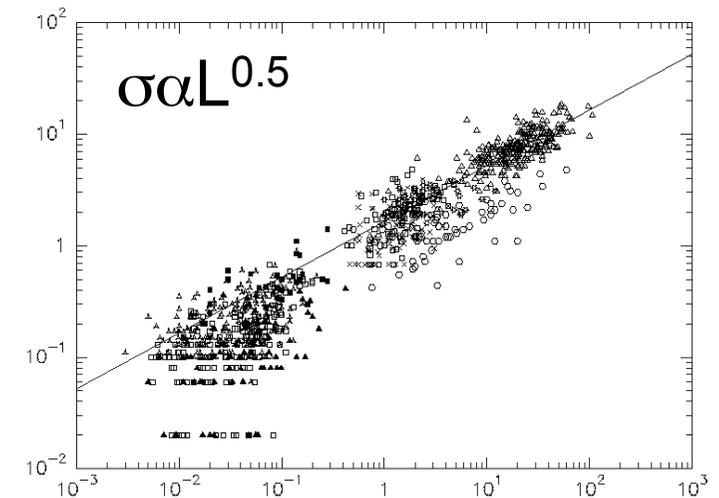
$$\sigma(L) \approx 1 \text{ km s}^{-1} (L/1 \text{ pc})^{0.5}$$



Compatible with Larson law  
=> is turbulence within GMC driven from outside ?  
=> is it driven by continuous accretion of HI ?

Klessen & Hennebelle (2010)

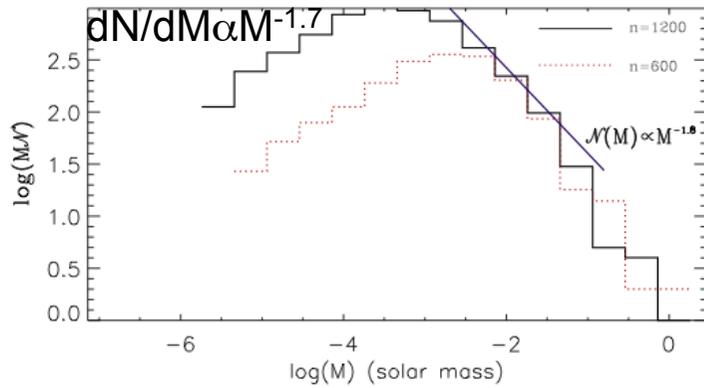
Goldbaum et al. (2011)



Falgarone 2000

# Mass spectrum and mass size

Mass spectrum of clumps

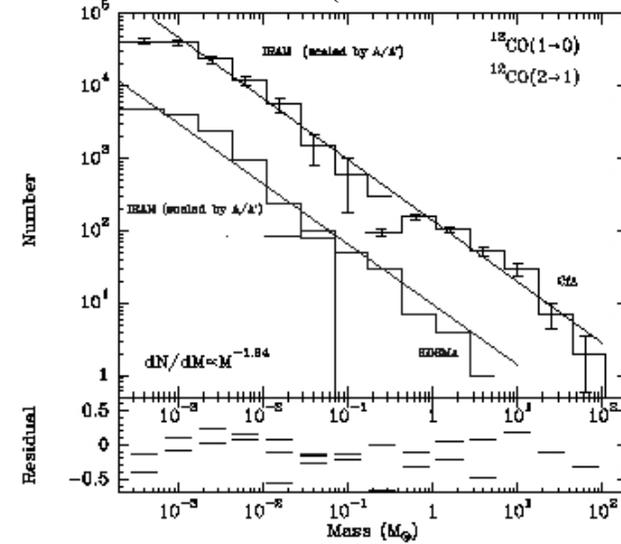


Link between the Kolmogorov exponent and the CO clump power spectrum

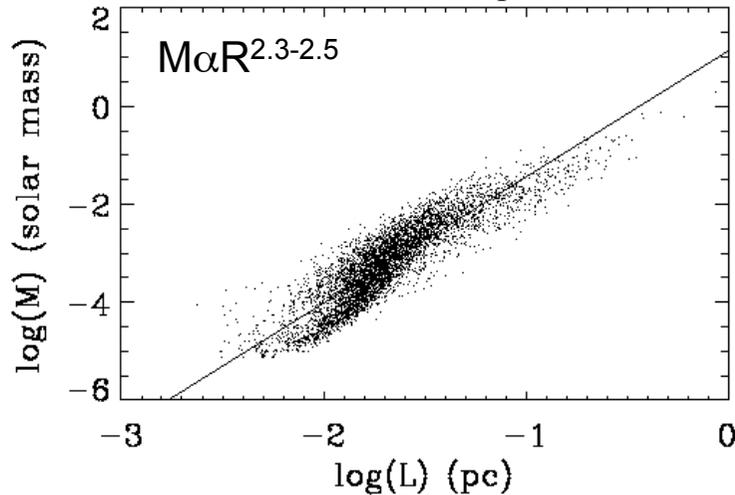
$$\frac{dN}{dM} = M^{-\left(2 - \frac{n' - 3}{3}\right)}$$

$$n' = \frac{11}{3} \Rightarrow \frac{dN}{dM} \propto M^{-1.78}$$

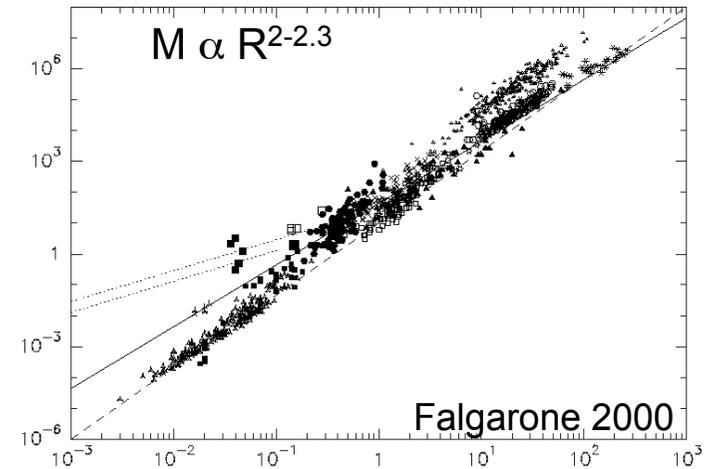
Universal Mass Spectrum  $dN/dM \propto M^{-1.6-1.8}$  (Heithausen et al .98)



Mass versus size of clumps



Mass versus size of CO clumps



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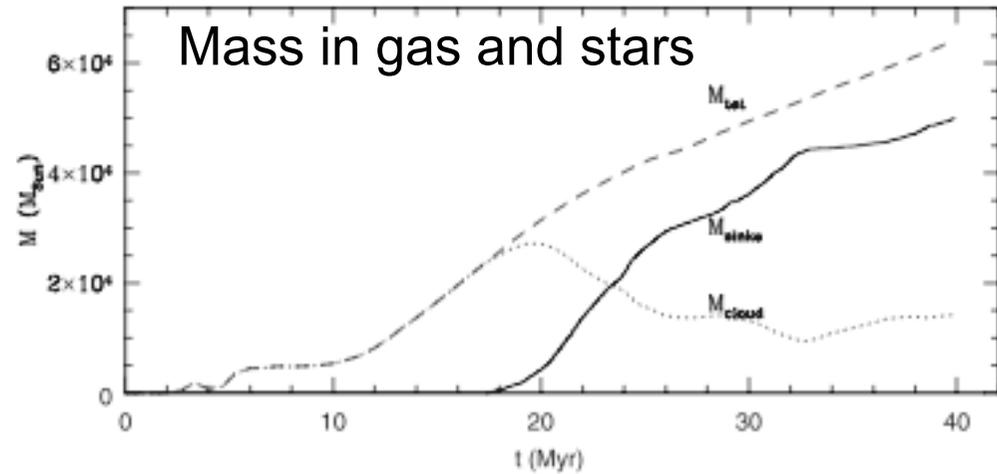
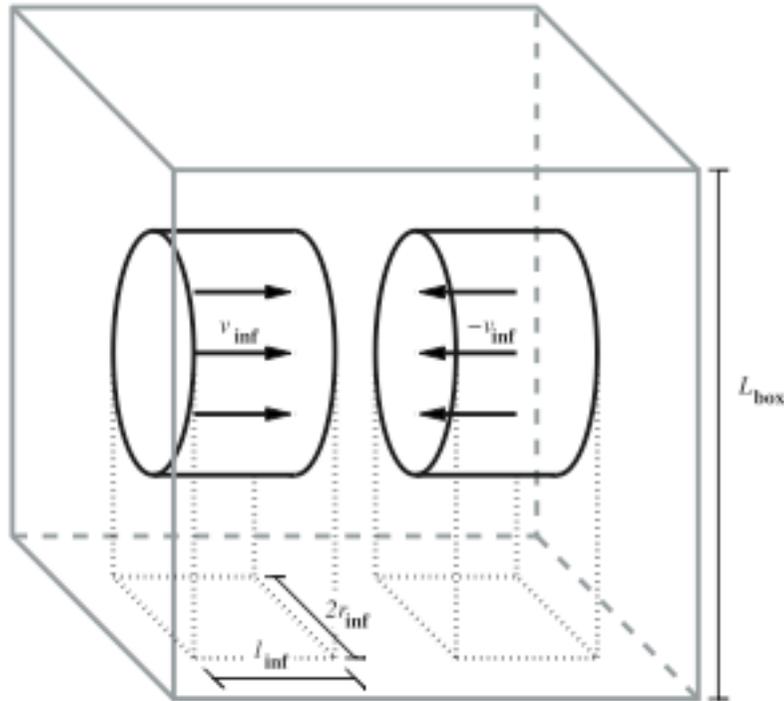
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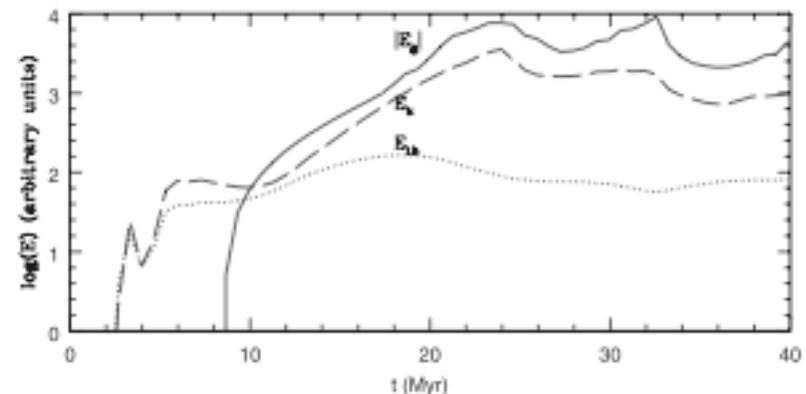
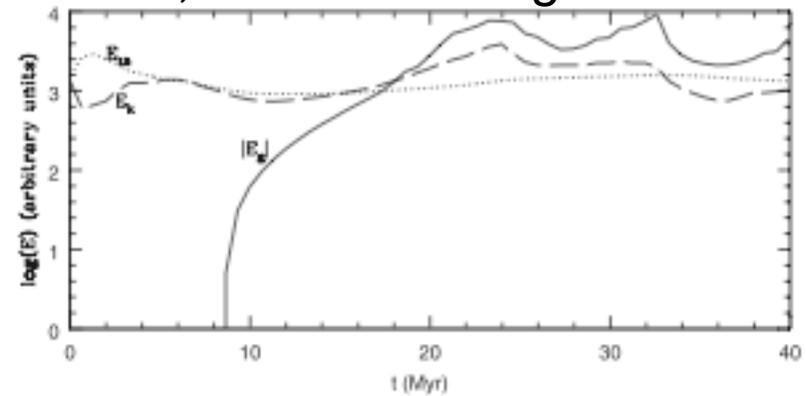
-a fully gravo-turbulent picture

# Star formation in a molecular cloud formed from HI

(Vazquez-Semadeni et al. 07)



## Ekin, Etherm and Egrav



The star formation is starting and happening *while* the cloud is accreting.

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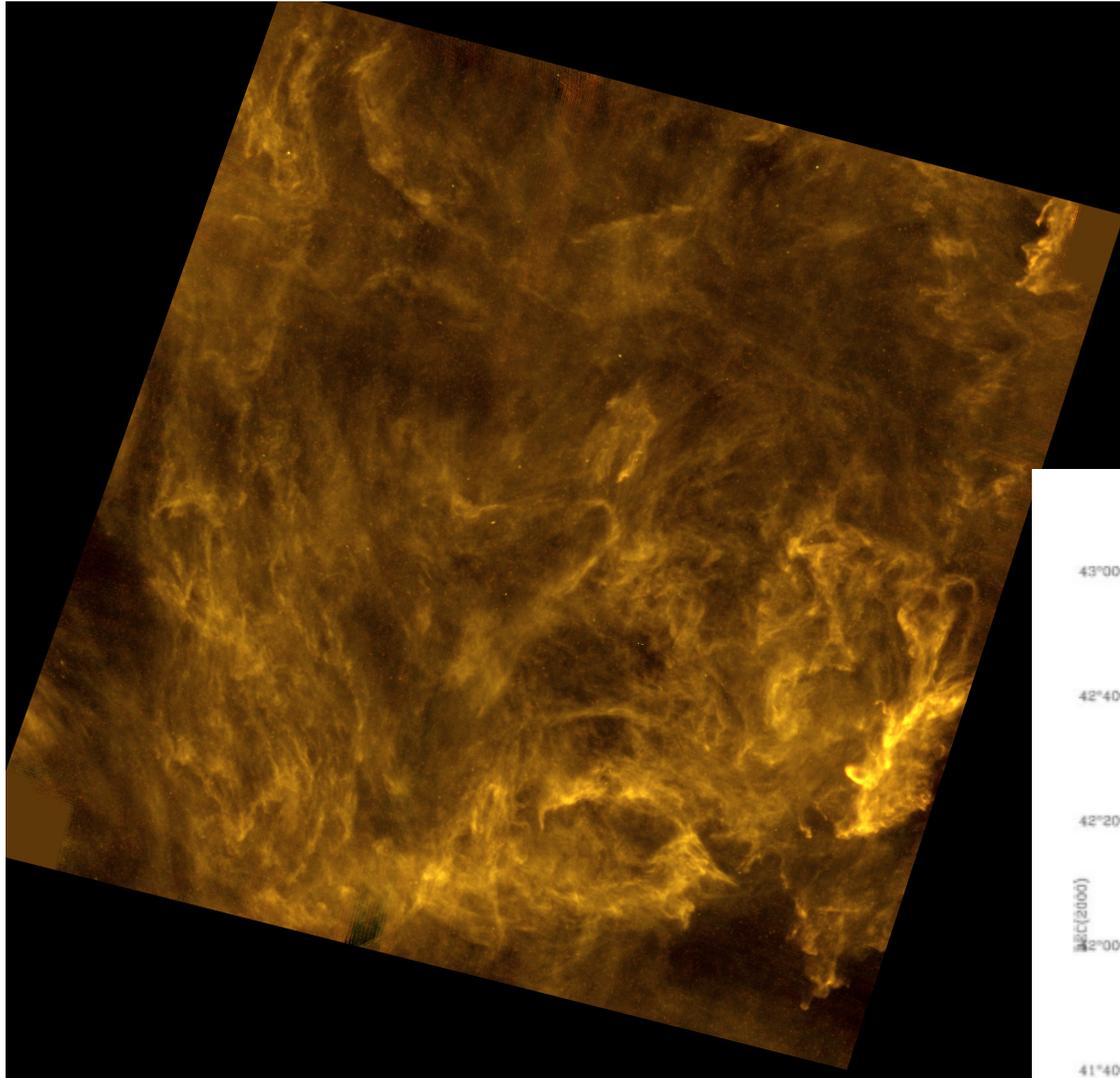
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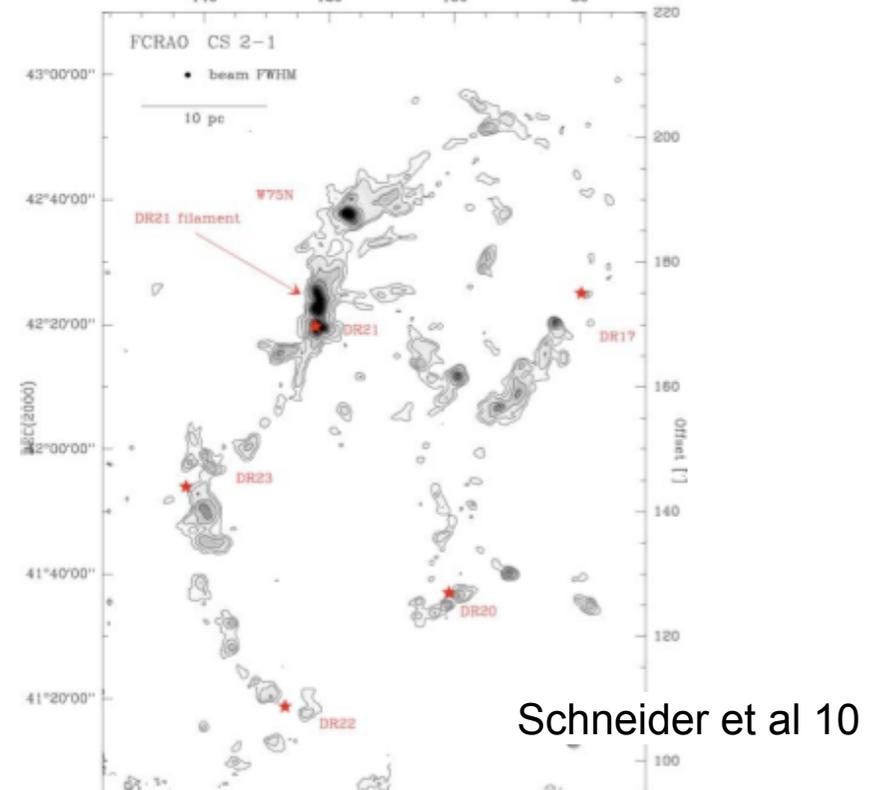
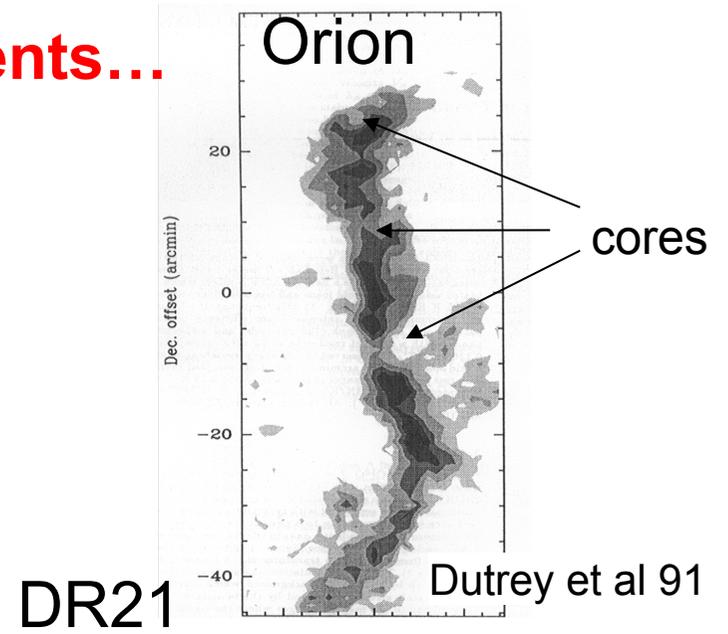
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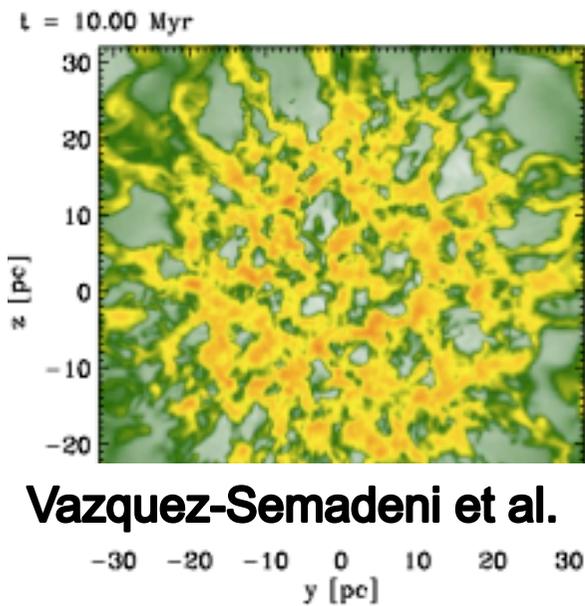
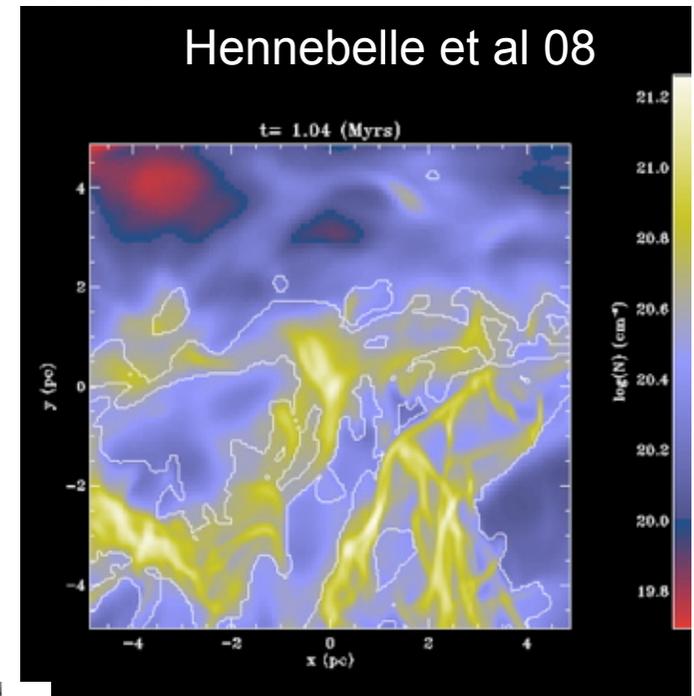
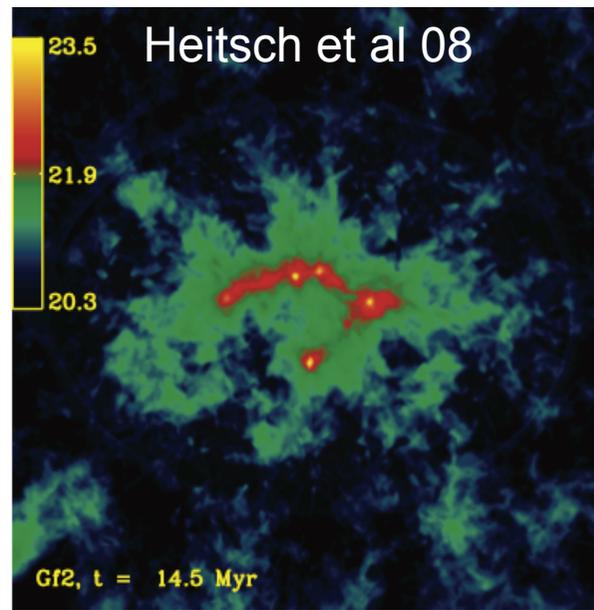
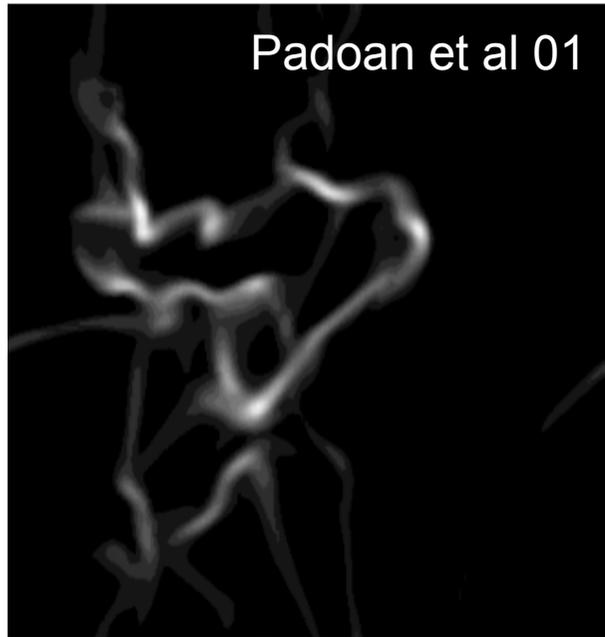
# A large diversity of observed filaments...



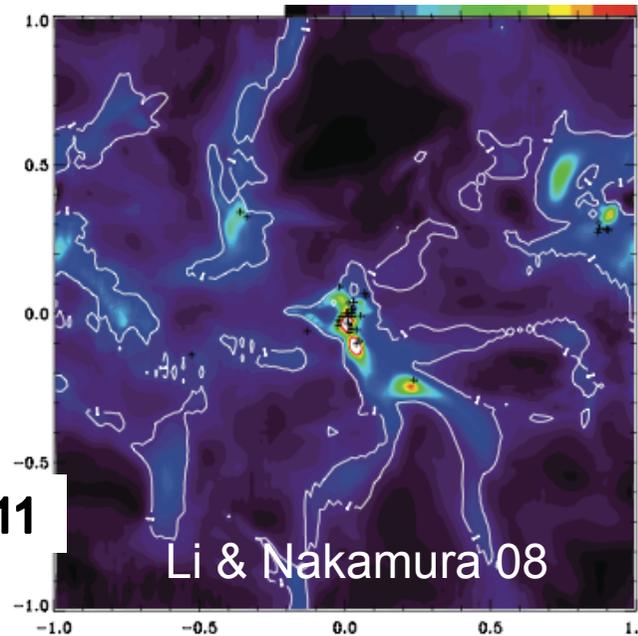
Polaris  
from the Gould belt survey  
André et al. 2010



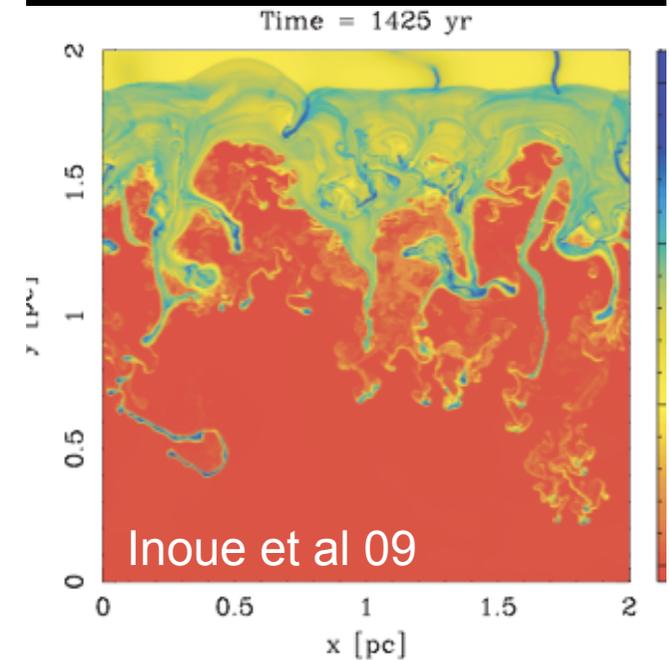
# A large diversity of simulated filaments...



Vazquez-Semadeni et al. 11



Li & Nakamura 08



Inoue et al 09

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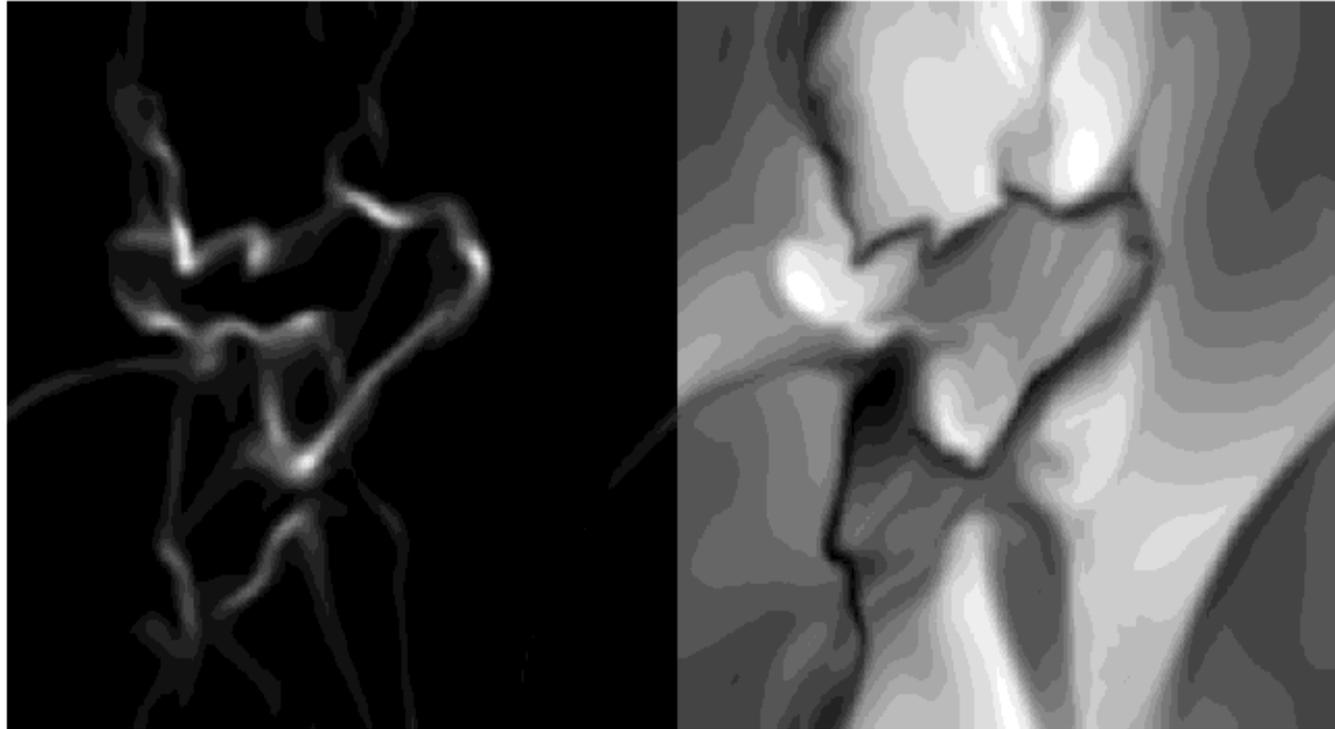
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# Formation of structures induced by turbulence (and not by gravity)

Padoan et al. 01



3D density field

velocity field (norm)

A turbulent molecular cloud (Mach 10).  
Includes the magnetic field (supercritical) but not gravity.

**Proposition: filaments are intersection of shocked sheets**

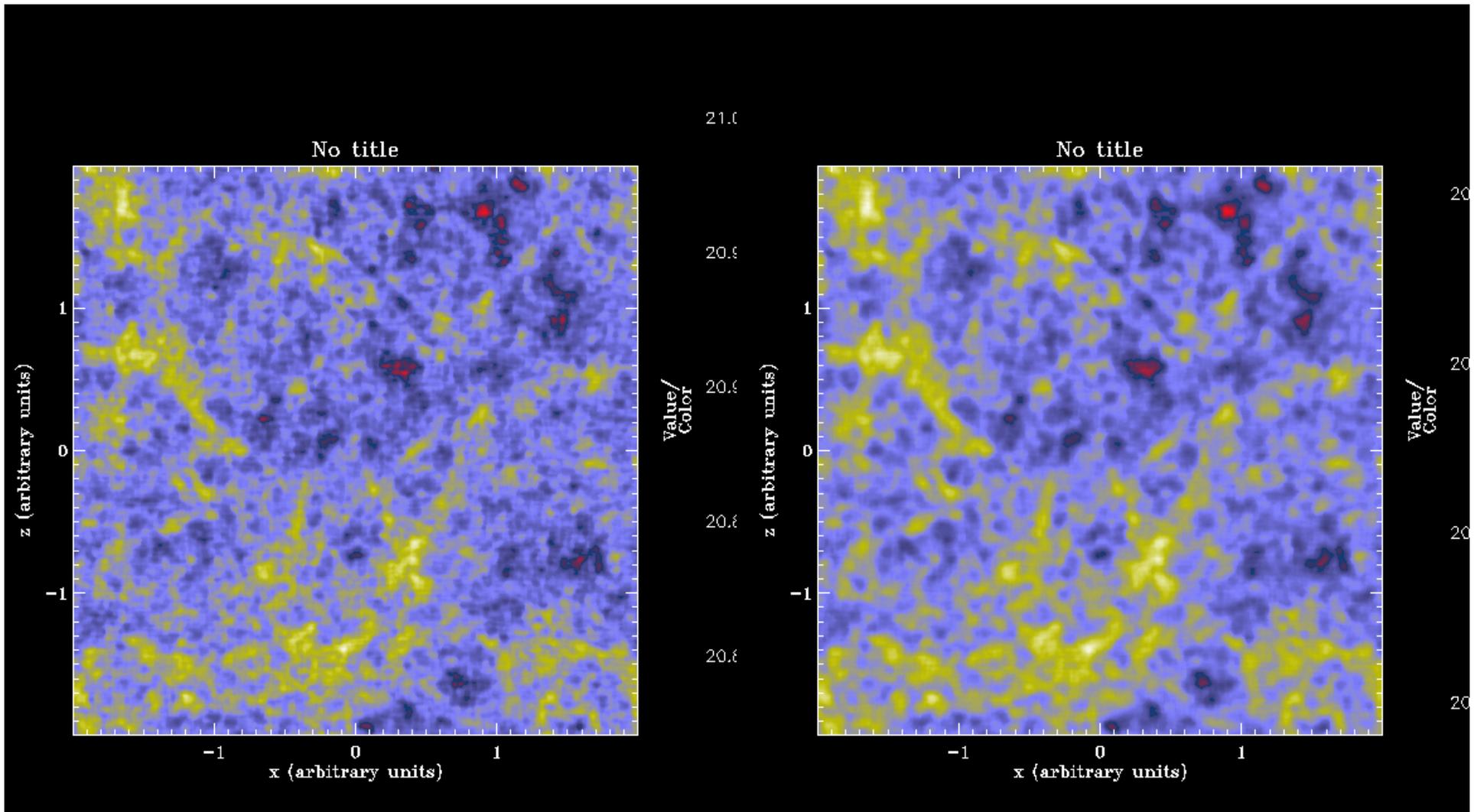
# Comparison between hydro and MHD simulations

Decaying turbulence, 2 phase-medium, no gravity,  $5 \text{ cm}^{-3}$

Initial Mach (wrt cold gas) : 10,  $B=0$  or  $5 \mu\text{G}$

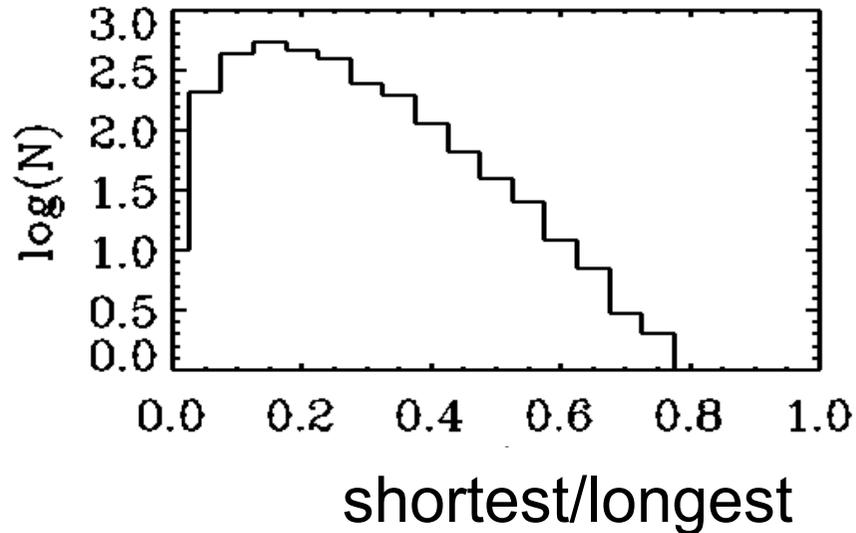
**HYDRO**

**MHD**

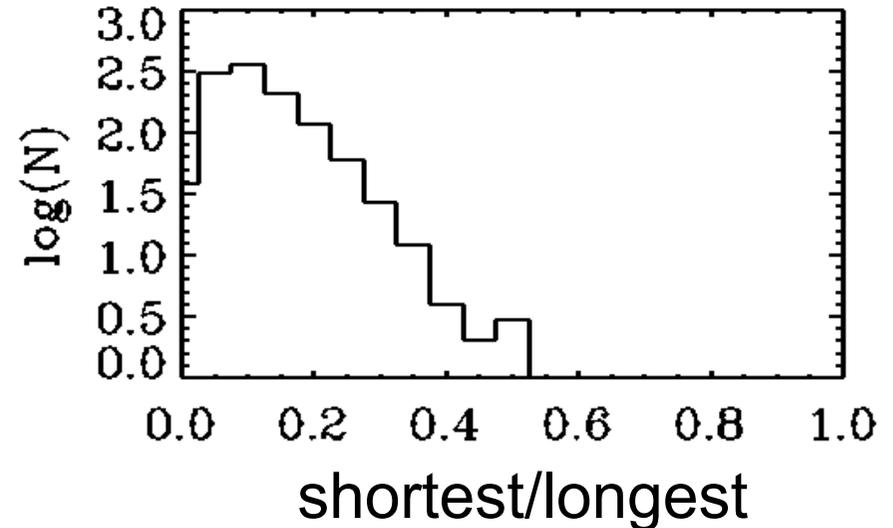


## Aspect ratio of clumps denser than $200 \text{ cm}^{-3}$

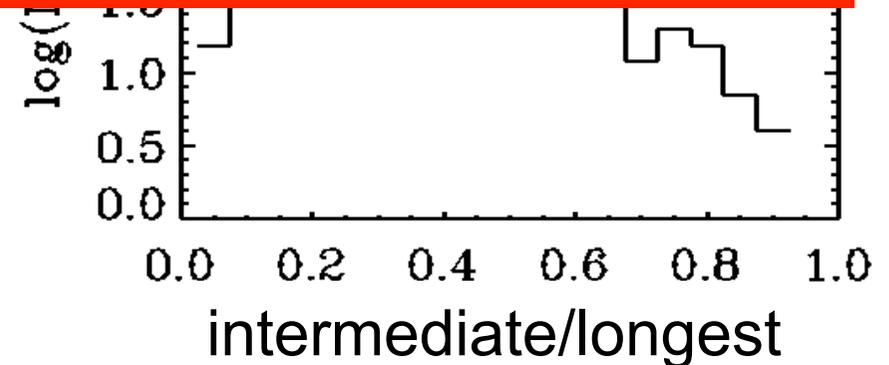
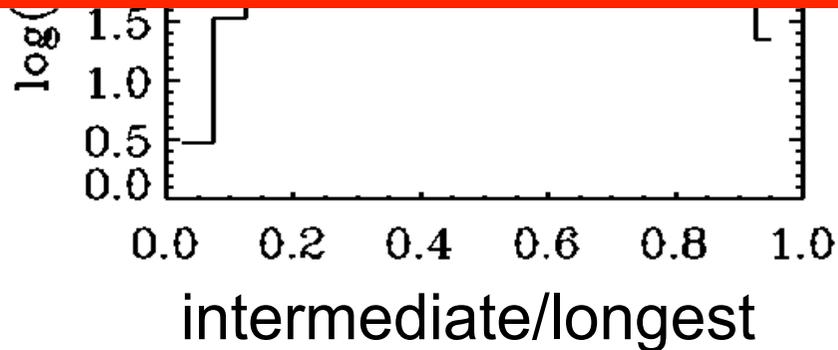
HYDRO



MHD

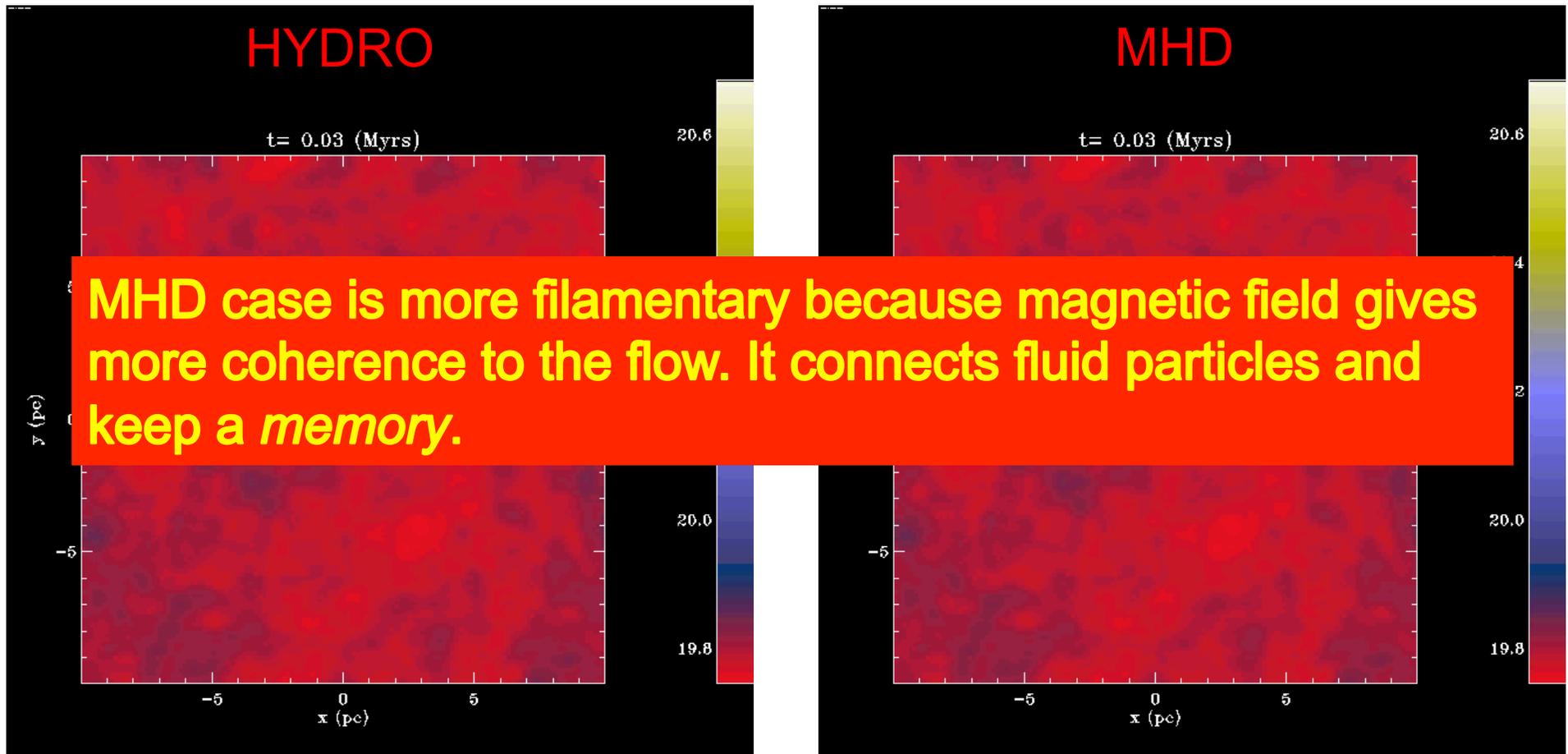
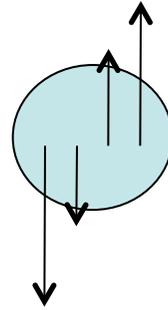


**MHD simulations are more filamentary while magnetic field should reduce the strength of the shocks...**



# Impact of an initial shear

Mach 5 turbulence initially



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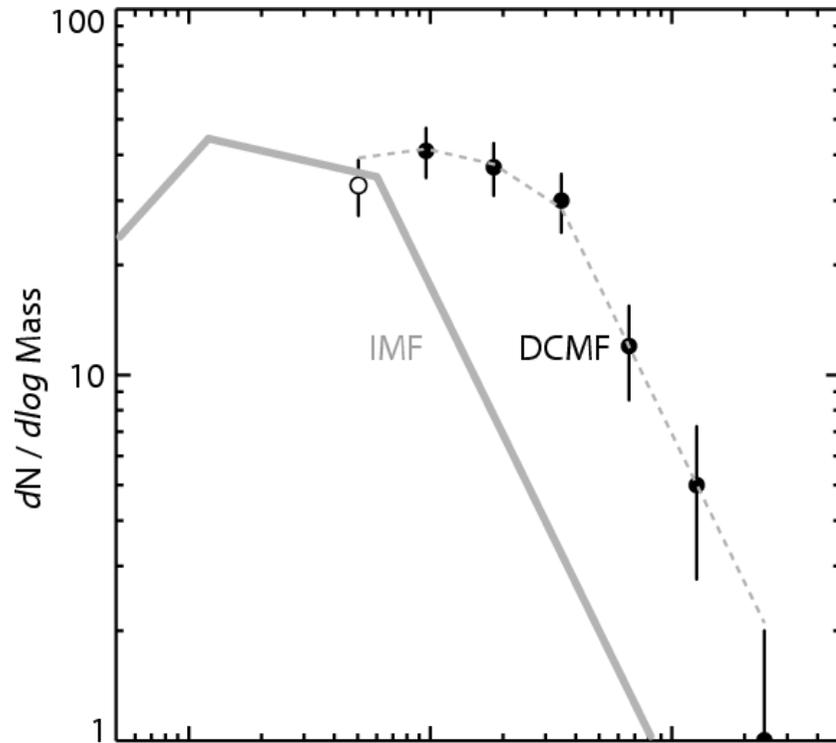
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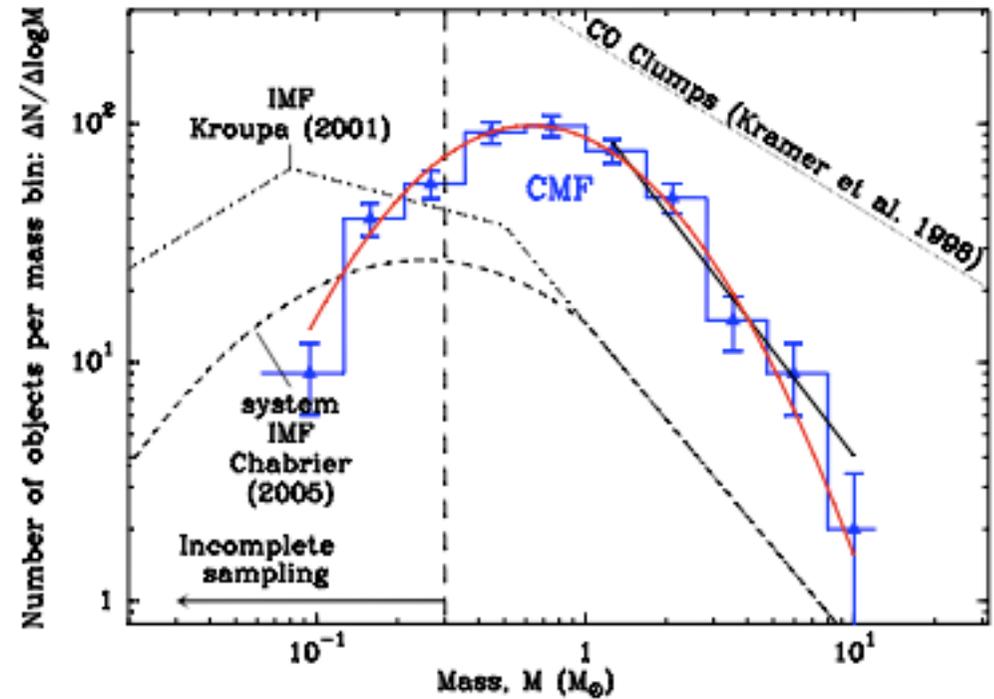
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## Similarity between IMF and CMF

(Motte et al. 1998, Testi & Sargent 1998, Alves et al. 2007, Johnstone et al. 2002, Enoch et al. 2008, Simpson et al. 2008)



Alves et al. 2007



Konyves, André et al. 2010

# Core as density fluctuations created by turbulence and selected by gravity

## Principles of Press-Schechter analysis

Used in cosmology to predict the mass spectrum of DM haloes: => *very successful*

- consider a spectrum of density fluctuations (Gaussian in the cosmological case) characterized by its powerspectrum and smooth it at scale R
- setup a criterion to decide which perturbations have to be considered (collapse time should be smaller than the age of the universe)
- sum over the corresponding fluctuations

## In the case of Molecular clouds

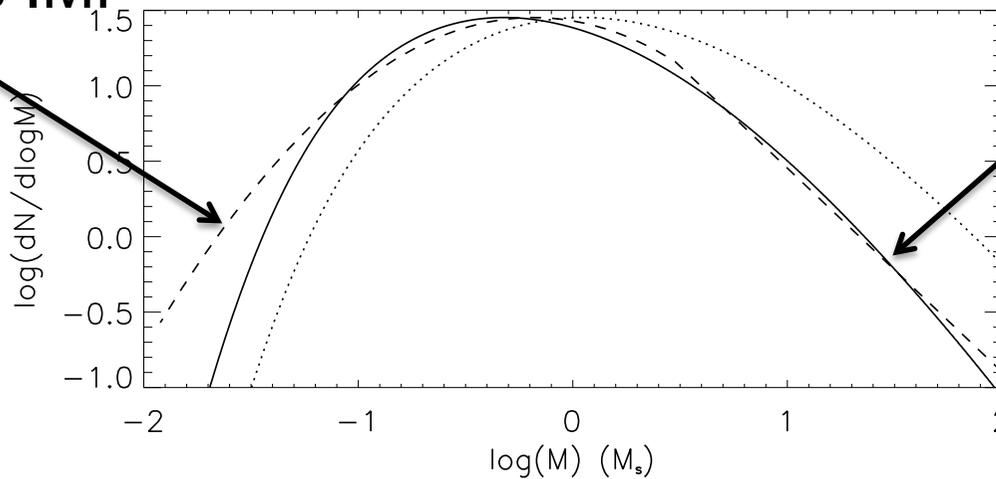
(Padoan et al. 1997, Hennebelle & Chabrier 2008, 2009, 2011, Hosking 2011, 2012)

- assume that the density PDF is log-normal (e.g. Vazquez-Semadeni 1994, Federrath et al. 2011)
- the power-spectrum of  $\log \rho$  is close to Kolmogorov
- consider self-gravitating structures

$$M_{tot}(R) = \bar{\rho} L^3 \int_{\delta_c}^{\infty} \frac{1}{\sqrt{2\pi\sigma(R)^2}} \exp\left(-\frac{\delta^2}{2\sigma(R)^2}\right) d\delta$$
$$= L^3 \int_{M(R)}^{\infty} \frac{dN}{dM'} M' P(M, M') dM'$$

# Comparison between predicted CMF and Chabrier IMF

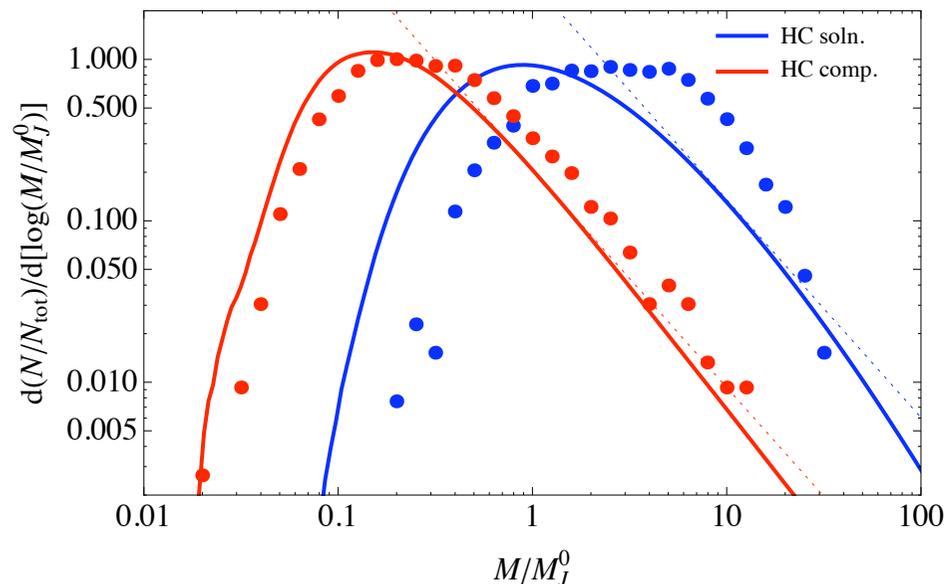
Chabrier's IMF



Analytical prediction

Hennebelle & Chabrier 2008  
Hennebelle & Chabrier in prep

# Comparison with high resolution numerical simulations



Schmidt et al. 2010

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# Fragmentation of sheet into filaments

Classical Jeans analysis:

$$\omega^2 = C_s^2 k^2 - 4\pi G \rho_0$$

The largest mode ( $k=0$ ) has the fastest growth rate.

Could be a problem for forming filaments by gravity but things are different for a self-gravitating sheet.

Linear stability of the self-gravitating sheet  
(Spitzer 78, Nagai et al. 98)

idem:  $k > k_{crit} \Rightarrow \omega^2 > 0$  but for:

$$k \rightarrow 0 \Rightarrow \omega^2 \propto -k^2$$

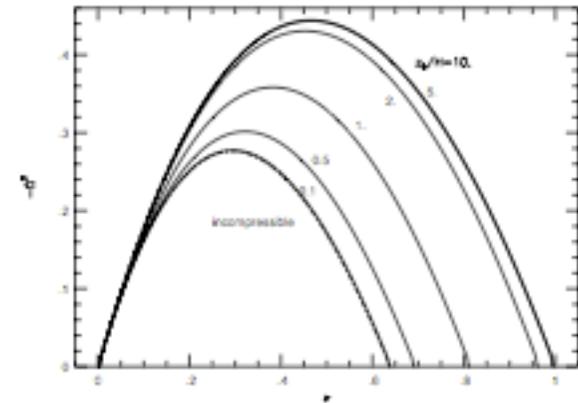
more unstable mode = typical width of the filaments :  $\lambda_J$

=> Fragmentation of a sheet into filaments

Note that Nagai et al. also infer that the orientation of the filaments depend on the magnetic field.

Along the field when  $P_{ext}$  is large and perpendicular to it otherwise.

Dispersion relation



# Fragmentation of sheet into filament

Exact Equilibrium Solutions in 2D (Schmid-Burgk 1976, Myers 2009)

$$\frac{n}{n_c} = \frac{1 - A^2}{[\cosh(z/l_M) + A \cos(x/l_M)]^2},$$

$$l_M \equiv \frac{\sigma}{\sqrt{2\pi G m n_c}}$$

Fragmentation of a sheet into filaments

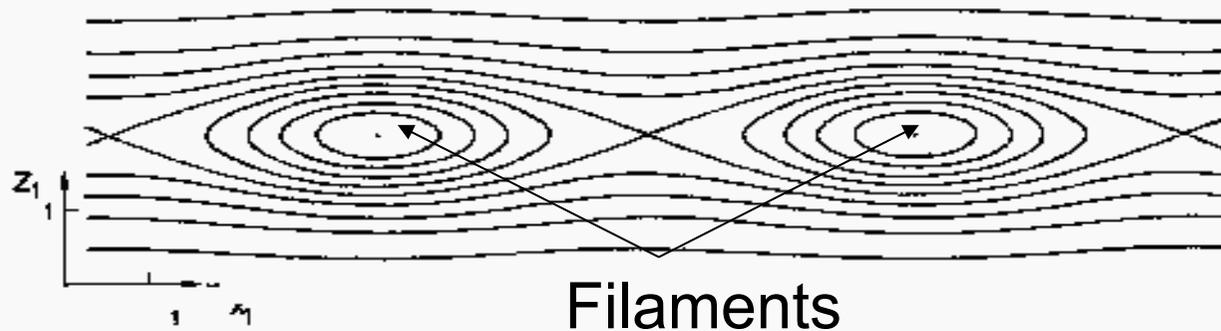


FIG. 1.—Lines of constant density for the case  $A = 0.17$ . Density along neighboring lines differs by  $\rho_{max}/10$

# Fragmentation of Filament in Cores

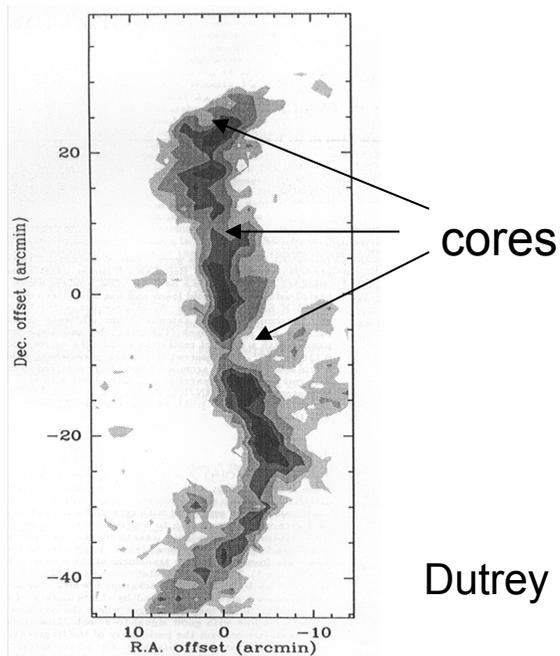
Self-gravitating filaments (Ostriker 64) :

-profile in  $1/r^4$

$$\rho(r) = \rho_0 / (1 + (r/l_0)^2)^2, \quad l_0 = C_s / \sqrt{\pi G \rho_0}$$

as for the self-gravitating sheet there is a more unstable wavelength

Suggest: the dense cores are elongated structures with a spatial period close to the Jeans Length.



Dutrey et al 91

Fig. 1.  $O^{18} O J = 1-0$  integrated area map. Contours levels are 1, 1.7, 2.6, 3.5, 4.2  $K km \cdot s^{-1}$ . The different clumps are roughly delineated by the 2.6  $K km \cdot s^{-1}$  level.

Development of the gravitational instability in a filament:

Formation of an elongated core

Fiege & Pudritz 00

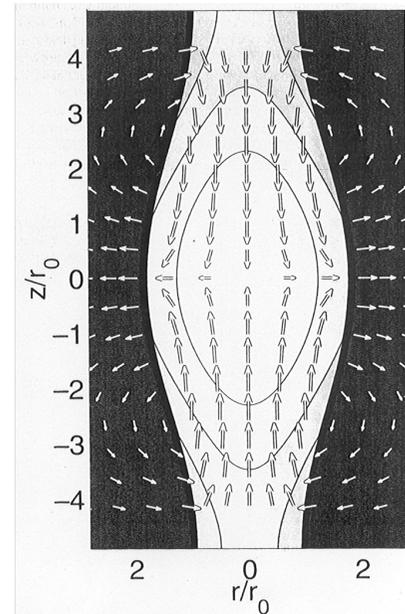


Figure 4. We show the eigenmode corresponding to the most unstable mode of a truncated Ostriker model with mass per unit length  $m/m_0 = \xi$  ( $m/m_{crit} = 0.199$ ). For this mode,  $r_{0k,max} = 0.462$  and  $-\omega^2(4\pi G R)^{-1} = 0.449$ .

# Overview

Formation of molecular clouds from diffuse gas

-observations

-2-phase turbulence

-formation of molecular clouds from diffuse gas

-statistics

-star formation

Formation of filaments and cores within molecular clouds:

-by pure MHD turbulence

-by turbulence but selected by gravity

-by pure gravity

**-a fully gravo-turbulent picture**

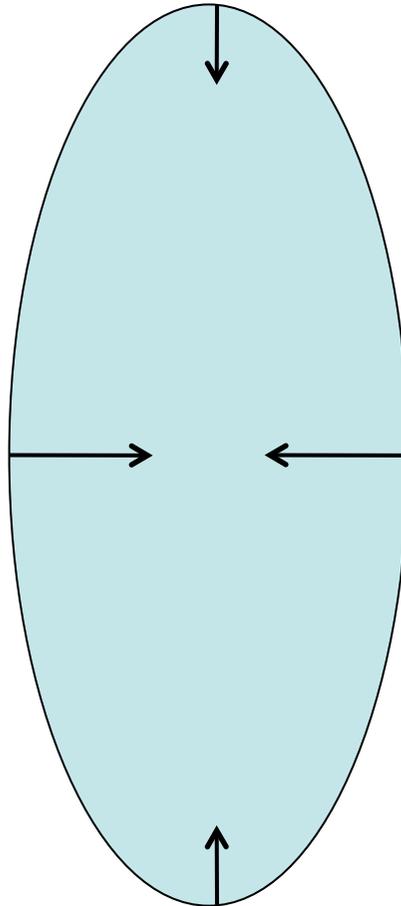
# Gravitational amplification of anisotropies seeded by turbulence

(Mestel et al. 71)

$$F_z \propto \frac{\phi}{l}$$

$$F_r \propto \frac{\phi}{r}$$

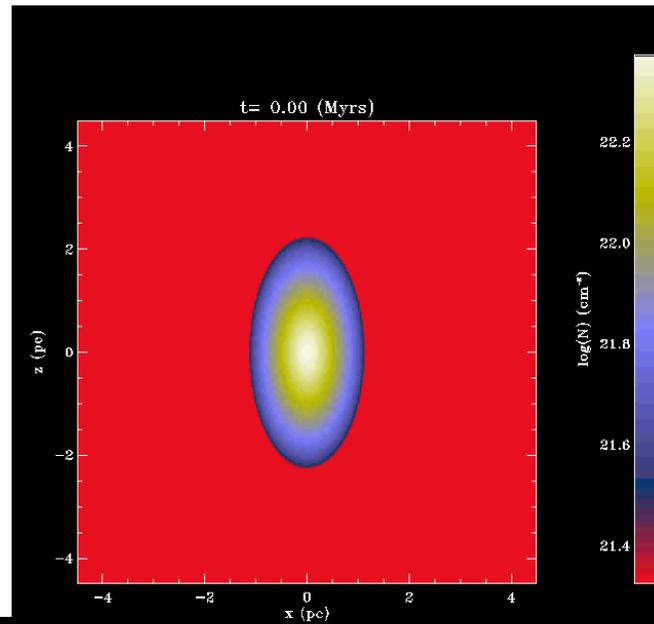
$$\Rightarrow F_z \leq F_r$$



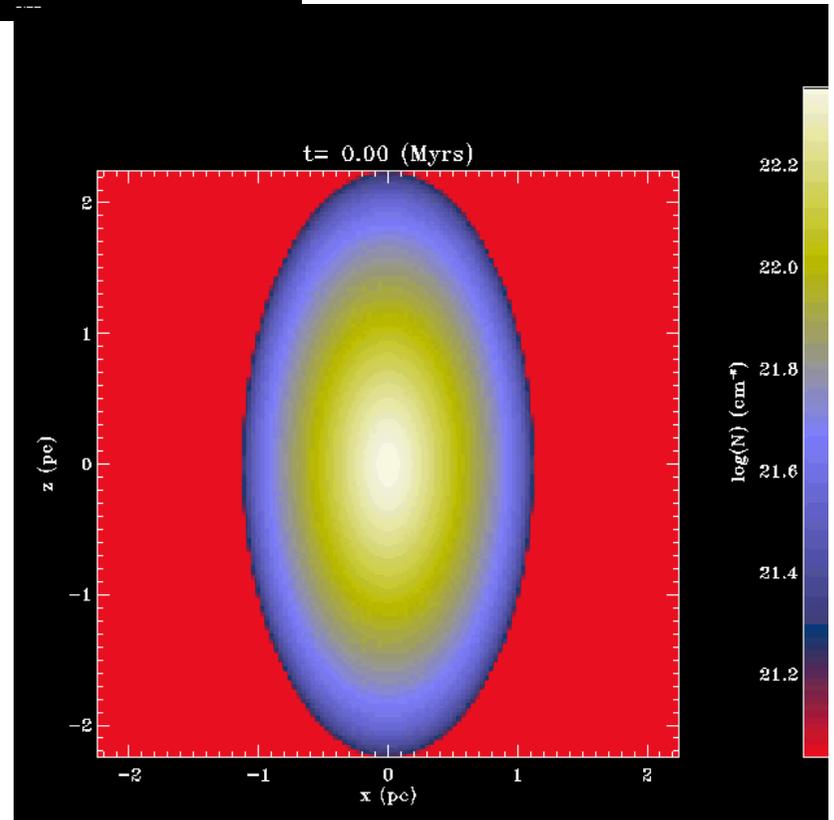
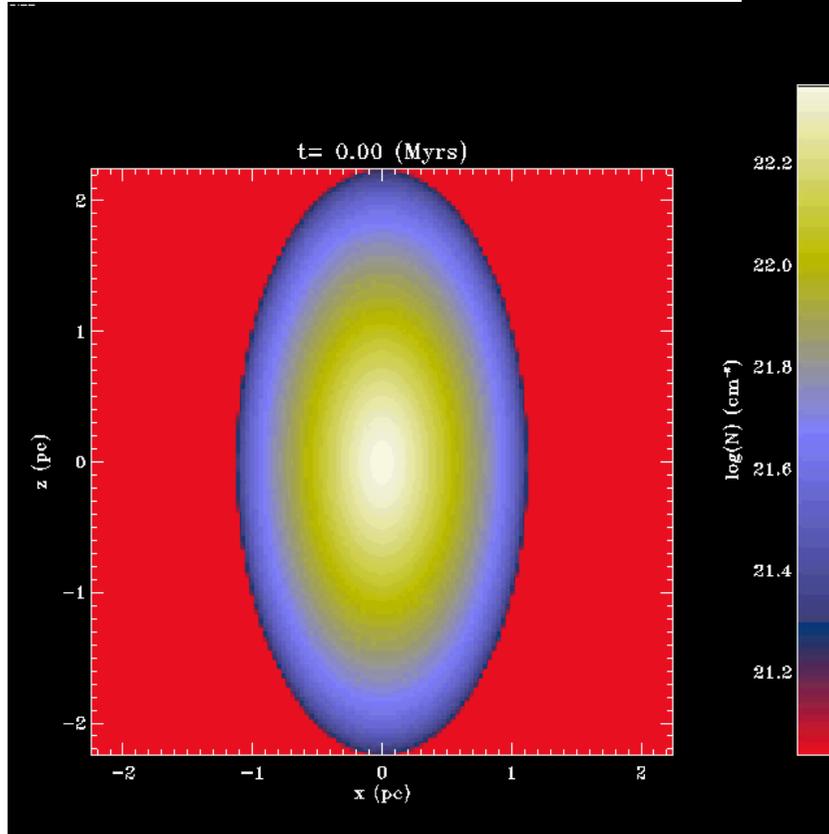
# Formation of filaments by gravitational amplification

Gravity  
No turbulence

Gravity  
Turbulence



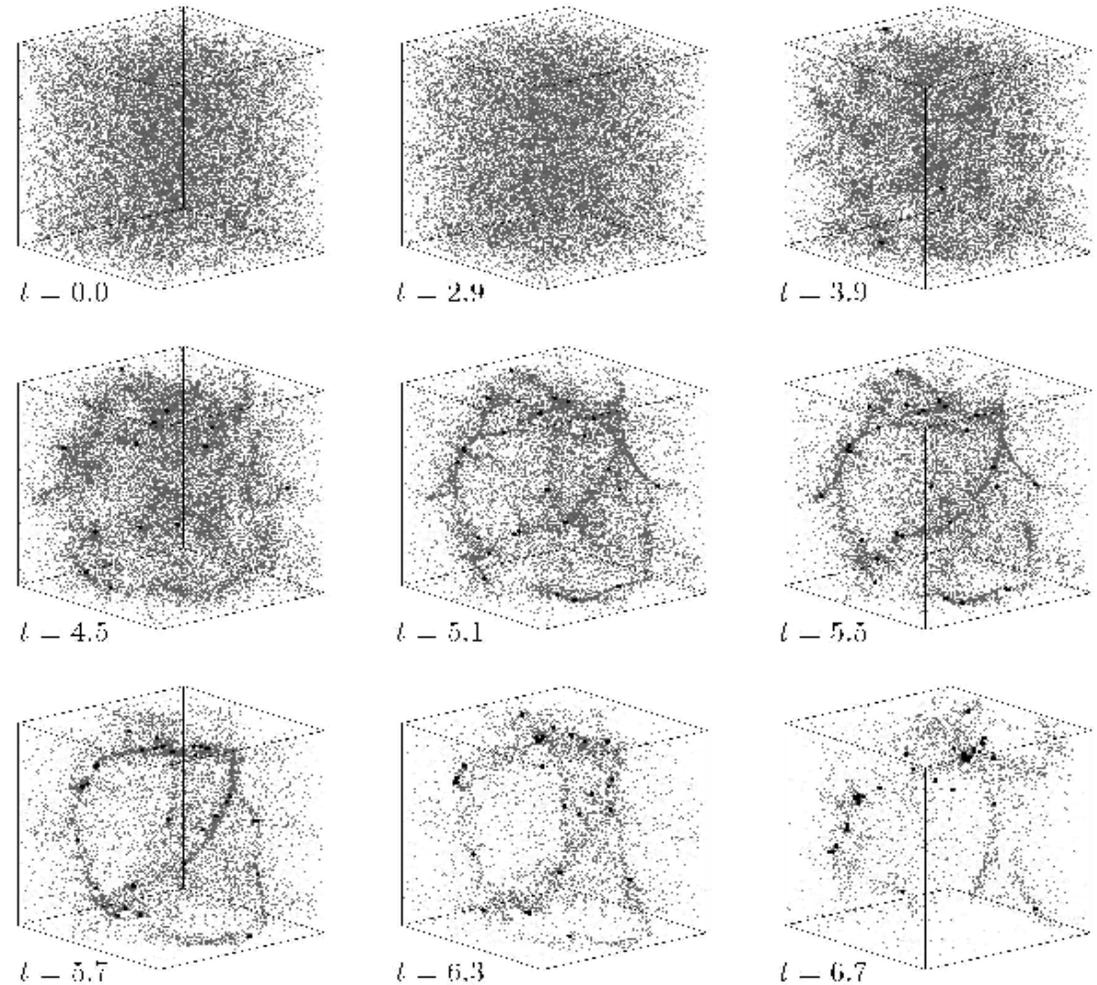
Gravity  
Turbulence  
+MHD



# Formation of filament in gravo-turbulent simulations

Evolution of the density field of a molecular cloud

The calculation (SPH technique) takes gravity into account but not the magnetic field.

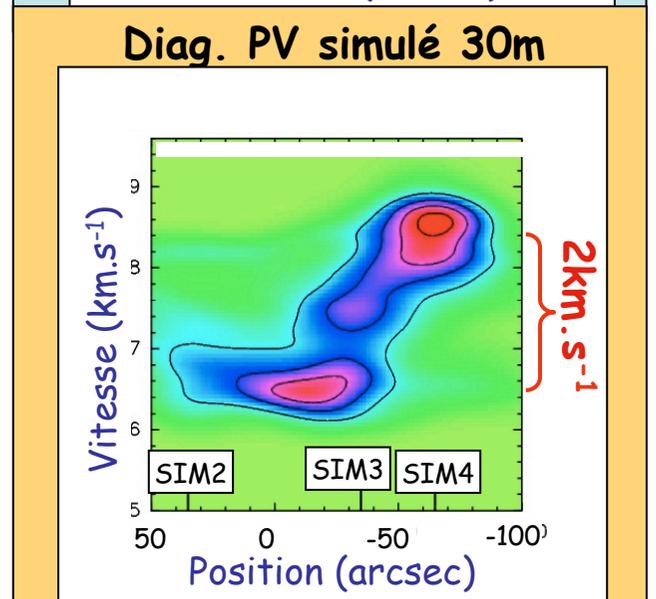
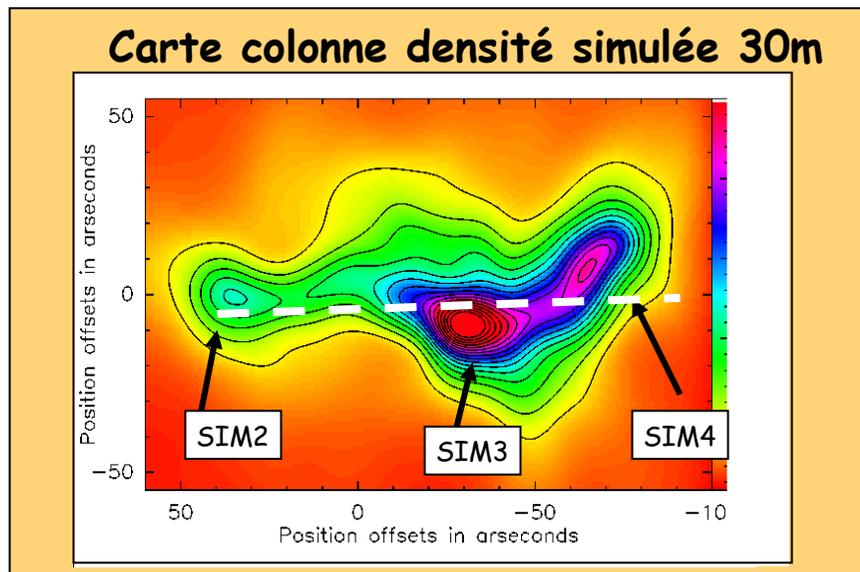
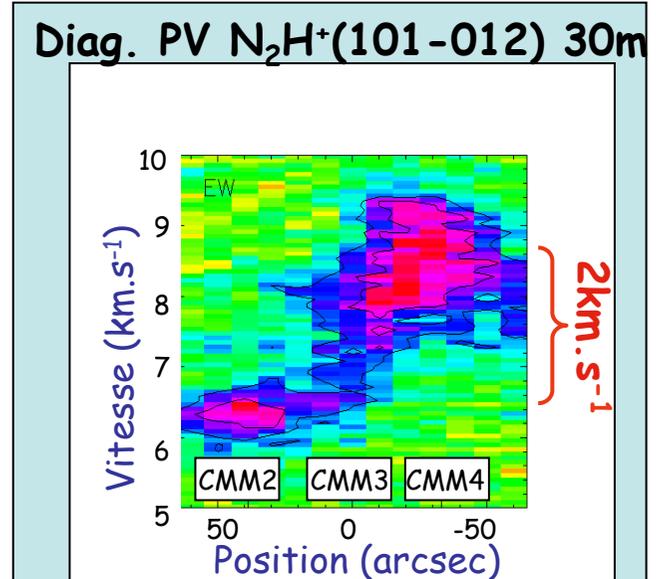
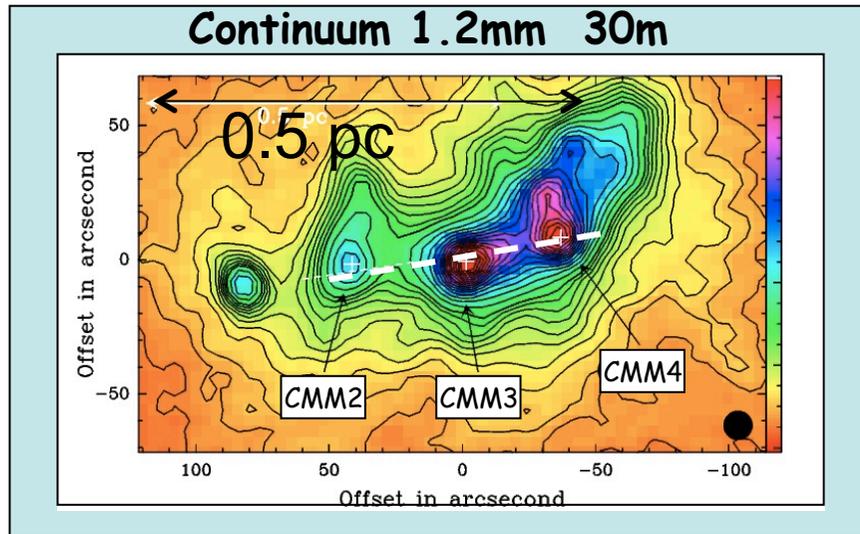


Klessen & Burkert (01) and many others

**Turbulence induces the formation of filaments, which become self-gravitating and collapse**

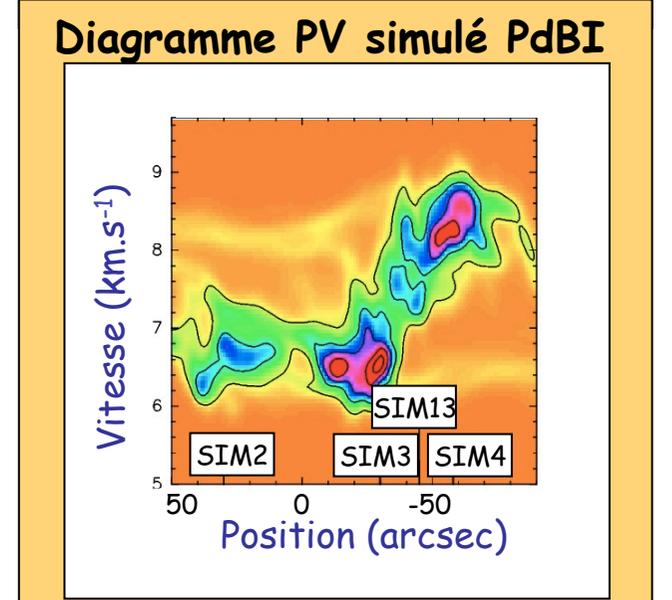
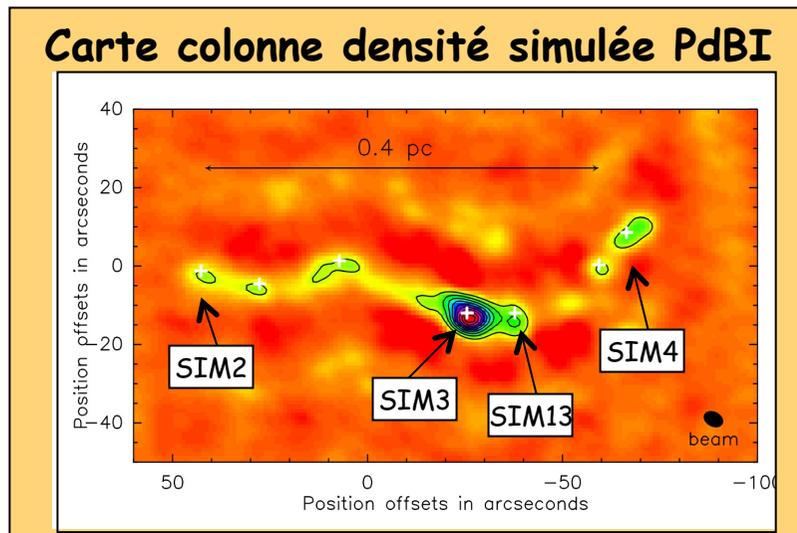
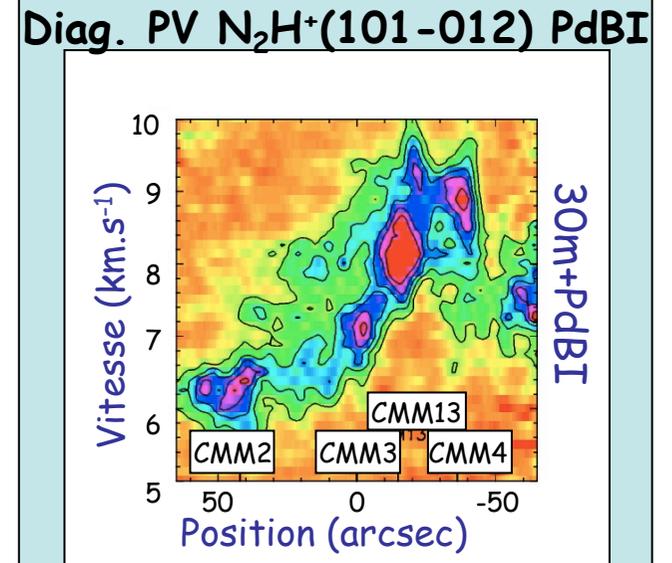
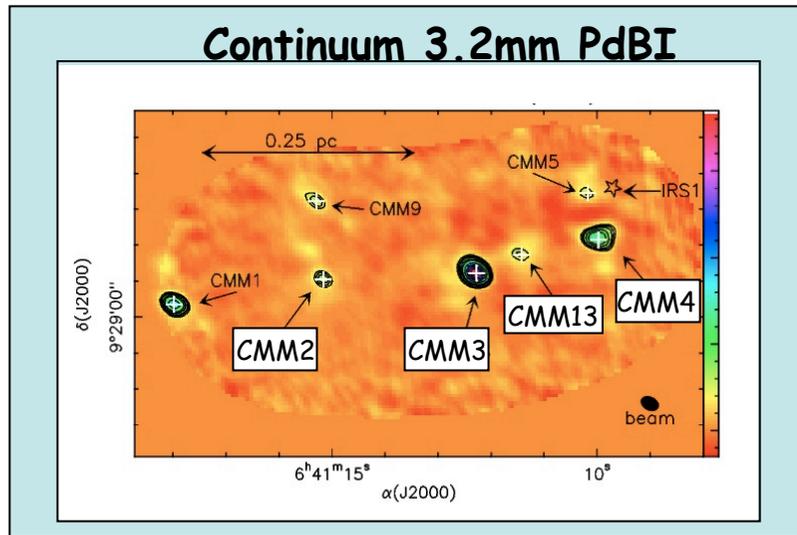
# Comparaisons Observations 30m/Simulations « Best-fit » Simulation

Peretto et al. 2007



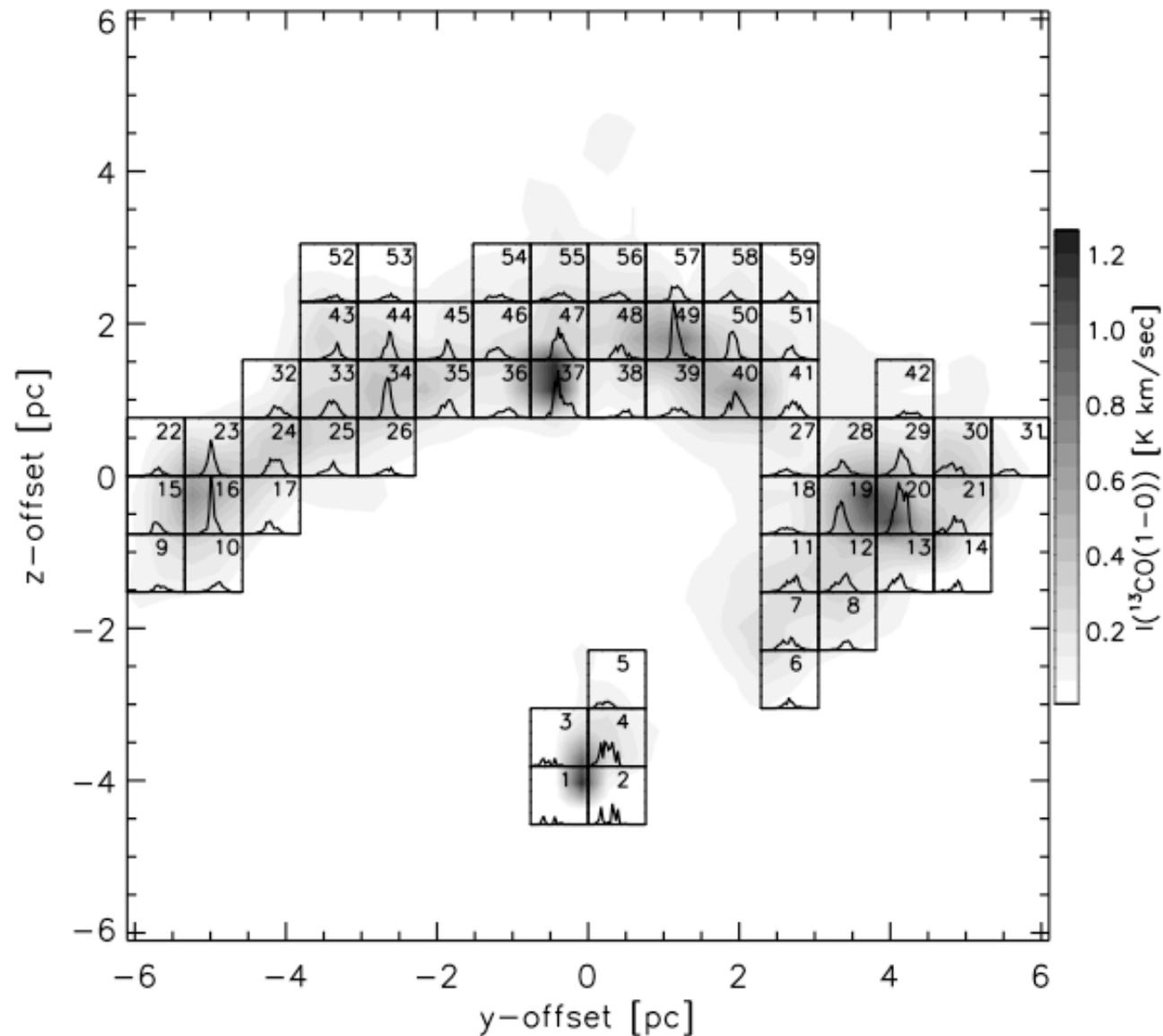
# Comparaisons Observations PdBI

Peretto et al. 2007

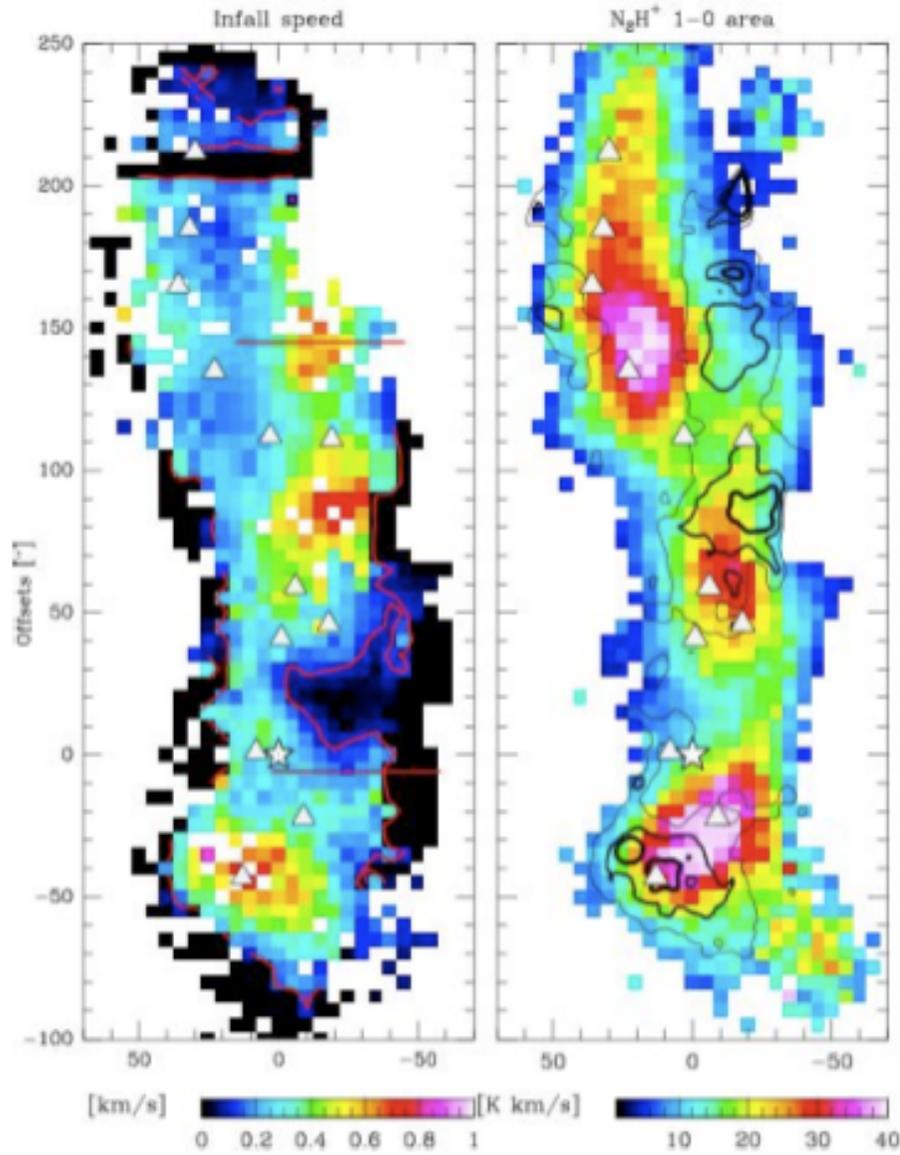


# Modeling and synthetic observations of the Pipe nebula

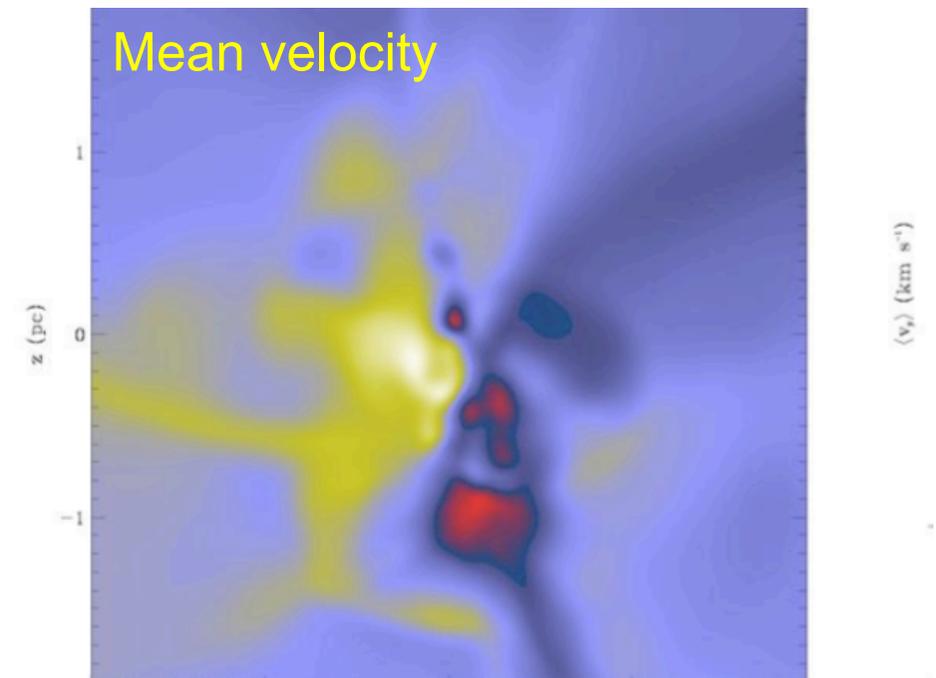
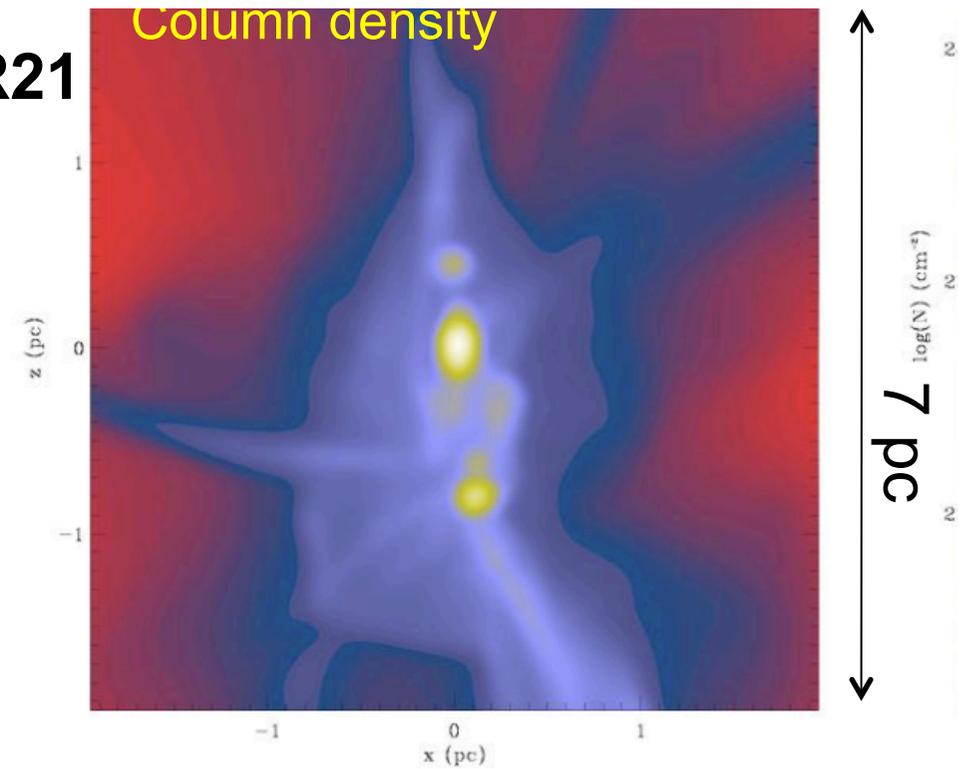
Heitsch et al. 08



# Observations and model of DR21



Schneider et al. 2010



# Conclusion

Numerical simulations suggest that molecular clouds may also have a 2-phase structure (WNM interclump medium)

-Reproduce various statistics of the observed ISM

-In a first phase turbulence is driven by accretion from the outside by the accretion of diffuse HI

***2-phase turbulent accreting flow paradigm ?***

Various regimes and ways to form filaments and cores:

-pure MHD turbulence (role of the shear and of B) forms filaments

-selection by gravity of turbulent density fluctuations forms core

-gravitational fragmentation can form filaments from layers and cores from filaments

-observations suggest some filaments (NGC2264c, Pipe, DR21 ?) are globally collapsing while fragmenting